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Analytic energy gradients in combined second order Møller-Plesset perturbation theory and conductorlike polarizable continuum model calculation

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The analytic energy gradients in combined second order Møller-Plesset perturbation theory and conductorlike polarizable continuum model calculations are derived and implemented for spin-restricted closed shell (RMP2), Z-averaged spin-restricted open shell (ZAPT2), and spin-unrestricted open shell (UMP2) cases. Using these methods, the geometries of the S0 ground state and the T1 state of three nucleobase pairs (guanine-cytosine, adenine-thymine, and adenine-uracil) in the gas phase and aqueous solution phase are optimized. It is found that in both the gas phase and the aqueous solution phase the hydrogen bonds in the T1 state pairs are weakened by \(\sim 1\) kcal/mol as compared to those in the S0 state pairs. © 2011 American Institute of Physics. [doi:10.1063/1.3649947]

I. INTRODUCTION

Dielectric solvation models\(^1\) are often used to estimate the average solvent effect on molecular structures and properties in solutions. The polarizable continuum models (the earlier DPCM (Ref. 2) and the more recent IEFPCM (Ref. 3)), conductorlike screening models (COSMO (Ref. 4) and GCOSMO (Ref. 5) or CPC (Ref. 6)), SS(V)PE (Ref. 7) models and SMx models\(^8\) are representative continuum solvation models. The conductorlike polarizable continuum model (CPCM) can be considered either as a high-dielectric limit of the more general IEFPCCM or a specific version of COSMO. Recently, we derived and implemented rigorous analytic CPCCM gradient for Hartree-Fock (HF), density functional theory (DFT), multiconfiguration self-consistent-field (MCSCF), generalized valence bond theory (GVB), and time-dependent DFT (TDDFT) methods.\(^9,10\)

In this work, we focus on second order Møller-Plesset perturbation theory (MP2) methods, including the spin-restricted closed shell RMP2, spin-unrestricted open shell UMP2, and the Z-averaged spin-restricted open shell ZAPT2 methods.\(^11,12\) The MP2 methods are accurate quantum chemical methods for recovering electron correlation energy. Except for a few cases such as aromatic ring stacking, large basis set MP2 calculation is able to give very accurate structures and intermolecular interaction energies for molecules and clusters consisting of H, C, N, and O atoms. Pople et al.\(^13\) derived and implemented the MP2 analytic gradient.\(^13\) Handy and Schaefer formulated the Z-vector method so MP2 gradient and some other molecular properties can be evaluated efficiently.\(^14\) The ZAPT2 analytic gradient was derived and implemented by Fletcher et al.\(^15\) and Aikens and co-workers.\(^16,17\)

Cammi et al.\(^18\) established a closed shell RMP2-PCM method that uses RHF-PCM orbitals and their energies to obtain the second order energy correction $E^{(2)}$. They also derived

and implemented a Z-vector method to determine the RMP2-PCM relaxed density and analytic gradient. To the best of our knowledge, PCM methods have not been combined with open shell MP2 methods such as ZAPT2 and UMP2. In this paper, an extension of Cammi et al.’s RMP2-PCM method to ZAPT2 and UMP2 is described. These methods are used to study the S0 and T1 states of acetone, nucleobases, and nucleobase pairs.

II. THEORY

A. MP2-CPCM gradient

The RMP2-PCM method established by Cammi et al.\(^18\) can be generalized to UMP2 and ZAPT2 methods such that the corresponding restricted Hartree–Fock (RHF)-PCM, unrestricted Hartree–Fock (UHF)-PCM, and restricted open Hartree–Fock (ROHF)-PCM orbitals and orbital energies are used to obtain the second order energy correction $E^{(2)}$, which is added to the corresponding HF-PCM energy.

Here, the RMP2-PCM, UMP2-PCM, and ZAPT2-PCM methods are considered. For all of these methods, the first derivative (gradient) of the second order energy correction $E^{(2)}$ with respect to a coordinate $x$ can be written in density matrices and basis function integrals:\(^19\)

$$
E^{(2),x} = -\sum_{\mu\nu} W^{(2)}_{\mu\nu} c^x_{\mu\nu} + \sum_{\mu\nu} \rho^{(2)}_{\mu\nu} h^x_{\mu\nu} + \sum_{\mu\nu\rho\sigma} \rho^{(2)}_{\mu\nu\rho\sigma} \Gamma^{NS}_{\mu\nu\rho\sigma} (\mu\rho|\nu\sigma)^x + \sum_{\mu\nu\rho\sigma} \rho^{(2)}_{\mu\nu\rho\sigma} (V^T_{\mu\nu} q_N)^x + \sum_{\mu\nu\rho\sigma} \rho^{(2)}_{\mu\nu\rho\sigma} (V^T_{\mu\nu} q_\sigma)^x,
$$

(1)

where $\mu$, $\nu$, $\rho$, and $\sigma$ are spin-orbital basis functions; $(\mu\rho|\nu\sigma)$ is the standard antisymmetrized two-electron integrals in the $(12)|12$ notation; $h$ is the one-electron integral; $S$ is the overlap integral; $W^{(2)}$ is the MP2 correction to the HF
energy-weighted density matrix; \( \mathbf{P} \) is the HF density matrix; \( \mathbf{P}^{(2)} \) is the MP2 correction to the HF density matrix, which can be determined via a modified Z-vector method (to be discussed below); \( \Gamma_{\mu\nu}^{NS} \) is the nonseparable two-particle density matrix. Here, \( \mathbf{V} \) is a set (vector) of electrostatic potentials at the molecular surface points created by the electron density of the basis set product; the superscript \( T \) denotes transpose here and hereafter; \( \mathbf{q} \) is a set (vector) of induced surface charges (\( \mathbf{q}_s \) due to nuclei and \( \mathbf{q}_{\sigma} \) due to electron density of the basis set product). All \( \mathbf{q} \) and \( \mathbf{V} \) satisfy the linear CPCM equation

\[
\mathbf{C} \cdot \mathbf{q} = -(1 - 1/\varepsilon) \mathbf{V}.
\]

(2)

The elements of the matrix \( \mathbf{C} \) are \( C_{ij} = 1.07 \sqrt{4\pi/\varepsilon_i} \) and \( C_{ij} = 1/(r_i - r_j) \), with \( \varepsilon_i \) being the area and \( r_i \) being the center coordinates of surface tessera \( i \). Here, \( \varepsilon \) is the dielectric constant of the solvent. Scaling factors other than \( (1 - 1/\varepsilon) \) were also suggested.4,6,20

The four first terms in Eq. (1) have exactly the same forms as those in the regular MP2 energy gradient formula.14

The last two terms in Eq. (1) can be written as

\[
\sum_{\mu\nu} P^{(2)}_{\mu\nu} (V_{\mu\nu} q_N)^x + \sum_{\mu\nu} P^{(2)}_{\nu\rho} \sum_{\rho\sigma} P^{(2)}_{\nu\sigma} (V_{\mu\nu} q_{\sigma})^x
\]

\[
= (V^{(2),x})^T q_N + \left( \frac{\varepsilon}{\varepsilon - 1} \right) (q^{(2)} )^T C^x q_N + (q^{(2)} )^T V_N^x
\]

\[
+ \left( \frac{\varepsilon}{\varepsilon - 1} \right) (q^{(2)} )^T C^x q_{HF} + (q^{(2)} )^T V_{HF}^x
\]

\[
= (V^{(2),x})^T (q_N + q_{HF}) + \frac{1}{2} \left( \frac{\varepsilon}{\varepsilon - 1} \right) (q^{(2)} )^T C^x (q_N + q_{HF})
\]

\[
+ (q^{(2)} )^T (V_N + V_{HF}) \tag{3}
\]

where \( V^{(2),x} \) is the electrostatic field created by \( \mathbf{P}^{(2)} \), \( q^{(2)} \) is the CPCM surface charge induced by the electrostatic potential created by \( \mathbf{P}^{(2)} \),

\[
q^{(2)} = \sum_{\mu\nu} P^{(2)}_{\mu\nu} q_{\mu\nu}^x.
\]

(5)

The first term in the final expression of Eq. (3) represents the force between \( q_N + q_{HF} \) (surface charge induced by nuclei and HF density \( \mathbf{P} \)) and the MP2 relaxed electron density \( \mathbf{P}^{(2)} \); The second term represents the force between \( q_N + q_{HF} \) and \( q^{(2)} \); the third term represents the force between \( q^{(2)} \) and solute nuclei, and the force between \( q^{(2)} \) and the HF electron density \( \mathbf{P} \).

The evaluation of Eq. (3) requires the derivatives of the tesserae coordinates and areas with respect to molecular geometric change. In the fixed points with variable areas (FIFXPA; Ref. 9) tessellation scheme, the positions of the surface tesserae are fixed relative to their center atoms so the tessera areas are smooth functions of their distances to neighboring spheres. Therefore, smooth and rigorous analytic derivatives of the tessera positions and areas with respect to atomic coordinates can be obtained.

### B. Z-vector equations

Cammi et al. showed that by taking into account induced surface charges, the Z-vector method originally developed by Handy and Schaefer14 can be used to determine the \( \mathbf{P}^{(2)} \) for RMP2-PCM methods.18 In this work, we extended the Z-vector method to open shell UMP2-PCM and ZAPT2-PCM methods. We follow the notations in several recent literature papers: the doubly occupied molecular orbitals are denoted as \( i, j, \) and \( k \), the singly occupied ones are denoted as \( x \) and \( y \), the virtual ones are denoted as \( a, b, \) and \( c \), general molecular orbitals (both occupied and virtual) are denoted as \( p \) and \( q \).

For closed shell RMP2, the occupied-occupied and virtual-virtual blocks of the \( \mathbf{P}^{(2)} \) can be readily evaluated using the RMP2 excitation amplitudes. The occupied-virtual blocks of \( \mathbf{P}^{(2)} \), when written as a vector (Lagrange multiplier), can be determined using the Z-vector equation14

\[
\sum_{b_j} A_{ai bj} P_{b j}^{(2)} = (\varepsilon_a - \varepsilon_i) P_{ai}^{(2)} = L_{ai} \tag{6}
\]

Here \( A_{ai bj} = (ij)|ab \rangle \langle ib|aj \rangle \) is the orbital Hessian matrix, \( \varepsilon_a \) and \( \varepsilon_i \) are the orbital energies, and \( \mathbf{L} \) is the Lagrangian.14 For RMP2-PCM, induced charge terms should be added to the orbital Hessian matrix \( \mathbf{A} \) and the Lagrangian \( \mathbf{L} \), and the occupied-occupied block of the \( \mathbf{W}^{(2)} \) matrix,

\[
A_{ai bj}^{pcm} = A_{ai bj} + 2 V_{ai}^T q_{bj},
\]

\[
L_{ai}^{pcm} = L_{ai} + \sum_{jk} P_{jk}^{(2)} V_{ai}^T q_{jk} + \sum_{bc} P_{bc}^{(2)} V_{ai}^T q_{bc},
\]

\[
W_{ij}^{(2), ppcm} = W_{ij}^{(2)} - \frac{1}{2} \sum_{pq} P_{pq}^{(2)} V_{ij}^T q_{pq} \tag{9}
\]

For open shell UMP2, two associated Z-vector equations for \( \alpha \) and \( \beta \) orbitals should be solved (see Eqs. (99) and (100) in Ref. 17). For UMP2-PCM, induced charge terms should be added to the orbital Hessian matrix \( \mathbf{A} \) (see Eqs. (91)–(94), (99), and (100) in Ref. 17), the Lagrangian \( \mathbf{L} \) (see Eq. (98) in Ref. 17), and the occupied-occupied block of the \( \mathbf{W}^{(2)} \) matrix (see Eq. (96) in Ref. 17),

\[
A_{\alpha i \beta j}^{pcm} = A_{\alpha i \beta j} + 2 V_{\alpha i}^T q_{\beta j},
\]

\[
L_{\alpha i}^{pcm} = L_{\alpha i} + \sum_{jk} P_{\alpha j \beta k}^{(2)} V_{\alpha i}^T q_{\beta k} + \sum_{bc} P_{\alpha c \beta b}^{(2)} V_{\alpha i}^T q_{\beta c},
\]

\[
L_{\beta i}^{pcm} = L_{\beta i} + \sum_{jk} P_{\beta j \alpha k}^{(2)} V_{\beta i}^T q_{\alpha k} + \sum_{bc} P_{\beta c \alpha b}^{(2)} V_{\beta i}^T q_{\alpha c},
\]

\[
W_{\alpha i \beta j}^{(2), ppcm} = W_{\alpha i \beta j}^{(2)} - \frac{1}{2} \sum_{pq} P_{\alpha p \beta q}^{(2)} V_{\alpha i \beta j}^T q_{pq} \tag{11}
\]

\[
W_{\beta i \alpha j}^{(2), ppcm} = W_{\beta i \alpha j}^{(2)} - \frac{1}{2} \sum_{pq} P_{\beta p \alpha q}^{(2)} V_{\beta i \alpha j}^T q_{pq} \tag{12}
\]
Here, only the α equations are given. The β equations can be obtained by switching α and β.

For open shell ZAPT2, a single Z-vector equation can be constructed using a nine-block (but only six independent blocks) orbital Hessian matrix A for doubly occupied, singly occupied and virtual orbitals (see Figure 3 in Ref. 16),

\[
\begin{pmatrix}
A_{xi,yj} & A_{xi,bj} & A_{xi,by} \\
A_{ai,yj} & A_{ai,bj} & A_{ai,by} \\
A_{ax,yj} & A_{ax,bj} & A_{ax,by}
\end{pmatrix}
\begin{pmatrix}
P_{xy} \\
P_{bj} \\
P_{by}
\end{pmatrix}
= \begin{pmatrix}
L_{xi} \\
L_{ai} \\
L_{ax}
\end{pmatrix}.
\]

(13)

For ZAPT2-CPCM, induced charge terms should be added to the orbital Hessian matrix A (see Eq. (14) in Ref. 16), the Lagrangian L (see Eq. (62)–(66) in Ref. 16) and the double-double, single-single and single-single blocks of the \(W^{(2)}\) matrix (see Eq. (55)–(61) in Ref. 16),

\[
\begin{align*}
A_{xi,yj}^{pcm} &= A_{xi,yj} + V_{xy} T q_{xi}, \\
A_{xi,bj}^{pcm} &= A_{xi,bj} + 2V_{ib} T q_{ai}, \\
A_{xi,by}^{pcm} &= A_{xi,by} + V_{ib} T q_{ax}, \\
A_{ai,yj}^{pcm} &= A_{ai,yj} + 4V_{ib} T q_{ai}, \\
A_{ai,bj}^{pcm} &= A_{ai,bj} + 2V_{ib} T q_{ax}, \\
A_{ax,yj}^{pcm} &= A_{ax,yj} + V_{by} T q_{ax}, \\
A_{ax,bj}^{pcm} &= A_{ax,bj} + 2V_{by} T q_{ax}, \\
A_{ax,by}^{pcm} &= A_{ax,by} + V_{by} T q_{ax},
\end{align*}
\]

(14)

For frozen core MP2 calculations, corresponding modifications can be made following the expressions in Refs. 16 and 17.

C. Solvation energy correction

The MP2-CPCM energy is the sum of the HF-CPCM energy and the second order energy correction \(E^{(2)}\). The advantage of using this formulation is that the analytic gradient can be derived. The disadvantage is that the CPCM solvation energy is obtained with the HF density instead of MP2 relaxed density. Here, we describe a simple method to obtain the solvation energy using the MP2 relaxed density. In the sense of perturbation theory, the solvation energy obtained using the second order relaxed density is actually at the fourth order.

The solvation energy at the HF level is defined as

\[
G_{sol}^{HF} = \frac{1}{2} (V_N + V_{HF})^T (q_N + q_{HF}) + \frac{1}{2} (V_N + V_{HF})^T (q^{(2)})
\]

(17)

where \(V_N\) and \(q_w\) are the potential and induced charges created by the nuclei, \(V_{HF}\) and \(q_{HF}\) are the potential and induced charges created by the HF electron density.

Similar to Eq. (17), a solvation energy \(G_{sol}^{MP2}\) can be defined using the MP2 relaxed density,

\[
G_{sol}^{MP2} = \frac{1}{2} (V_N + V_{HF} + V^{(2)})^T (q_N + q_{HF} + q^{(2)})
\]

\[
= \frac{1}{2} (V_N + V_{HF})^T (q_N + q_{HF}) + \frac{1}{2} (V_N + V_{HF})^T (q^{(2)})
\]

\[
+ \frac{1}{2} (V^{(2)})^T (q_N + q_{HF}) + \frac{1}{2} (V^{(2)})^T (q^{(2)}).
\]

Here, \(V^{(2)}\) and \(q^{(2)}\) are the potential and induced charges created by \(P^{(2)}\). The \(G_{sol}^{HF}\) defined in Eq. (17) for HF-CPCM calculation is the first term in Eq. (18). The second and third terms in Eq. (18) are equal to each other and can be combined. We can choose to use the third term (doubled). Therefore, the correction of the solvation energy due to \(P^{(2)}\) is

\[
G_{sol}^{(2)} = G_{sol}^{MP2} - G_{sol}^{HF}
\]

\[
= (V^{(2)})^T (q_N + q_{HF}) + \frac{1}{2} (V^{(2)})^T (q^{(2)})
\]

\[
= (V^{(2)})^T (q_N + q_{HF} + \frac{1}{2} q^{(2)}).
\]

(19)

It is difficult to derive the expression of the analytic nuclear gradient for \(G_{sol}^{MP2}\) or \(G_{sol}^{(2)}\). Therefore, Eq. (19) is best used as a single point energy correction.

III. IMPLEMENTATION AND COMPUTATIONAL METHODOLOGY

The MP2-CPCM gradient code was implemented by the authors in the GAMESS (Ref. 21) package based on several gas phase MP2 programs and the CPCM code previously implemented by Li and Jensen22 on the basis of the IEFPCM program originally implemented by Mennucci et al.3,23,24 The MP2 programs include the serial RMP2 and UMP2 program,12 the parallel RMP2 program implemented by Fletcher et al.,25 the parallel RMP2 program implemented by Ishimura et al.,26 the parallel ZAPT2 program implemented by Fletcher et al.15 and Aikens et al.,16 and the parallel UMP2 program implemented by Aikens and coworkers.17,27 Numerical tests using the FIXPVA (Ref. 9) testset calculation for CPCM show that the accuracy of the analytic gradients obtained with GAMESS default settings is typically \(10^{-6}\) hartree/bohr. Tightening the default settings leads to better accuracies such as \(10^{-7}\) hartree/bohr, suggesting that the implementations are correct. Using FIXPVA, the
TABLE I. Energies (hartree) of acetone computed using the aug-cc-pVTZ basis set. The gas phase results in each case are based on the MP2-CPCM optimized geometry in the case. CPCM effect is in kcal/mol.

<table>
<thead>
<tr>
<th>Method</th>
<th>$E^{\text{HF}}$</th>
<th>$E^{(2)}$</th>
<th>$E^{\text{MP2}}$</th>
<th>$G^{(2)}_{\text{sol}}$</th>
<th>$E^{\text{MP2}} + G^{(2)}_{\text{sol}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMP2 gas phase</td>
<td>−192.035264</td>
<td>−0.825358</td>
<td>−192.860622</td>
<td>0</td>
<td>−192.860622</td>
</tr>
<tr>
<td>RMP2-CPCM</td>
<td>−192.048094</td>
<td>−0.822840</td>
<td>−192.870934</td>
<td>−0.002789</td>
<td>−192.873724</td>
</tr>
<tr>
<td>CPCM effect</td>
<td>−8.05</td>
<td>+1.58</td>
<td>−6.47</td>
<td>−1.75</td>
<td>−8.22</td>
</tr>
<tr>
<td>ZAPT2 gas phase</td>
<td>−191.942713</td>
<td>−0.769660</td>
<td>−192.712173</td>
<td>0</td>
<td>−192.712373</td>
</tr>
<tr>
<td>ZAPT2-CPCM</td>
<td>−191.948211</td>
<td>−0.769946</td>
<td>−192.718157</td>
<td>+0.000527</td>
<td>−192.717630</td>
</tr>
<tr>
<td>CPCM effect</td>
<td>−3.45</td>
<td>−0.18</td>
<td>−3.63</td>
<td>+0.33</td>
<td>−3.30</td>
</tr>
<tr>
<td>UMP2 gas phase</td>
<td>−191.951690</td>
<td>−0.763264</td>
<td>−192.714954</td>
<td>0</td>
<td>−192.714954</td>
</tr>
<tr>
<td>UMP2-CPCM</td>
<td>−191.957147</td>
<td>−0.763617</td>
<td>−192.720765</td>
<td>+0.00593</td>
<td>−192.720172</td>
</tr>
<tr>
<td>CPCM effect</td>
<td>−3.42</td>
<td>−0.22</td>
<td>−3.65</td>
<td>+0.37</td>
<td>−3.27</td>
</tr>
</tbody>
</table>

MP2-CPCM potential energy surfaces are rigorously continuous and smooth. Equation (19) was also implemented. The $E^{\text{MP2}} + G^{(2)}_{\text{sol}}$ energy is printed out as “EMP2 + EPCM(2)” in the GAMESS output file.

In the CPCM calculations, spheres with radii of 0, 2.124, 2.016, and 1.908 Å (after scaled by 1.20) were used for H, C, N, and O atoms, respectively, to define the molecular cavity; no additional spheres were used. Using zero radii for H atoms means that they do not contribute to form the surface. The tessellation scheme FIXPVA was used with 240 initial tesserae per sphere. The induced surface charges were determined by a semi-iterative DIIS procedure\textsuperscript{24,28} with no charge renormalization. A dielectric constant $\varepsilon = 78.39$ was used to represent water solvent. Only the CPCM electrostatic solvation energy was included in these calculations. The aug-cc-pVTZ and aug-cc-pVDZ basis set\textsuperscript{29} were used for acetone and nucleobases, respectively. Geometry optimization was performed in internal coordinates generated by the automatic delocalized coordinates algorithm.\textsuperscript{30} No symmetry was imposed in the geometry optimization.

The $T_1$ excited states of acetone, cytosine, thymine, and uracil can be well described using coupled cluster linear response theory because they are dominated by single excitation of the partial negative charges on the O atom. The ZAPT2 optimized carbonyl C=O bond lengths are 1.327 Å in the gas phase and 1.327 Å in water. The UMP2 optimized bond lengths are 1.325 Å in the gas phase and 1.327 Å in water. The 0.002 Å lengthening of the C=O bond in water is probably due to the CPCM stabilization of the partial negative charges on the O atom. The $T_1$ triplet state acetone optimized using the gas phase RHF method has a trigonal planar skeleton. The $T_1$ triplet state acetone optimized using the gas phase ZAPT2 and UMP2 and the solution phase ZAPT2-CPCM and UMP2-CPCM shows a trigonal pyramidal skeleton. In general, the geometries in the gas phase and water are very similar to each other for the same electronic state.

IV. RESULTS AND DISCUSSION

A. Acetone $S_0$ and $T_1$ states

Acetone is used as a simple example to illustrate the MP2-CPCM methods.

The $S_0$ ground state acetone optimized using the gas phase MP2 and solution phase MP2-CPCM has a trigonal planar skeleton. The $T_1$ triplet state acetone optimized using the gas phase ZAPT2 and UMP2 and the solution phase ZAPT2-CPCM and UMP2-CPCM shows a trigonal pyramidal skeleton. In general, the geometries in the gas phase and water are very similar to each other for the same electronic state. The RMP2 optimized carbonyl C=O bond lengths are 1.215 Å in the gas phase and 1.222 Å in water, respectively. The 0.007 Å lengthening of the C=O bond is probably due to the CPCM stabilization of the partial negative charges on the O atom.

The energies calculated using HF and MP2 methods for acetone are listed in Table I. As expected, CPCM always leads to some solvation energy for the variational HF methods. This should be true for all molecules. The CPCM implicitly affects $E^{(2)}$ by affecting the HF orbitals and orbital energies. The CPCM effects in $E^{(2)}$ can be positive and negative, depending on how the orbitals and orbital energies are affected. Since $E^{(2)}$ typically contains thousands to millions terms, it is very difficult to determine which terms are more important. $G^{(2)}_{\text{sol}}$ can be either positive or negative. For $S_0$ acetone, $G^{(2)}_{\text{sol}}$ is $-0.002789$ hartree or $-1.75$ kcal/mol. We used RHF and RMP2 methods to calculate the dipole moments of gas phase acetone in $S_0$ state optimized with the RMP2 method. The RHF and RMP2 results are 3.46 and 2.98 Debye, respectively. If only the dipole moment is considered, a larger dipole moment at the RHF level of theory should cause an
overestimation of the magnitude of the CPCM solvation energy, and the $G_{sol}^{(2)}$ should be positive. Therefore, the dipole moment along cannot be used to explain the negative $G_{sol}^{(2)}$.

The analytic gradient of $G_{sol}^{(2)}$ is not available. Geometry optimized on the potential energy surface of EMP$_2$ [i.e., $E_{HF} + E^{(2)}$ in both the gas phase and CPCM solution phase] is not necessary the minimum point on the potential energy surface of EMP$_2 + G_{sol}^{(2)}$. Various tests show that $G_{sol}^{(2)}$ is virtually a constant near a minimum point on the potential energy surface of EMP$_2$, so the minimum point is virtually the minimum point on the potential energy surface of EMP$_2 + G_{sol}^{(2)}$. Table II lists the EMP$_2$ and EMP$_2 + G_{sol}^{(2)}$ of the last seven steps in the geometry optimization process of S$_0$ acetone with the RMP2-CPCM method and that of the T$_1$ acetone with the ZAPT2-CPCM method. Clearly, $G_{sol}^{(2)}$ is very close to a constant. In the RMP2-CPCM case, the minimum on the EMP$_2$ surface has an EMP$_2 + G_{sol}^{(2)}$ energy that is $5.8 \times 10^{-7}$ hartree ($3.7 \times 10^{-4}$ kcal/mol) higher than the lowest EMP$_2 + G_{sol}^{(2)}$ energy encountered in the optimization route. In the ZAPT2-CPCM case, the minimum on the EMP$_2$ surface indeed gives the lowest EMP$_2 + G_{sol}^{(2)}$ energy in the optimization route. Our experience shows that in ~70% geometry optimization cases, the EMP$_2$ minima coincide with the EMP$_2 + G_{sol}^{(2)}$ lowest energies. For the rest cases, the EMP$_2 + G_{sol}^{(2)}$ energies at the EMP$_2$ minima are always within $10^{-7}$ hartree (0.006 kcal/mol) to the lowest EMP$_2 + G_{sol}^{(2)}$ energies.

We recommend the use of EMP$_2$ for geometry optimization, and the use of EMP$_2 + G_{sol}^{(2)}$ for the total energy.

### B. Nucleobases

The S$_0$ ground state adenine, guanine, cytosine, thymine, and uracil all show planar skeletons after gas phase RMP2 optimization (Figure 1). Cytosine, thymine, and uracil should have $C_s$ symmetry (no symmetry is imposed in the geometry optimization). Adenine and guanine do not have symmetry because their amino groups prefer trigonal pyramidal geometries. In the S$_0$ ground state, the methyl group of thymine has two H atoms pointing toward the neighboring carbonyl O atom.

After gas phase ZAPT2 and UMP2 optimization, the T$_1$ excited states of cytosine, thymine, and uracil all adapt nonplanar geometries (Figure 1). In the T$_1$ state, the methyl group of thymine has only one H atom pointing toward the neighboring carbonyl O atom. The T$_1$ excited states of uracil, thymine, and cytosine can all be considered as the results of $\pi \rightarrow \pi^*$ excitation of their C=C double bonds, which destroys the C=C double bonds, the aromaticity, and the planarity of these molecules. The changes in the bond lengths clearly indicate that the excitations are localized at the C=C double bonds. In the S$_0$ states optimized using the gas phase RMP2 method, the C=C double bond length is 1.364, 1.366, and 1.371 Å, respectively, in uracil, thymine, and cytosine. In the T$_1$ states optimized using the gas phase ZAPT2 method, these bond lengths are 1.500, 1.505, and 1.492 Å, respectively. Other bond lengths change by at most 0.03 Å.

![FIG. 1. Geometries of the S$_0$ and T$_1$ states of adenine-thymine (A-T), adenine-uracil (A-U), and guanine-cytosine (G-C) pairs optimized using RMP2-CPCM and ZAPT2-CPCM methods and the aug-cc-pVDZ basis set. The gas phase geometries of these pairs are similar to those in the CPCM solution phase. Free thymine, uracil, and cytosine have S$_0$ and T$_1$ geometries similar to those in the pairs.](Image)
The solution phase RMP2-CPCM and ZAPT2-CPCM optimized S0 and T1 state geometries are very similar to those in the gas phase. The CPCM solvation can alter the bond lengths by as large as 0.01 Å. In the gas phase S0 and T1 states, the amino group of cytosine has a trigonal pyramidal geometry, while in the CPCM solution phases S0 and T1 states, it has a trigonal planar geometry.

The CPCM effects in the T1 state cytosine, thymine, and uracil are 1.91, 2.40, and 2.92 kcal/mol (ZAPT2 results in Table III) smaller in magnitude than those for the S0 states (RMP2 results in Table III). The reduction in the CPCM solvation energy is mainly caused by the changes in the electronic structure, with contributions from geometry relaxation.

The UMP2 results are very similar to the ZAPT2 results. The UHF spin contamination is not significant, with $S^2$ being ∼2.05 in all the cases.

### C. Nucleobase pairs

The S0 ground state adenine-thymine (A-T), adenine-uracil (A-U), and guanine-cytosine (G-C) hydrogen bonding pairs are optimized with the gas phase RMP2 method (Figure 1). In all of these three S0 state pairs, the geometries of adenine, guanine, thymine, uracil, and cytosine are very similar to those of their free S0 states. The A-T pair has a planar skeleton with two H atoms of the thymine methyl group sticking out of the plane; the A-U pair is planar; the G-C pair is not planar because the amino group of guanine prefers a trigonal pyramidal geometry (the dihedral angle formed by the two aromatic planes is ∼5.5°).

The T1 excited states of A-T, A-U, and G-C pairs can also be described by ROHF, UHF, ZAPT2, and UMP2 methods because the excitations are localized in thymine, uracil, and cytosine. Here, only the ZAPT2 method is used because the UMP2 method is more costly. After the gas phase ZAPT2 optimization, the T1 state A-T, A-U, and G-C pairs adapt non-planar geometries (Figure 1). In all of these three T1 state pairs, the geometries of adenine and guanine are very similar to those of their free S0 states, and the geometries of thymine, uracil, and cytosine are very similar to those of their free T1 states. Therefore, these T1 excited state pairs can be considered as dimers formed by S0 state adenine/guanine and T1 state uracil/thymine/cytosine. In the S0 state pairs optimized using the gas phase RMP2 method the C=C double bond lengths are 1.365, 1.367, and 1.369 Å, respectively, in uracil, thymine, and cytosine. In the T1 state optimized using the gas phase ZAPT2 method these bond lengths are 1.498, 1.505, and 1.492 Å, respectively. These values are almost identical to those in the free uracil, thymine, and cytosine. In the pairs, other covalent bond lengths change at most by 0.03 Å from S0 to T1, while the hydrogen bond lengths change more significantly.

The geometries after solution phase RMP2-CPCM and ZAPT2-CPCM optimization are very similar to those in the gas phase. The CPCM solvation can alter covalent bond lengths by as large as 0.03 Å, and hydrogen bond lengths by as large as 0.14 Å. For example, in the S0 state A-U pair, the middle hydrogen bond is shortened by 0.10 Å, while the other hydrogen bond is lengthened by 0.14 Å, ongoing from the gas phase to CPCM.

The gas phase formation energy of the S0 ground state G-C pair is −30.27 kcal/mol as calculated from the difference between the gas phase RMP2 optimized energy of the G-C pair (Table IV) and the sum of the RMP2 optimized monomer energies (Table III). The solution phase formation energy of the S0 state G-C pair is −10.36 kcal/mol as calculated from the RMP2-CPCM optimized energies. So, the formation of the S0 state G-C pair in water is 19.91 kcal/mol less favorable than in the gas phase because water tends to dissolve the pair. The gas phase formation energy of the T1 state G-C pair is −29.86 kcal/mol as calculated from the difference between the gas phase ZAPT2 optimized energy of the G-C pair and the sum of the RMP2 optimized energy of S0 guanine and the ZAPT2 optimized energy of T1 cytosine. The solution phase formation energy of the T1 state G-C pair is −9.49 kcal/mol. The values for the A-U and A-T pairs are listed in Table IV for comparison.

Clearly, in both the gas phase and the solution phase, the hydrogen bonds in the T1 state A-U, A-T, and G-C pairs is ∼1 kcal/mol weaker than those in the S0 state pairs, and the CPCM solvation does not appear to significantly affect the weakening of the hydrogen bonding ongoing from S0 to T1 state. We performed aug-cc-pVQZ (Ref. 29) interaction analysis using the localized molecular orbital energy decomposition analysis (LMO-EDA) method for select pairs and found that the basis set superposition error (BSSE) in the formation energy calculated using the MP2/aug-cc-pVDZ methods is ∼4 kcal/mol.
The CPCM solvation effects in the T1 state G-C, A-T, and A-U pairs are 2.36, 2.05, and 2.61 kcal/mol smaller in magnitude than those for the S0 states (Table IV). These differences are similar to those (1.91, 2.40, and 2.92 kcal/mol) found for free cytosine, thymine, and uracil, implying that they are caused by local changes in the electronic structures and molecular geometries of these molecules.

V. CONCLUSION

Analytic energy gradient are derived and implemented for MP2-CPCM methods. Very accurate gradient and smooth and continuous potential energy surfaces are obtained by using the FIXPVA surface tessellation scheme for CPCM. All closed shell and open shell MP2 methods (RMP2, ZAPT2, and UMP2, serial and parallel programs) in GAMESS are enabled to perform MP2-CPCM gradient calculations. A better CPCM solvation energy can be obtained efficiently by using the MP2 relaxed density. The open shell ZAPT2 and ZAPT2-CPCM methods are used to study the T1 excited states of three nucleobase pairs (adenine-thymine, adenine-uracil, and guanine-cytosine) in the gas phase and aqueous solution phase. It is found that in both the gas phase and solution phase, the hydrogen bonds in the T1 excited state base pairs are ~1 kcal/mol weaker than those in the S0 states.

ACKNOWLEDGMENTS

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TABLE IV. Energy (hartree) of optimized nucleobase pairs in the gas phase (E_{MP2}) and solution phase (E_{MP2} + G_{solv}^{(2)}) using the aug-cc-pVDZ basis set. The CPCM effect and formation energy are in kcal/mol.

<table>
<thead>
<tr>
<th></th>
<th>Adenine-uracil</th>
<th>Adenine-thymine</th>
<th>Guanine-cytosine</th>
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