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# A Dynamic Real-time Scheduling Algorithm for Reduced Energy Consumption in I/O Devices

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## Abstract

*In real-time systems, Dynamic Power Management (DPM) techniques have traditionally centered on the CPU with less focus given to I/O. However, I/O-based DPM techniques have been popularly researched in non-real-time systems. These techniques focus on switching I/O devices to low power states based on some policy. These methods, however, are not applicable to real-time environments because of the non-deterministic nature of the policies. Recently, scheduling techniques to reduce power consumption of I/O devices in real-time systems have emerged. In this paper, we propose an online task scheduling algorithm, Slack Utilization for Reduced Energy (SURE), which utilizes slack in periodic task systems to reduce power consumption in I/O devices.*

## 1 Introduction

Power conservation in embedded systems is traditionally implemented via efficient power management. Dynamic power management (DPM) techniques are those that are applied at run-time based on workload variation [6]. DPM techniques can be classified as CPU-based or I/O based. An example of CPU-based DPM is Dynamic Voltage Scaling (DVS) wherein the operating voltage of the CPU is varied to save energy. I/O based DPM techniques focus on switching I/O devices into low power states based on predictive, stochastic or timeout policies [7].

In real-time systems, dynamic power management has centered mainly on the CPU with little focus given to I/O. I/O-based DPM techniques used for non-real-time systems cannot be used for real-time systems because of their non-deterministic nature. For example, probabilistic power-saving policies for shutting down I/O devices cannot be implemented in hard real-time systems, as jobs are not guaranteed to meet deadlines.

Recently, a few I/O based DPM techniques for real-time systems, have emerged. A DPM algorithm, Low Energy Device Scheduler (LEDES), for hard real-time systems is presented in [9]. LEDES generates a sequence of sleep/working states for each device. This sequence is interpreted as a *device schedule*. This device schedule is generated online using a per-task device-usage list and by looking ahead a limited number of entries in a task schedule such that the energy consumed by the devices is minimized and no task misses its deadline. LEDES is similar to SURE in that devices with two power states are considered. The LEDES algorithm was extended to work with I/O devices with multiple power states in [10]. Multi-state Constrained Low Energy Scheduler (MUSCLES) generates a similar sequence of power states for devices while guaranteeing that real-time constraints are not violated. However both LEDES and MUSCLES use a pre-determined task schedule to dynamically generate the sequence of states for each device such that the total energy consumed by the devices is minimized. This is different from SURE in that both LEDES and MUSCLES do not reorder jobs either online or offline to generate a task schedule that reduces energy consumption in devices.

The pruning-based scheduling algorithm, Energy-optimal Device Scheduler (EDS), is different from LEDES in that jobs are rearranged to find the minimum energy task schedule [11]. In this respect, EDS is more similar to the work done here. EDS generates a schedule tree by selectively pruning the branches of the tree. If a resulting schedule along a branch results in a missed deadline, this infeasible schedule is removed from the tree. In addition, if a feasible schedule along a branch is determined to consume higher energy than an alternative feasible schedule, the branch leading to this schedule is pruned. The algorithm we present is different from EDS in that EDS is an offline algorithm, with schedules computed statically, whereas SURE is an online algorithm that arranges jobs at runtime to reduce energy.

The rest of this paper is organized as follows. Section 2 describes the problem and the motivation for the algorithm. We present the energy conserving algorithm in Section 3. and conclude in Section 5.

## 2 Problem Description

The task model that we adopt is the periodic task model as proposed by Liu and Layland [5], with deadlines equal to the periods. A periodic task set is defined with a release time, period, worst-case execution time and a deadline. Suppose that the set of devices required by each task during its execution is specified along with the above parameters. The generalized problem can now be stated as follows.

Given a periodic task set,  $\{T_1, T_2, \dots, T_n\}$ ,  $T_i = (\phi_i, p_i, e_i, d_i, \Lambda_i)$  where,

$\phi_i$  is the release time or phase,

$p_i$  is the period,

$e_i$  is the worst case execution time,

$d_i$  is the deadline and

$\Lambda_i = \{\lambda_1, \lambda_2, \dots, \lambda_m\}$  is the device requirement specification for the task  $T_i$ ,

is there a schedule which meets all deadlines and also reduces the energy consumed by each device  $\lambda_j$ ?

Modern I/O devices have at least two power states: *idle* and *active*. The rate at which energy is consumed is different in each state with less power being used at the *idle* state. Thus to save energy, devices can be switched to the *idle* state, when it is not in use. In a real-time system, in order to guarantee that jobs will meet their deadlines, a device cannot be made *idle* without knowing when it will be requested by a job. But, the precise time at which an application requests the operating system for a device is usually not known. Predictive algorithms try to forecast the rate at which requests come in or make an estimate based on past requests. However, even without knowing the exact time at which requests are made, we can safely assume that devices are requested within the time of execution of the process or job making the request. We can also assume that in the absence of DMA or other such mechanisms, a device will be used within the execution time of a job. Thus, given these assumptions, we can determine the upper bound on the utilization of a device  $\lambda_i$ . We define this upper bound as the **Device Utilization Factor**  $U_{\lambda_i}$ . For the periodic task model as specified earlier in this section,

$$U_{\lambda_i} = \sum_{\forall T_j, \{\lambda_i\} \subseteq \Lambda_j} (e_j/p_j)$$

Thus, the Device Utilization Factor of a device is the sum of the CPU utilization of the tasks using the device. In a hyperperiod, the total time that a device  $\lambda_i$  will be used is  $U_{\lambda_i} \cdot H$ . This means that the device is not in use for at least  $(1 - U_{\lambda_i}) \cdot H$  time units.

For the periodic task model, consider the energy consumed over one hyperperiod. If the device remained *active* over the entire hyperperiod, the total energy consumed would be

$$E_{orig} = P_{active} \cdot H$$

where  $P_{active}$  is the rate at which energy is consumed when the device is *active*. Since the device is not in use for at least  $(1 - U_{\lambda_i})H$ , the device does not need to be *active* for the entire hyperperiod. However, significant cost is incurred when an I/O device switches or transitions from one power state to another. This cost is high in terms of both time and energy. The total energy consumed by a device  $\lambda_i$  in the hyperperiod  $H$ , is given by,

$$E_{\lambda_i} = E_{active} + E_{idle} + E_{sw} \quad (1)$$

where,  $E_{active}$  is the energy consumed when  $\lambda_i$  is in the *active* state and  $E_{idle}$  is the energy consumed by  $\lambda_i$  when it is in *idle* state and  $E_{sw}$  is the energy consumed when  $\lambda_i$  is in transition states.

$$E_{active} = P_{active} \cdot U_{\lambda_i} \cdot H$$

For simplification, let the time taken to switch from *active* to *idle* and vice-versa be the same. Let us call this switch time  $t_{sw}$ . In addition, let the power consumed during both transitions be the same. Let this power be  $P_{sw}$ . Then,

$$E_{sw} = \sigma_i \cdot P_{sw} \cdot t_{sw}$$

where  $\sigma_i$  is the total number of device state switches in a hyperperiod. So, the actual time the device is in the *idle* state is  $[(1 - U_{\lambda_i})H - \sigma_i t_{sw}]$ . Thus,

$$E_{idle} = P_{idle}[(1 - U_{\lambda_i})H - \sigma_i \cdot t_{sw}]$$

where  $P_{idle}$  is the rate at which energy is consumed when the device is *idle*. Substituting for  $E_{active}$ ,  $E_{idle}$  and  $E_{sw}$  in Equation (1), the total energy consumed by  $\lambda_i$  in a hyperperiod is,

$$E_{\lambda_i} = [P_{active}U_{\lambda_i} \cdot H] + [P_{idle}(1 - U_{\lambda_i})H - P_{idle}\sigma_i t_{sw}] + [\sigma_i \cdot P_{sw} t_{sw}]$$

The energy savings incurred if the device is made *idle* whenever it is not in use, is given by,

$$\begin{aligned} E_s(\lambda_i) &= E_{orig} - E_{\lambda_i} \\ &= P_{active} \cdot H - [P_{active} \cdot U_{\lambda_i} \cdot H \\ &\quad + P_{idle}(1 - U_{\lambda_i})H - \sigma_i P_{idle} t_{sw} + \sigma_i \cdot P_{sw} \cdot t_{sw}] \\ &= P_{active}(1 - U_{\lambda_i})H - P_{idle}(1 - U_{\lambda_i})H \\ &\quad - \sigma_i t_{sw}(P_{sw} - P_{idle}) \\ &= (P_{active} - P_{idle})(1 - U_{\lambda_i})H - \sigma_i t_{sw}(P_{sw} - P_{idle}) \end{aligned}$$

Thus, to increase energy savings, the time for which the device  $\lambda_i$  is *idle* must be increased whereas the total number of power state transitions ( $\sigma_i$ ) must be decreased. The online energy conserving algorithm proposed in the next section does this by allowing jobs that require the same device to run in succession. Thus, if a device is in the *active* state, ready jobs requiring the device are executed in succession such that only few device state changes occur. If a device is in the *idle* state, the execution of jobs is delayed as much as possible so that the jobs do not miss their deadlines but also allows the device to be in the *idle* state for a longer duration. This results in combining small and scattered device idle times to generate device idle times of longer duration. In addition, CPU idle times are combined to produce longer intervals of CPU idle time. During these CPU idle intervals, the entire system can be switched to a low power mode to save additional power.

### 3 Algorithm Description

In a real-time system, there is seldom any gain in finishing jobs early. For example, in hard real-time systems, as long as deadlines are met, there is no incentive for an early response time. At any instant  $t$ , the amount of time job execution can be delayed without resulting in any job in the task set to miss its deadline is called the system slack at time  $t$  denoted as  $\Omega(t)$ . If an I/O device is *idle* and a job requiring that device is released, then if there is system slack at that time, the device is allowed to stay idle till system slack becomes zero. At this point, the job has to be executed to meet its deadline. Similarly, suppose a device was *active*, and the job with the nearest deadline, i.e., the highest EDF priority job, did not require the device (henceforth, we use the term priority to mean the priority assigned by the EDF scheduling algorithm). At this time, there could be another lower priority job requiring the same device. If there is slack in the system, the higher priority job could be deferred and the lower priority job is executed till there is no more slack in the system. At this point, the higher priority job has to execute to meet its deadline.

The heuristic here is that a device state change from *active* to *idle* or vice-versa is delayed as much as possible. The overall result of the algorithm is that smaller chunks of device idle times and usage times are grouped together. This results in reducing the total number of state transitions in the hyperperiod. The algorithm is presented in Figure 1 and Figure 2.

The algorithm combines slack utilization with EDF to produce an energy conserving schedule. At  $t = 0$ , all devices are in the *idle* state.  $J_{curr}$  corresponds to the currently executing job and is initialized to  $\phi$ . Each scheduled job is given an execution budget before execution. The execution budget of  $J_{curr}$  is tracked with the variable  $B_{curr}$ , which is initialized to zero. The scheduler is invoked when a job is released or when a job completes or finishes its execution budget. The boolean variable *noSlack* is used to indicate that there is no slack in the system and is initially made *false*. The boolean variable *computeSlack* determines when to compute the system slack and is made *false* at  $t = 0$ .

At  $t = 0$ , when a job is released, since all devices are in the *idle* state, if there is slack in the system, the execution of jobs is deferred to keep the devices in the *idle* state as long as possible. Hence, *computeSlack* is made *true* and slack is computed. If system slack is greater than zero, then *do\_SURE()* is invoked. Here,  $J_{curr}$  remains equal to  $\phi$  and  $B_{curr}$  is made equal to  $\Omega(t)$ . When this execution budget expires, the scheduler is invoked again. Now, since all the system slack has been consumed, *do\_EDF()* is invoked and the job with the nearest deadline or the highest priority job,  $J_{high}$  is executed. The devices required by this job, as specified by  $\Lambda_{T(high)}$  will all be changed to the *active* state.  $T(high)$  refers to the task of the highest priority job  $J_{high}$ .

$J_{high}$  will execute till it completes, at which point the scheduler is invoked again. Whenever a job completes or finishes its budget, slack is computed and *do\_SURE()* is invoked. Now, if there is another job,  $J_{sh}$ , which shares the maximum number of devices with the previously executed job, then  $J_{sh}$  is executed immediately. *devShare* denotes the set of devices shared by

```

scheduler() :
Initialize at t= 0: {
    noSlack ← false ;
    Jcurr ← φ;
    Bcurr ← 0;
    computeSlack ← false;
    devShare ← φ;
    return;
}
If (t: instance when job is released) {
    If (Jcurr == φ) // the CPU is idle
        computeSlack ← true
    else
        computeSlack ← false
    If (noSlack) { // the system has no slack
        do_EDF();
        return;
    }
}
If (t: instance when job finishes its execution budget) {
    If (job queue is empty) {
        Jcurr ← φ; // make CPU idle
        Bcurr ← 0;
        return;
    }
    computeSlack ← true; // need to recompute slack
}
If (computeSlack) {
    Compute Ω(t);
    If (Ω(t) > 0)
        do_SURE ();
    else
        do_EDF();
}

```

Figure 1. The SURE Scheduler.

$J_{curr}$  and  $J_{sh}$ . Some *active* devices which are not needed by  $J_{sh}$  will be made *idle* and other *idle* devices required by  $J_{sh}$  will be made *active*.  $J_d$  is executed with a budget equal to the system slack at that time. However, if none of the ready jobs require any of the *active* devices, then the CPU is idled for a time equal to the system slack.

After  $J_d$  finishes its execution budget, the SURE scheduler is invoked again. Now, if there are no more jobs to execute, the CPU is idled and  $B_{curr}$  is made zero. All *active* devices will be made *idle*. Again when a job is released, its execution is delayed as much as possible till there is no more slack.

