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Effect of Change in Moment of Inertia on Line Intensities of Parallel Vibration-Rotation Bands of Symmetric Top Molecules

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and C-Si-C angle (111°2') were obtained from observed rotational constants of (CH₃)₂SiH₂.

The rotational spectrum of $(CH_3)(CD_3)SiH_2$ was found to consist of closely spaced doublets (see Table II). Tunnel effect splittings due to the CD_3 group are immeasurably small and the molecule behaves essentially as a one rotor molecule as far as the microwave spectrum is concerned. From the observed splittings, the barrier was calculated to be 1657 ± 10 cal/mole.

It is interesting to note that the rotational constants and splittings are consistent with coaxial methyl group and C-Si axes (cf. reference 3). The agreement between the two V_3 determinations leads us to believe that accuracy here is limited predominantly by uncertainties in methyl group parameters, and not by neglect of cross terms in the potential energy. We are presently investigating the possibility of setting an upper limit to these cross terms. The results will be published in full at a later date, together with results for other isotopic species, the spectra of which are now being measured.

The author is greatly indebted to Dr. J. D. Swalen and Dr. Dudley R. Herschbach for many helpful discussions.

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¹ For a derivation of (1) and definitions see D. R. Herschbach, J. Chem. Phys. 31, 91 (1959).
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⁴ R. W. Kilb and L. Pierce, J. Chem. Phys. **27**, 108 (1957).

Effect of Change in Moment of Inertia on Line Intensities of Parallel Vibration-**Rotation Bands of Symmetric Top Mole**cules

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CEVERAL authors¹⁻³ have investigated the degree to N which theory can predict the individual line intensities in vibration-rotation bands by considering the first-order corrections due to the moment of inertia change. We wish to report an extension of these calculations to include symmetric top molecules and experimental determination of the change in the moment of inertia effect on the line intensities of the parallel bands of ammonia.

The equations show, as with diatomic and linear molecules, a line intensity dependence on a quantity θ_k , which equals $\mu_0 \xi_k / \mu_{1,k}$ where μ_0 is the static dipole moment of the molecule, $\mu_{1,k}$ is the rate of change of the dipole moment with the normal vibration k and ξ_k is the Taylor's series coefficient in the expansion of the moment of inertia in terms of the normal coordinate Q_k . The complete intensity formula differs from the zeroorder formula by factors as follows:

$$I_k{}^{R} \sim [1 + \delta_k (1 - 4\theta_k) (J + 1)],$$

$$I_k{}^{P} \sim [1 - \delta_k (1 - 4\theta) J],$$

where $\delta_k = 2B_e/\nu_k$.

Measurements were carried out on the parallel bands of ammonia as the total integrated band intensity⁴ and additional molecular parameters are available.⁵ The ratios of the calculated zero-order intensities to the measured intensities for low values of J give experimental values of θ_k , from which ξ_k can be calculated. The data obtained are as follows:

ModeFreq.
$$\xi_k(calc.) \times 10^{-20}$$
 $\xi_k(exptl.) \times 10^{-20}$ ν_1 3337 cm^{-1}0.190.11/g¹-cm ν_2 9500.460.64

These calculations are made on the assumption that other effects are negligible, in particular the Coriolis corrections. Calculations indicate that the Coriolis effect contributes to the intensities only in the second order. These will be reported in a forthcoming paper.

It has been found that sum rules for the ξ 's exist of the form

$$\sum_k \xi_k^2 = 1/I_B.$$

This gives a comparison with an independently determined experimental quantity. The $1/I_B$ from infrared data⁶ gives 0.35×10^{40} while from the above data it is 0.42×10^{40} and the agreement seems satisfactory.

Calculations of the potential function for ammonia using the additional data furnished by the relationship between the ξ 's and the symmetry force constants are being carried out in this laboratory and the results will be reported in a forthcoming article.

* Dupont Postgraduate Teaching Assistant 1958-1959.

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⁵G. Herzberg, Infrared and Raman Spectra of Polyatomic Molecules (D. Van Nostrand Company, Inc., Princeton, New Jersey, 1945), p. 177.

