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Indexing principles and a widely applicable paradigm for indexing animal populations

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Abstract. Monitoring animal populations is an essential component of wildlife research and management. Population indices can be efficient methods for monitoring populations when more labour-intensive density-estimation procedures are impractical or invalid to apply, and many monitoring objectives can be couched in an indexing framework. Indexing procedures obtain maximal utility if they exhibit key characteristics, including being practical to apply, being sensitive to changes or differences in the target species’ population, having an inherent variance formula and allowing for precision in index values, and relying on as few assumptions as possible. Additional useful characteristics include being able simultaneously to monitor multiple animal species and to describe spatial characteristics of the species monitored. Here, a paradigm is presented that promotes the characteristics that make indices most useful. Observations are made at stations located throughout the area of interest. Stations can take many forms, depending on the observations, and range from points for visual counts to tracking plots to chew cards, and many others. A wide variety of observation methods for many animal species can fit into this format. Observations are made at each station on multiple occasions for each indexing session. Geographic location data for each station are encouraged to be collected. No assumptions of independence are made among stations, nor among observation occasions. Measurements made at each station are required to be continuous or unboundedly discrete. The formula for a general index to describe population levels is presented and its variance formula is derived. Issues relevant to the application of this methodology, and indices in general, are discussed.

Introduction

Monitoring animal populations is crucial to wildlife researchers and managers for a wide spectrum of reasons, including setting harvest-management parameters, assessing biodiversity, tracking threatened or endangered species, disease surveillance, management of wildlife in conflict with human interests, compliance with regulatory requirements, and the general accumulation of knowledge. Ideally, the exact number of animals within an area of interest would be known but, in reality, this is a rare circumstance and population size is often assessed through sampling procedures. Density-estimation procedures such as mark–capture (e.g. Otis et al. 1978) and line transect (e.g. Burnham et al. 1980) methods attempt to estimate the actual number or density of animals in an area, but they are often difficult or expensive to implement for many animal species, and they may require difficult-to-meet analytical assumptions that, when violated, result in estimates of questionable quality (see Krebs 1998 and Leidloff 2000 for an examination of potential problems with mark–recapture methods and Burnham et al. 1980 for a similar discussion on line-transect methods). Often, problems couched in terms of absolute density can be redefined such that an index parameter reflective of population abundance will provide an efficient solution (Caughley 1977; Krebs 1998). Indexing procedures are additional tools in the armamentarium of methods available for monitoring wildlife populations (e.g. Engeman 2003). Examples include tracking rates, faeces deposition, capture rates, bait consumption, or visual observations, among a host of possibilities. Because indices are not estimates of actual population numbers, they are applied to make relative comparisons between populations or to monitor trends within a population (e.g. Caughley 1977; Krebs 1998).

Here, a general observational and analytical paradigm is presented into which a wide variety of measurement methods for indexing many species of animals can fit. The data structure from which index values are calculated leads to the derivation of the index variance estimate while requiring minimal analytical assumptions about the observations.

Desirable qualities for an index

An indexing methodology obtains maximal utility when it possesses certain desirable characteristics. Some of these result from the data structure or the analytical method, whereas others can result from observational methods.

Practicality. An index method must be practical to apply. This might be said of any sampling procedure but, beyond that, practicality is a prime deciding factor for choosing to use an index in the first place. The index method should be user-friendly, with the procedures and concepts for recording...
information easily understood, and with little chance for confusion among species. Methods must impose minimal inconvenience on landowners and managers to be acceptable.

**Sensitivity.** An index should be sensitive to differences in population size, whether making simultaneous comparisons among multiple populations, or monitoring for change within the same population. That is, the measurements upon which the index is based should change if the population changes. For example, structure counts often are used as indices to compare muskrat (*Ondatra zibethicus*) populations between areas (Proulx and Gilbert 1984). However, the longevity of structures built by muskrats make structure counts an inefficient method to index short-term changes within muskrat populations, whereas rigorously designed visual counts may provide suitable sensitivity for this application (Engeman and Whisson 2003).

**Precision and variance estimation.** Given an appropriate observation, the ability of an index to statistically detect population differences increases with its precision. This highlights a contrast between density estimation and indexing. Density estimation strives to identify actual population abundance directly, whereas indexing procedures seek to use reflective measures for detecting differences in abundance. Thus, general applications for density estimation place a premium on accuracy (low bias), but the applications for indices make precision of the utmost importance (e.g. Caughley and Sinclair 1994). An index that is easily applied in the field will likely encourage more observations, with a consequent improvement in precision.

Since precision is essential to an index, it follows that the data structure, measurements and index calculations define an inherent estimate of variance, which in turn allows for the application of standard statistical procedures. Often a situation exists where observations are made and an index produced, but the only avenue for estimating variance is to first subdivide the data into units that can contribute to the variance calculations. This approach, especially if done post hoc, can produce variance estimates that vary subjectively with the definition of the units.

**Robustness.** The most robust inferences are produced if the calculated index and associated variance are burdened with as few assumptions as possible about the data structure and the distribution of the observations. Violation of analytical assumptions is the bane of density-estimation methods (see Krebs 1998 for a general overview), and can be a compelling reason to apply an index rather than estimating density. An index heavily reliant on analytical assumptions is of minimal use to the investigator.

**Other useful characteristics.** Other characteristics can make an indexing procedure more informative. First, if the observation methods allow simultaneous monitoring of multiple species, then economy of effort is achieved over simultaneously applying different methods for different species. Also, if information on geographic location is collected along with the index observations, then spatial characteristics of the population(s) may also be described.

### General index format

A tremendous array of indexing procedures has been applied to many species of animals. Each combination of observation, sampling frame and computation procedure results in a parameter estimate for a population characteristic that is reflective of animal abundance. Here, an indexing paradigm is provided with a sampling structure in which many existing, or new, observation and measurement methods can be couched so that the calculated estimates (index values) possess useful statistical properties. The key components to this paradigm are defining where the observations are taken, the time dimension for taking observations, the measurements to make, and the data structure and analytical procedures for calculating an index and its variance estimate.

**Observation stations**

The locations where observations are taken will be referred to generically as stations. In practice, for example, each station might be a plot for observing tracks or other animal signs, a tracking tile, a chew card, a point where animal counts are made, a site where bait consumption is measured, a camera location, or even a trap line.

To index a population within an area, observation stations should be set throughout the survey area of interest. That being said, the distribution of observation stations must be carefully considered relative to efficiency in obtaining adequate measurement of the animals being monitored, and avoiding bias in the results that could be induced by station placement. Rarely do animals operate in a spatially random pattern. Station locations may take advantage of behavioural characteristics by placement where they would most likely intersect the usual activities of the target animals (Engeman et al. 2002). This is similar in concept to the capture of animals. Capture devices are not placed with complete randomness, but rather are placed where an animal is most likely to encounter the capture device. Consider a tracking plot example for collecting index data. Many species such as canids preferentially use dirt roads or tracks as travel ways. Placement of stations along such travelways is an efficient means to obtain observations. If such travelways are distributed throughout the area of interest, they can provide a means for station placement that is an efficient and representative sampling of the population using the surrounding habitat. Care and common sense must be applied when choosing to take advantage of these behavioural characteristics for monitoring animals. If roads or tracks are not dispersed through the area of interest, then observations only from them would not be representative of the population throughout the area. If multiple indexing assessments are to be made through time on the same area, then the same station locations should be used if possible (e.g. Ryan and Heywood...
2003). If the area of interest is comprised of different habitat types, then it is advisable to stratify station placement according to habitat type, thus helping to ensure that the calculated index reflects the population throughout the area rather than being overly biased towards (or away from) a particular subset of habitat. Stratification also allows index comparisons among the habitats within the area of interest, information about which is often of biological and management importance.

Stations should be dimensionally consistent in preparation. This applies to area dimensions of the stations, as well as to time, weight or any other characteristic of the stations. Thus, not only should stations such as tracking plots, tracking tiles or chew cards have consistent sizes (e.g. rectangular dimensions), but chew cards should all have the same thickness, bait-take stations should each start with the same amount of bait, stations for making animal counts should be observed for the same length of time and out to the same distance.

**Time dimension**

Animal activity often is variable over even short periods. Thus, to account for variability over time, the stations are best observed on more than one occasion during an assessment period. Typically, this means taking measurements at each station on each of multiple days, but for some applications this could mean taking measurements every other day, or multiple times during a day, or at some other period. For simplicity, the time dimension will be referred to here as a day effect, representing a common situation where observations at each indexing session would be made on multiple, usually consecutive, days. The time elapsed between successive observations at each station should remain constant. For example, assume observations are to be made at three time points. The time lapsed for accumulation of data should be constant at each of the three observation times. Say tracking plots are to be observed 24 h after plot preparation, then each succeeding observation of the plots should also be made 24 h after plot preparation.

**Measurements**

Many types of measurements can fit the above observational structure, including the general categories of animal counts, measurement of animal sign, and catch per unit effort. For the purposes of the methodology presented here, the observations taken at each station should be non-binary, that is, continuous or unboundedly discrete. The variety of non-binary indexing measurements at different types of observation stations include the number of intrusions by each species of animal onto a dirt tracking plot, the area or proportion of a tracking tile tracked by each species, the proportion or area of a chew card consumed, the number of individuals of each species observed in a fixed amount of time within a fixed distance at each station (standardised by time of day), or the daily number of captures or catch rate from each of a number of trap lines in the area of interest (e.g. Allen et al. 1996; Engeman and Witmer 2000; Engeman and Whisson 2003).

Often, potentially continuous measures have been neglected in favour of binary observations, i.e. presence-absence measures at each station. Reduction of potentially continuous data to binary observations is easily demonstrated to have less descriptive ability and result in a greater opportunity for erroneous inferences (Engeman et al. 1989), and this principle has been well demonstrated for tracking-plot data (e.g. Allen et al. 1996; Engeman et al. 2000, 2002).

Binary observations have often been made because a continuous measurement was difficult to measure or was not considered. For example, tracking tiles or chew cards are easier to record as showing activity or not, without accurately recording the intensity of activity at each station. Observations on intensity of activity at these types of stations may be made by measuring the area of activity at each station. This measurement can be reliably approximated by counting the squares on an overlaid grid showing activity. Moreover, the universality of modern computing equipment makes highly accurate area measurements a relatively simple process using commonly available software.

A corollary to the use of continuous rather than binary measures is that stations should be designed so that total saturation at a station is unlikely. That is, an entire chew card would be unlikely to be consumed overnight, not all bait at a bait station would be consumed, or a tracking tile would not be totally obliterated by animal activity. All stations can receive activity, but an increase in intensity can still be detected.

Another valuable measure at each station is its geographical location. This can be accomplished by the use of global positioning devices, maps, or relative measurements among station locations. Potentially, measuring or calculating distances among stations can be used in conjunction with station observations to also index the spatial pattern of animal activity within the survey area. One approach modifies Hopkins' (1954) index of aggregation, which has seen other useful modifications (e.g. Engeman and Sugihara 1998). The IP (for index of pervasiveness) is defined mathematically as:

\[ IP = \frac{1}{n} \sum \frac{w_1}{w_2}, \]

where \( n \) is the number of active stations, \( w_1 \) is the square of the distance from an active tracking station to the nearest active station (nearest neighbour sample: Engeman et al. 1994), and \( w_2 \) is the square of the distance from that nearest station to its nearest active station (second-nearest neighbour sample: Engeman et al. 1994). When the pattern is entirely random, \( IP = 1 \). If the stations with activity show aggre-
gations (localised concentrations), then IP > 1. For systematic spatial patterns of activity, IP < 1.

**Data structure**

The data structure, defined by the station placement design and measurement method, provides the framework from which a general index and its variance can be calculated. To formalise a mathematical description of the data structure, assume there are s stations at which observations will be made on each of d time points (days). The measurement from the rth station on the jth day, \( x_{rj} \), can be represented as a linear model:

\[
x_{rj} = \mu + S_r + D_j + e_{rj},
\]

where the term \( \mu \) is the overall mean measurement value per station per day for the area being assessed. \( D_j \) is a random effect due to the day on which an observation was made, with \( j = 1, 2, 3 \ldots d \). \( S_r \) is a random effect due to the rth station with \( i = 1, 2, 3 \ldots s \) representing the number of stations contributing data on the jth day. The \( e_{rj} \) represent random observational noise, and are considered independent and identically distributed with mean = 0 and variance = \( \sigma_e^2 \).

In practice, it would be unreasonable to assume that each station would contribute data each day. Tracking plots can be obliterated by livestock or vehicle traffic. Chew cards can become lost. Observations at some stations may be missed owing to unforeseen access restrictions. Thus, the number of stations contributing data each day is allowed to vary.

To assume that stations are uncorrelated, or that observation days are uncorrelated, would be biologically unreasonable in most circumstances. For example, animals may roam greater distances than those separating the stations. Also, stations that are closer together may share more characteristics than do more distantly separated stations. Similarly, environmental or climatic conditions should not be assumed to be unrelated across days of observation. The stations in this sampling framework are not assumed independent of each other nor are days assumed independent of each other, i.e. a non-zero covariance structure is assumed to exist among stations and among days. Thus, the derivation of the variance estimate is not reliant on a potentially unrealistic assumption of independence.

**Index calculations**

The calculation of the general index (GI) begins by taking the mean of the observations across all stations each day (this is done separately for each species if more than one is measured at each station). The GI is the mean of the daily means, and provides an average view of the measurements over space and time within the area of interest. The GI can be written in the linear model terminology as:

\[
GI = \frac{1}{d} \sum_{j=1}^{d} \frac{1}{s_j} \sum_{i=1}^{s_j} x_{ij},
\]

The variance formula for the GI is:

\[
\text{var}(GI) = \frac{\sigma_y^2}{d} \sum_{j=1}^{d} \frac{1}{s_j} + \frac{\sigma_d^2}{d^2} \sum_{j=1}^{d} \frac{1}{s_j} + \frac{\sigma_e^2}{s^2},
\]

where the \( \sigma_y^2, \sigma_d^2, \) and \( \sigma_e^2 \) are, respectively, the components for station-to-station variability, daily variability, and random observational variability associated with each station each day. A computational procedure such as SAS PROC VARCOMP (SAS Institute 1996), using a restricted maximum-likelihood estimation procedure (REML), can be used to calculate the variance components (Searle et al. 1992) needed in the GI variance-estimation formula. If all \( s \) of the tracking stations provide observations each day, the formula simplifies to:

\[
\text{var}(GI)_{\text{equal}} = \frac{\sigma_y^2}{s} + \frac{\sigma_d^2}{d} + \frac{\sigma_e^2}{s d^2}.
\]

The existence of an inherent variance estimate for GI allows standard statistical procedures such as confidence intervals and hypothesis tests to be applied, as appropriate. Appendix 1 provides an example for calculating the GI and its variance.

**Discussion**

Population indexing and density estimation are among the population-monitoring tools available to the investigator (Engeman 2003). An investigator needs to be clear on the monitoring objectives when deciding whether to estimate the numerical size or density of the population, or whether to apply an index reflective of the population. Given that an indexing procedure would be suitable for the situation, a great diversity of observation and measurement methods can be integrated into the general index procedures presented here, as illustrated in Table 1.

Although indices are valuable for detecting differences in population abundances, they are not estimates of the numerical abundance. An attempt to estimate actual abundance or density from an index would require additional study where known densities (not density estimates) are related to index values with a statistical model. Although frequently seen in the wildlife literature, attempting to define a relationship between an index and true population numbers by establishing a relationship between an index and an estimate of density is inappropriate, because this yields only an indication of correspondence among methods, with the benchmark still only an estimate of unknown quality (e.g. Caughley and Sinclair 1994; Leidloff 2000).

If a population estimate is mandatory, then it is sensible initially to devote the resources necessary for density or abundance estimation. As White (2001) cautioned, 'Don't even start the project if you can't do it right'. The investigator should be prepared to do all that is necessary in terms of resources and information to adequately design a study that ensures that adequate numbers are observed or captured, and
that data are appropriately modelled without violating the underlying assumptions for calculating the density estimate. This is not a simple task. McKelvey and Pearson (2001) found in a five-year literature review of small mammal studies that 98% of the studies resulted in too few data for valid mark–recapture population estimation. Such frequent difficulties in meeting the requirements for density-estimation procedures led Caughley and Sinclair (1994) to assert that absolute estimates of population size or density require a ‘leap of faith’ by the manager concerning the validity of analytical assumptions and the resulting accuracy of estimates.

Application of the paradigm for data gathering and index calculation goes a long way towards ensuring that the resulting index will possess many of the desirable qualities described earlier. Nevertheless, a useful data structure and analytical procedures by themselves do not guarantee that an indexing method is suitable for meeting objectives. Considerable room exists for artistry by the investigator in deciding on the measurements to take and how to place the stations. Sometimes a number of methods may be available from which the most appropriate method must be selected. On the other hand, a proven method may not be available. A method successfully applied to a similar species or a similar situation would be a good candidate method to test and apply.

Fully enumerated wild populations upon which methods can be tested are rare. Therefore, examination of the utility of an indexing procedure is properly approached through experimentation. A straight-forward strategy is to index a population, change that population, and then index the population again. This can be repeated multiple times and is best if a control area with no induced population change is simultaneously monitored using the same indexing method.

An index should increase if the population increases and decrease if it decreases. Therefore, an index needs to be monotonic relative to the true population to effectively discern differences. Ideally, the index would have a linear relationship with the population size, but to assume linearity for analytical purposes would transform an index method into a density-estimation method, with all of the associated difficulties concerning analytical assumptions. The resultant variability of an index determines the statistical detectability of population differences. As long as they do not interfere with one another, simultaneous application of multiple procedures provides comparisons on how each follows population changes. A method would be selected on the basis of its sensitivity to population differences and field logistics. If a seemingly reasonable station placement and observation method do not produce useful results, then minor changes in methods may improve sensitivity to the presence of animals. For example, a chew card might receive little attention by the animal of interest even though populations are high. A change in the impregnating substance could result in an improved response. But clearly, a chew card index calculated from responses using one impregnating substance is an entirely different index, and not comparable with, an index calculated from responses using a different impregnating substance.

Many of the observational methods that can fit into the GIS format are suitable for simultaneously monitoring multiple species of animals (e.g. tracking stations, visual counts). Simultaneous monitoring of multiple species allows infer-

<table>
<thead>
<tr>
<th>Station example</th>
<th>Potential (non-binary) measurement</th>
<th>Examples of potential species observed</th>
<th>Example citations for the type of station or measurement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dirt tracking plots</td>
<td>Number of intrusions by each species into plot</td>
<td>Medium to large mammals (e.g. carnivores, ungulates, macropods)</td>
<td>Allen et al. (1996), Engeman et al. (2000), (2001), (2003a), (2003b); Mahon et al. (1998)</td>
</tr>
<tr>
<td>Tracking tiles/plates</td>
<td>Proportion/area tile tracked each species</td>
<td>Rodents, small to medium-sized carnivores</td>
<td>Barret (1983), Fiedler (1994); Zielinski and Kucera (1995)</td>
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<tr>
<td>Mound count plot</td>
<td>Number of mounds or feeder plugs in plot</td>
<td>Pocket gophers</td>
<td>Reid et al. (1966); Anthony and Barnes (1983); Engeman et al. (1993); Caughley et al. (1998); Engeman and Witmer (2000)</td>
</tr>
<tr>
<td>Chew cards</td>
<td>Proportion/area removed (or remaining)</td>
<td>Rodents and other small to medium-sized mammals</td>
<td>Fagerstone and Biggs (1986); Menkens et al. (1990); Powell et al. (1994); Robbins et al. (1986); Severson and Plumb (1998); Servoss et al. (2000); Engeman and Whisson (2003)</td>
</tr>
<tr>
<td>Visual observation sites</td>
<td>Number seen within a fixed time and distance</td>
<td>Birds, ground squirrels, muskrats</td>
<td>Chitty (1954); Choquet et al. (1996)</td>
</tr>
<tr>
<td>Bait take</td>
<td>Amount or proportion of bait removed</td>
<td>Rodents, swine, deer, bear</td>
<td>Chitty (1954); Choquet et al. (1996)</td>
</tr>
<tr>
<td>Apple slice(s)</td>
<td>Amount or proportion of apple removed</td>
<td>Voles</td>
<td>Byers (1975); Tobin et al. (1992)</td>
</tr>
<tr>
<td>Road segment</td>
<td>Number of scats deposited in fixed time frame</td>
<td>Canids</td>
<td>Davison (1980); Andelt and Andelt (1984)</td>
</tr>
</tbody>
</table>
ences on relative population levels within each species, but comparisons of index values across species is not appro-
riate. For example, consider monitoring multiple species using intrusions to tracking plots on dirt roads. Different
species would have different home ranges, road usage, and travel rates. Spoor-deposition rates, and hence GI values,
would differ among species even if their populations were the same.

The variance components calculated for use in the GI variance formula also provide helpful planning information
(e.g. Searle et al. 1992). The relative contributions of station-to-station variation and day-to-day variation can be exami-
ned to optimise the combination of days and stations for subsequent indexing assessments. For example, if the com-
ponent of variance for station-to-station variation was much larger than the other sources of variation, then the emphasis
would be placed on the number of stations. However, if the weather changed during the assessment period, then the
number of observation days should be increased, or the assessment delayed. In reality, logistics and resources often
are the most important influences on sampling designs for wildlife surveys.

The applications of the indexing methodology described here have been exemplified by vertebrate animal popu-
lations, but the methodology is more broadly applicable. Invertebrate animals can be indexed by this paradigm using
standard entomological methods. The observation stations could be pitfall traps or standardised sweep-net collections,
with the measurements being daily counts at each station of number of species, or number of insects of each species. The
same tracking plots as have been used to index populations of vertebrate predators of marine turtle nests (Engeman et al.
2003b) could have been applied to index crab populations, which also represent a substantial predation threat to the
turtle nests (Stancyk 1982). The GI also holds many general ecological applications. Stations could be sediment or litter
traps to index daily deposition in streams or elsewhere. Similarly, various plot and measurement configurations
could index leaf, needle or seed fall in plant communities. As long as a suitable layout of stations is designed and appro-
priate observations are made, the methods summarised here provide a straight-forward indexing procedure with useful
quantitative properties.

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References


Appendix 1. Example for calculating the General Index

The data in Table 2 were collected for assessing a dingo population on a cattle station in south-west Queensland, Australia. A sample of \( n = 50 \) tracking plots was placed on dirt roads throughout the study area and observed for \( d = 4 \) consecutive days. The number of track intrusions into each plot by dingoes was observed each day. The average number of sets of intrusions per plot per day were 0.94, 0.82, 1.30, 0.82 for Days 1, 2, 3, 4, respectively (Table 2). The GI index value was calculated as:

\[
\frac{(0.94 + 0.82 + 1.30 + 0.82)}{4} = 0.97.
\]

Application of \textsc{Varcomp} in \textsc{SAS} produced variance component estimates of \( \sigma_g^2 = 0.1075, \sigma_d^2 = 0.0199, \) and \( \sigma_e^2 = 1.5767. \) We can use the equal-sample-size formula because all plots were measurable on each of the four days, i.e. \( p_1 = p_2 = p_3 = p_4 = 50 \) for Days 1-4. Insertion of the above information into the equal-sample-size equation for \textit{var(GI)} yields:

\[
\text{var(GI)} = \frac{0.1075}{50} + \frac{0.0199}{4} + \frac{1.5767}{200} = 0.0150
\]

standard error (s.e.) = 0.122

coefficient of variation (c.v.) = 0.126.