### Example

Consider the task set  $\{T_1, T_2\}$ ,  $T_1 = (0, 2, 1, 2, \{\lambda\})$ ,  $T_2 = (0, 5, 1, 5, \{\lambda\})$  where the deadline is equal to the period and release time is 0. Both tasks require device  $\lambda$ . The hyperperiod is 10. Fig. 3 shows both the EDF schedule and the SURE schedule for the task set where the device  $\lambda$  is idle whenever the CPU is idle (since all tasks use device  $\lambda$ ). At  $t = 0$ , the device  $\lambda$  is *idle*. With EDF the idle times in a hyperperiod are  $\{1, 1, 1\}$  time units and the total number of switches is 6. Since the task sets have zero phase, the EDF schedule will be the same in all subsequent hyperperiods. With the SURE schedule, at  $t = 0$ , the device  $\lambda$  is idled for 1 time unit. At  $t = 1$ , the highest EDF priority job is executed. Subsequent eligible jobs which require  $\lambda$  are all executed in succession. At  $t = 7$ , the ready job queue becomes empty and the CPU is idled. The device is changed to the *idle* state. At  $t = 8$ ,  $J_{1,5}$  is released. But, since  $\lambda$  is already in the *idle* state, execution of this job is delayed as much as possible. The device remains in the *idle* state till  $t = 9$ . The remaining jobs all execute in time and complete within their deadline. With slack utilization, the device idle time is 1 time unit in the beginning of the first hyperperiod. Subsequently, longer idle time of 2 time units are obtained. The total number of switches in a hyperperiod is reduced to 3 and the total idle time, of course, remains constant.

```

do.EDF(){
  If ( $J_{curr} \neq J_{high}$ ) {
     $devShare \leftarrow \{\Lambda_{T(curr)} \cap \Lambda_{T(high)}\}$ ; //  $devShare$  is the set of devices shared by  $J_{curr}$ 
    and  $J_{sh}$ 
    Make devices in  $\{\Lambda_{T(curr)} - devShare\}$  idle; // the set of active devices not required by
     $J_{sh}$  is made idle
    Make devices in  $\{\Lambda_{T(high)} - devShare\}$  active; // the set of idle devices required by  $J_{sh}$ 
    are made active
     $J_{curr} \leftarrow J_{high}$ ; // execute the highest priority job
     $B_{curr} \leftarrow e_{high}$ ;
     $noSlack \leftarrow true$ ;
  }
  return;
}
do.SURE () {
  If ( $J_{curr} \neq \phi$ ) {
    // Determine the job  $J_{sh}$  which shares the maximum number of devices with  $J_{curr}$ 
     $devShare \leftarrow \{\Lambda_{T(curr)} \cap \Lambda_{T(sh)}\}$ ;
    If ( $|devShare| == 0$ ) { // no job share any device with  $J_{curr}$ 
      Make devices in  $\{\Lambda_{T(curr)}\}$  idle; // Make all devices used by  $J_{curr}$  idle
       $J_{curr} \leftarrow \phi$ ; // Make CPU idle
    }
    else {
      Make devices in  $\{\Lambda_{T(curr)} - devShare\}$  idle;
      Make devices in  $\{\Lambda_{T(sh)} - devShare\}$  active;
       $J_{curr} \leftarrow J_{sh}$ ;
    }
  }
   $B_{curr} \leftarrow \Omega(t)$ ;
   $noSlack \leftarrow false$ ;
  return;
}

```

Figure 2. do.EDF() and do.SURE () procedures.

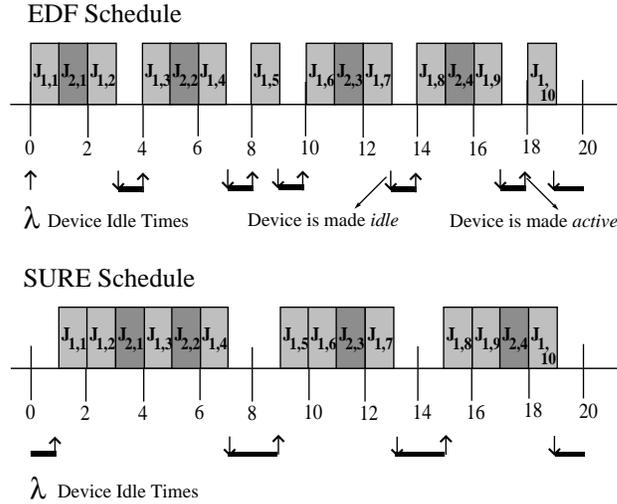


Figure 3. Schedule for  $\{T_1, T_2\}$ ,  $T_1 = (0, 2, 1, 2, \{\lambda\})$ ,  $T_2 = (0, 5, 1, 5, \{\lambda\})$

## 4 Temporal Correctness

In this section, we prove the temporal correctness of the SURE scheduling algorithm. We use the symbol  $J_i$  to denote a job, for  $i = 1$  to  $N$ , where  $N$  is the total number of jobs released in the hyperperiod. Before we prove necessity, consider the

following lemma.

**Lemma 1.1**

If  $U \geq 1$ , there is no slack, that is,  $\forall t \geq 0, \Omega(t) \leq 0$ .

**Proof:** Let the slack of a job  $J_i$  at  $t$  be  $\omega(t)$ . At  $t = 0, \omega(0) = D_i - \sum_{D_j \leq D_i} e_j$ , where  $D_i$  is the absolute deadline of  $J_i$ . At  $t = 0$ ,

$$\begin{aligned}\omega_1(0) &= D_1 - \sum_{D_j \leq D_1} e_j \\ \omega_2(0) &= D_2 - \sum_{D_j \leq D_2} e_j \\ &\dots \\ \omega_i(0) &= D_i - \sum_{D_j \leq D_i} e_j\end{aligned}$$

Since the tasks are synchronous, every task has one job with the deadline as  $H$ . Thus, there will be  $n$  jobs with deadlines as  $H$ . These set of jobs have the slack as,

$$\begin{aligned}\omega_k(0) &= H - \sum_{D_j \leq H} e_j \\ &= H - \{e_1 + e_2 + \dots + e_N\} \\ &= H - \{\text{sum of execution times of all jobs in H}\}\end{aligned}$$

$$\begin{aligned}\text{But, \{\text{sum of execution times of all jobs in H}\}} &= \sum_{i=1}^n e_i \cdot \frac{H}{p_i} \\ &= U \cdot H\end{aligned}$$

$$\begin{aligned}\text{Thus, } \omega_k(0) &= H - U \cdot H \\ &= H \cdot (1 - U)\end{aligned}$$

Since,  $U \geq 1$ ,

$$\omega_k(0) \leq 0$$

Since slack gets consumed as time progresses, the slack of a job at any time cannot be greater than its slack at time zero. Thus we have,

$$\begin{aligned}\forall t \geq 0, \omega_k(t) &\leq \omega_k(0) \leq 0 \\ \Rightarrow \omega_k(t) &\leq 0\end{aligned}$$

At any time  $t \geq 0$ , the system slack is,

$$\begin{aligned}\Omega(t) &= \min\{\omega_i(t)\}_{\forall i=1,2,\dots,N} \\ \Rightarrow \Omega(t) &\leq \omega_k(t) \leq 0 \\ \Rightarrow \Omega(t) &\leq 0\end{aligned}$$

Hence, if  $U \geq 1$ , there is no slack at any time  $t \geq 0$ . □

**Lemma 1.2**

When there is no slack, SURE reduces to EDF.

**Proof:** In the algorithm presented in Section 3, whenever  $\Omega(t) = 0$ , control goes to *do\_EDF()* procedure. If the scheduler was invoked because a new job was released, then control goes directly to *do\_EDF()*. If the scheduler was invoked because a

job finished execution,  $computeSlack$  is made *true*. When there is no slack and there are jobs to execute, the control goes to  $do\_EDF()$ .

In  $do\_EDF()$ , if the CPU had been idle till now, then a newly released job would immediately execute. If a lower priority job had been executing, it would be pre-empted by the newly released job. If there are no jobs to execute, then CPU is idled. Thus if there is no slack at all times, the highest EDF priority job is executed each time the scheduler is invoked. In addition, the job is executed immediately since there is no slack at any time to defer the execution of the job. Hence, the algorithm reduces to EDF.  $\square$

**Lemma 1.3**

*Under SURE, there is no slack in the system at the end of an idle instant, that is if  $t$  is the end of an idle instant  $\Omega(t) = 0$ .*

**Proof:** Since SURE may not execute jobs as soon as they become eligible, it is a non-work conserving schedule. Hence, at an instant when the CPU is idle, the job queue may or may not be empty. There can be no other state of the job queue when the CPU is idle. Hence, there are only two cases to consider: (a) CPU is idle because there are no jobs to execute and (b) CPU is idle but the job queue is not empty.

**Case (a): CPU is idle because there are no jobs to execute.**

Suppose the CPU is idled because there are no jobs to execute. When a job is released, the SURE scheduler is invoked. As shown in Figure 1, since  $J_{curr} = \phi$  whenever the CPU is idle,  $computeSlack$  is made *true* and system slack is computed. If there is some system slack at this time, the budget of  $J_{curr}$  is increased and CPU will continue to idle for  $\Omega(t)$  time units. When the execution budget of  $J_{curr}$  is over, the scheduler is again invoked. If there is some more system slack at this time, once again  $J_{curr}$  is scheduled with a new budget. Finally, when there is no more system slack  $do\_EDF()$  is invoked. Here, the highest priority job is selected for execution. This marks the the end of the idle instant.

**Case (b): CPU is idle but the job queue is not empty.**

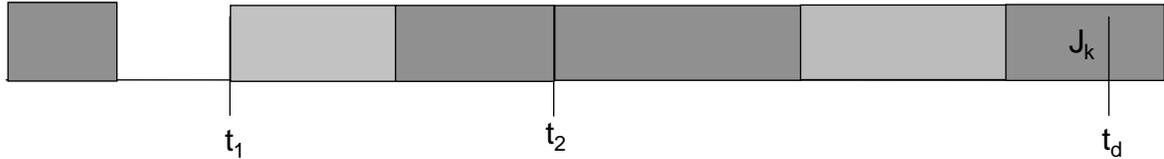
In this case, the CPU is idled because it results in the minimum number of device state switches. Here, no job shares any device with  $J_{curr}$ . Hence in  $do\_SURE()$ ,  $J_{curr}$  is made equal to  $\phi$  and the CPU is idled. The execution budget  $B_{curr}$  is made equal to the system slack at that time. As in Case (a), when the execution budget of  $J_{curr}$  is over, the scheduler is again invoked. If there is some more system slack, CPU is continued to idle with a new budget. Finally, as in Case (a), when the system slack is zero,  $do\_EDF()$  is invoked and the highest priority job at that time is executed. This marks the end of the idle instant.

Thus, in both cases, at the end of idle instant, the system slack is zero.  $\square$

**Theorem 1**

*A set of synchronous periodic tasks  $T = \{T_1, T_2, T_3, \dots, T_n\}$ , with deadlines equal to their periods, can be feasibly scheduled on a single processor with pre-emptive SURE if and only if  $\sum_{i=1}^n \frac{e_i}{p_i} \leq 1$ .*

**Proof:** For the necessity of Theorem 1, suppose that  $U > 1$ . From Lemma 1.1, we know that if  $U \geq 1$ , there is no slack. From Lemma 1.2, we know that if there is no slack at any time, then SURE reduces to EDF. Hence, we can conclude that since  $U > 1$ , SURE reduces to EDF. We know that if  $U > 1$ , EDF will fail to find a schedule. Since SURE reduces to EDF, SURE will also fail when  $U > 1$ . Thus, necessity is proved.



**Figure 4. Theorem 1**

For sufficiency, assume that  $U \leq 1$ , but tasks cannot be feasibly scheduled. In Fig. 4, let  $J_k$  be the first job to miss its deadline at  $t_d$  and  $t_1$  be the end of the last idle instant before  $t_d$ .  $t_1$  can be traced back to 0 if there are no idle instants thereafter. From Lemma 1.3, we can conclude that,

$$\Omega(t_1) = 0 \tag{2}$$

Let  $t_2$  be the latest instant before  $t_d$  such that  $\Omega(t_2) = 0$  and before which the system slack is greater than zero. This also means that the system slack is never positive in the interval  $[t_2, t_d]$ . We can quickly establish this by proving the contrapositive.

If the system slack is positive at some instant in  $[t_2, t_d]$ , then  $t_2$  cannot be the *latest* instant before  $t_d$ , before which the system slack is greater than zero. Thus, the relation  $t_2 < t_d$  holds true.

Since  $\Omega(t_1) = 0$ , by its definition,  $t_2$  cannot be less than  $t_1$ . However, if the system slack is never more than zero after  $t_1$ ,  $t_2$  could be equal to  $t_1$ . Thus we have the relation,

$$0 \leq t_1 \leq t_2 < t_d \quad (3)$$

Note that since slack could be positive in  $[t_1, t_2)$ , any job with a deadline greater than  $t_2$  may execute in the slack time in  $[t_1, t_2)$  if it reduces the number of device state switches at that time. Thus, the CPU demand in  $[t_1, t_2)$  is the demand of jobs with deadlines in the interval  $(t_1, t_2]$  as well as the demand of some jobs with deadlines greater than  $t_2$  which may execute in this interval. This CPU demand cannot be tightly bound since it depends on the device request specification of jobs executing in this interval.

However, since slack is never positive in  $[t_2, t_d]$ , no job with deadline greater than  $t_d$  will be scheduled by the SURE scheduler in this interval, i.e., no job with a lower priority than  $J_k$  will be scheduled in  $[t_2, t_d]$ . Hence the CPU demand in this interval will be the demand by jobs with deadlines in  $(t_2, t_d]$ . We can bound this demand by considering the earliest instant of time in this interval when a job of a task  $T_j$  will be released.

$$\begin{aligned} \text{Earliest time when a job of task } T_j \text{ is released in } (t_2, t_d] &= t_2 - (p_j - 1) \\ \Rightarrow \text{Effective length in } (t_2, t_d] \text{ for each task } T_j &= t_d - [t_2 - (p_j - 1)] \\ &= t_d - t_2 + (p_j - 1) \\ \Rightarrow \text{Total number of jobs of task } T_j \text{ with deadlines in } (t_2, t_d] &= \left\lfloor \frac{t_d - t_2 + p_j - 1}{p_j} \right\rfloor \end{aligned}$$

Since  $J_k$  missed its deadline at  $t_d$ , the demand by all jobs with deadlines in  $(t_2, t_d]$  is greater than the available time in the interval  $(t_2, t_d]$ . Thus,

$$(t_d - t_2) < \text{Demand of jobs with deadlines in } (t_2, t_d] \quad (4)$$

$$\text{But, Demand of jobs with deadlines in } (t_2, t_d] = \sum_{j=1}^n \left\lfloor \frac{t_d - t_2 + p_j - 1}{p_j} \right\rfloor \cdot e_j \quad (5)$$

Hence, from Equation (4) and (5) we have,

$$\begin{aligned} (t_d - t_2) &< \sum_{j=1}^n \left\lfloor \frac{t_d - t_2 + p_j - 1}{p_j} \right\rfloor \cdot e_j \\ &\leq \sum_{j=1}^n \frac{t_d - t_2 + p_j - 1}{p_j} \cdot e_j \\ &= \sum_{j=1}^n \frac{t_d - t_2}{p_j} \cdot e_j + \sum_{j=1}^n \frac{p_j - 1}{p_j} \cdot e_j \\ &= (t_d - t_2) \cdot \sum_{j=1}^n \frac{e_j}{p_j} + \sum_{j=1}^n 1 - \frac{e_j}{p_j} \\ &= (t_d - t_2) \cdot U + \sum_{j=1}^n 1 - \frac{e_j}{p_j} \\ \text{But, } \sum_{j=1}^n 1 - \frac{e_j}{p_j} &\geq 0 \\ \Rightarrow (t_d - t_2) &< (t_d - t_2) \cdot U \\ &\Rightarrow 1 < U, \text{ a contradiction} \end{aligned}$$

This implies that, if the schedule is invalid,  $U > 1$ . Hence, sufficiency is proved.  $\square$

## 5 Conclusions and work-in-progress

The SURE, online real-time scheduling algorithm was presented in this paper. We note that there are remain many implementation details to be addressed. For instance, when we use the network card as the I/O device, the non-deterministic nature of ethernet must be taken into account. In addition, the overhead involved in switching the device states must also be addressed in the implementation. At present, we are implementing the algorithm in the microC OS-II real-time OS in the Rabbit 3000 microprocessor and are currently carrying out a preliminary evaluation of the algorithm.

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