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Comments and Errata

Note on a Paper by B. F. Gray

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 \mathbf{Y} RAY¹ has recently given an iteration procedure for U for which he has concluded that convergence is limited only by the presence of significant amounts of continuum contaminant in the initial wave function. He then points out that no known approximate wave function for the helium atom converges even on the first cycle. The conclusion is that the best available helium wave function² contains appreciable continuum contaminant. That this conclusion is unwarranted³ is seen by the following counter-example. Let exp- $(1+\delta)r$ be an approximate wave function for the hydrogen atom. Application of Gray's proposed iteration technique leads to a first improved wave function

$$(1+\delta)^2 \exp(-(1+\delta)r - 2\delta r^{-1}\exp(-(1+\delta)r)$$

The second term is unacceptable for all $\delta \neq 0$. Nevertheless, the weight of the continuum in the initial wave function for small δ is easily found to be $0.3262_{5}\delta^{2} + 0(\delta^{3})$; i.e., negligible for δ small enough. In order to recognize a similar type of error, consider the following only apparently correct argument for another criterion of significant continuum contaminant. Suppose we have an approximate normalized wave function for some system,

$$\psi = \sum_{n} a_n \phi_n$$
 with $\sum_{n} a_n^2 = 1$,

where the ϕ_n are the exact eigenfunctions of the system, and the summation is understood to include an integration over the continuum. With obvious notation, we have the identity

$$E_0^2 - \langle H^2 \rangle = \sum_n a_n^2 (E_0^2 - E_n^2).$$
 (1)

Now suppose

so that

$$a_n$$
 negligibly small for all $E_n^2 > E_0^2$, (2)

[i.e., Eq. (2) is to be valid for the greater part of the continuum], so that the right side of Eq. (1) is a positive quantity. Thus it follows that

$$\langle H^2 \rangle \leqslant E_0^2$$
.

From the variational theorem we have (assuming $E_0 < 0$, and ψ reasonably good)

$$\langle H \rangle^2 \leqslant E_0^2$$
,

and since the width is necessarily a positive quantity

$$\langle H^2 \rangle \geqslant \langle H \rangle^2$$
,

$$\langle H \rangle^2 \leqslant \langle H^2 \rangle \leqslant E_0^2. \tag{3}$$

Equation (3) says that a power of the Hamiltonian gives a better energy than the Hamiltonian itself. Equation (3) should now be a test for the presence of significant continuum contaminant. The necessary quantities using the approximate hydrogen wave function above are easily calculated, and it follows rigorously that for no choice of δ can Eq. (3) be satisfied (except in the physically unrealistic case $\delta < -0.31$). Nor does Kinoshita's² best wave function satisfy Eq. (3). The source of the trouble in both this argument and in Gray's can only be the assumption of Eq. (2). In both cases the a_n have been fixed by the

choice of the initial wave function considered, and then, in effect, integrations over a broad spectrum involving the product of these fixed numbers and a quantity which increases without limit (the E_n) are neglected. Thus a wave function whose continuum expansion coefficients do not fall off faster than $E_n^{-\frac{1}{2}}$ will fail on Gray's first iteration, and a fortiori on the test of Eq. (3). But this refers to the functional behavior of the expansion coefficients and not to their magnitudes. Indeed, the counter-example shows their magnitudes may be as small as we please; the limiting behavior of its a_n for large positive E_n and δ small is of the form $\delta E_n^{-\frac{3}{2}}$. This note does not affect the arguments of the first part of Gray's paper which retains its high interest.⁴

¹ B. F. Gray, J. Chem. Phys. 29, 272 (1958).

² T. Kinoshita, Phys. Rev. 105, 1490 (1957).

³ The conclusion should now read that this wave function contains *some* continuum contaminant.

⁴ Gray's iteration procedure [as well as my own Eq. (3)] may still be useful of course; e.g., in cases similar to the examples treated by Gray, or to detect, with some ambiguity, the presence of continuum contaminant.

Comment on "Infrared Spectra of Partially Deuterated Diboranes"

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(Received May 6, 1959)

I N view of recent work on the infrared spectra of monomethyl-¹ and monoethyldiboranes² we have come to the conclusion that the weak band at 2128 cm⁻¹, rather than 1900 cm⁻¹, in the infrared spectrum³ of B_2H_5D represents the symmetric in-phase B—H' bridge breathing frequency in the terminally deuterated compound (II). A similar band is observed at 2110 to 2114 cm⁻¹ in the monoalkyldiboranes.

This reassignment would lower the observed Teller-Redlich product of I/II for A' from 1.84 to 1.64 (see Table VII in reference 3). To bring this value back up to 1.84, ν_9 in compound II is changed from an estimated 940 cm⁻¹ to the observed very weak band at 858 cm⁻¹, while ν_{12} is reassigned from 858 cm⁻¹ to an estimated 840 cm⁻¹ (unobserved). The net effect of all these changes is an increase in the sum for II+XX (see Table VIII) from 59.4 to 60.1, in perfect agreement with the sum for I+XXI.

This modification of the assignment results in greater over-all consistency (see Table VI). For instance, a weak band, similar to the 858 cm⁻¹ band in B₂H₅D, is found at 800 cm⁻¹ in the spectrum of B₂D₅H and has been assigned to ν_9 of compound XX; ν_{12} as in II, is unobserved. Further, the new assignment for ν_2 is in accord with the idea that terminal substitution will have relatively little effect on bridge frequencies.

The modified sections of Table VI should now read: