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Evaporation induced two-dimensional buckling within liquid droplet

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Evaporation of a liquid droplet containing a thin layer of surfactants atop could generate two-dimensional buckling on surfaces. Herringbone features were produced via embedded nanoparticle beds. We assign transient surface tension as the driving force for such a phenomenon. Considering the surfactant layer as a thin elastic film, a continuum model is employed to calculate the mechanical properties of the layer. Particularly, we estimated an elastic modulus of 4 GPa for the surfactant layer, indicating rather strong mechanical properties of these small molecules when they are close packed to form supramolecules via noncovalent binding. © 2009 American Institute of Physics. [doi:10.1063/1.3269930]

Buckling or wrinkling exists in numerous forms over wide length scales and their common forms include wrinkling of human skin, shrinking surfaces of dried fruits, and even the formation of mountain ridges. This phenomenon has been utilized in the field of nanofabrication, where buckling of a stiff thin film on a compliant substrate might be useful in optoelectronics, generating applications from nature-mimic compound eyes$^1$ to stretchable metal oxide semiconductors.$^2$ Generally, all these bucklings occurred in solid thin films supported by solid substrates. We learned that, beyond a critical strain, the elastic energy required to compress the solid film can be reduced by an out-of-plane bending, or the formation of buckling. Minimization of the total elastic energy leads to scaling relationships between the amplitude and wavelength of those buckled features,$^3,4$ which can be even applied in mechanical characterizations of thin polymer films.$^5,6$ In contrast, buckling of a thin film on liquid surfaces is rarely studied.$^7$

In this letter, we investigate the formation of two-dimensional (2D) buckling regulated via surfactant monolayers. Surfactants are amphiphilic molecules that have been widely used in organic/inorganic hybrid systems during nanofabrication. When concentrated molecules are dispersed in an aqueous liquid, a monolayer could cover the entire air and water interface, stabilizing the liquid droplet by reducing the surface tension. Presumably, when the liquid volume is condensed, a compression could be applied to the monolayer, inducing periodic topography features or buckling. The periodic buckling was discovered in the evaporation of a water droplet containing a very small amount (1.0 wt %) of monodispersed polystyrene spheres (Duke Scientific, Inc.). The mean sphere size is 30 or 80 nm with a standard deviation of 18%. Among this droplet, 0.1 wt % of sodium dodecylsulfate was also added as surfactants to stabilize the nanoparticles before evaporation. And we record the entire evaporation process under an optical microscope (ML8000 Meiji) equipped with a digital camera (Moticam 2000).

It is well known that, during the evaporation of a pure water droplet, the contact angle gradually increases as the droplet shrank. In contrast, the contact angle change in our droplet (weight ≈30 mg) differs due to the presence of a mixture of nanoparticles within and a monolayer of surfactants at the air-liquid interface. The droplet initially spread out as a circle with a diameter of 1.0 cm and a contact angle ($\alpha$) of 15° [phase 1, Fig. 1(a)]. Next, nanoparticles were driving from the inside of the droplet and piled as aggregated precipitates at the inner rim of the droplet [phase 2, Fig. 1(a)]. This essentially delivers a water reservoir surrounded by a bank of nanoparticles and a further evaporation created the so called “coffee-ring,”$^8$ where both the radius of the droplet $R$ and the contact angle $\alpha$ of the droplet remain relatively constant. In both phases, the liquid edge is always standing statically on the substrate (glass). Overall force acting at this edge along the horizontal direction is, $\Sigma F_x = f_{LV} \cos \alpha + f_{SL} - f_{VS} = 0$, where $f_{LV}$, $f_{VS}$, and $f_{SL}$ are the ten-

FIG. 1. (a) Schematic illustration of the 2D buckling formation process and the corresponding free-body diagrams. Phase 1, evaporation stage ($\Sigma F_x = f_{LV} \cos \alpha + f_{SL} - f_{VS} = 0$); phase 2, coffee-ring formation ($\Sigma F_x = f_{LV} \cos \alpha + f_{SL} - f_{VS} = 0$); phase 3, transition stage ($\Sigma F_x = f_{LV} + f_{SL} > 0$); and phase 4, coffee-ring evaporation ($\Sigma F_x = f_{LV} \cos \alpha + f_{SL} = 0$). A compressive transient surface force is experienced atop the surfactant layer in phase 3, leading to the 2D buckling. (b) A top view on liquid front moving toward the center during the transition stage. Shaded areas with a dark color represent aggregated nanoparticles at the corner of the liquid droplet, while areas with a light gray color for water.
tended into the liquid reservoir from region I to III, indicating the buckling occurred long before the formation of those three regions. We used tapping mode of an atomic force microscope (AFM) to characterize region II, as shown in Figs. 2(b) and 2(c). In both panels, nanospheres of 30 and 80 nm, respectively, demonstrated waving or wrinkling features over an area approximately $20 \times 20 \, \mu m^2$. On 30 nm particle film, the wavelength is 4.6 $\mu m$, and the amplitude is 50 nm, while on 80 nm particle film, they are, respectively, 5.5 $\mu m$ and 25 nm. All these wavelengths match with a prediction by Milner et al.\textsuperscript{11} that Langmuir monolayers may buckle like a plate or beam.

One might suggest that water wave or layered sliding among packed nanoparticles could have contributed to the observed 2D features, our verdict is otherwise. In particular, water wave usually bears a sinusoidal pattern, radially distributed from the center of the droplet toward the outer edge. Accordingly, concentric rings, instead of the observed zig-zag feature, should be revealed on surfaces of the particle bank. Layered sliding, on the other hand, should generate terraces of close-packed particles with a sharp step edge. These two features are all clearly different from a zig-zag feature. Hence, both motions are excluded from the cause of buckling, and the surfactant is the only component that could play a dominant role in the formation of these 2D features. Since the buckling requires the stiffness of film far larger than that of underlying substrate, the observed buckling implies that the nanoparticles formed a noncontact network rather than contacted ones. Seemingly surprising, recent observations in a drying film supported this argument.\textsuperscript{12}

The buckling features are best modeled using a quasi-quantitative means. The dynamic surface area change can be shown in Fig. 1(b). Such a change caused a reduction of the surface free energy of the liquid film, which can be described as $\Delta G = \gamma \Delta A$, where $\gamma$ is the surface tension of the film and $\Delta A = 2\pi R \Delta R$ is the area change due to the evaporation. The axial and tangential compressive strain are, respectively, $\varepsilon_1$ and $\varepsilon_2$. Then, $\varepsilon_1 = \Delta R / R$ and $\varepsilon_2 = (2\pi R - 2\pi R') / (2\pi R) = \Delta R / R$. This equation suggests the axial and tangential compressive strain will be equal if the droplet has a circular shape. Certainly, a deviation from a circular shape for the droplet is possible, which will affect the stress distribution in the surface layer.

Several mechanics models have been developed for buckling in heterogeneous structure of this type.\textsuperscript{4,5} For a pre-stretched thin film (prestrain, $\varepsilon$) of thickness $h_f$ and elastic modulus $E$ on a substrate of modulus $E_s$, releasing the pre-strain leads to purely sinusoidal displacement distributions. Mechanics models give the wavelength $\lambda = \pi h_f / \sqrt{E_s}$ and amplitude $A = h_f \sqrt{(\varepsilon / \varepsilon_{cr}) - 1}$,\textsuperscript{4,5} where $\varepsilon_{cr} = 1 / (4(3E_i / E)^{5/3})$ is the critical buckling strain given in terms of the plane-strain elastic moduli $E$ and $E_i$ of the film and substrate. The following relationship can be obtained:

$$h_f = \sqrt{\frac{\lambda^2 \varepsilon}{\pi^2}} - A^2.$$  \hspace{1cm} (1)

Both of the wavelength and amplitude can be informed from our AFM measurements. From the expression of wavelength and critical buckling strain, we can see the wavelength is proportional to $(E_i)^{1/3}$. Since the effective modulus of 30 nm particle-assembly is larger, the observed buckling wave-

![FIG. 2.](Image) Color online (a) An optical microscopic image (left) and its illustration (right) of a drying suspension with nanoparticles. An array of herringbonetype buckling feature formed prior to cracking. Scale bar: 100 $\mu m$. (b) and (c) AFM images ($20 \times 20 \, \mu m^2$) of the buckled feature near the droplet edge. The diameter of the nanoparticle is 30 nm in (b) and 80 nm in (c).
length will be smaller. This is consistent with the AFM measurements shown in Figs. 2(b) and 2(c). During the transition phase shown in Fig. 1(a), the surface energy converts to strain energy. Before the buckling the strain energy stored in the surface film is

$$ W = \frac{1}{2} \int \sigma_{ij} \varepsilon_{ij} \, dV = \frac{E \varepsilon^2}{1 - \nu} \pi R^2 h_f, \tag{2} $$

where $\sigma_{11} = \sigma_{22} = (E \varepsilon)/(1 - \nu)$, and $\nu$ is the Poisson ratio of surface film. If we assume more than half of the change of surface free energy $\Delta G$ is converted to strain energy [Eq. (2)], i.e., $\Delta G/2 = W \leq \Delta G$, then we can get

$$ \frac{\gamma}{\varepsilon h_f} \leq \frac{E}{1 - \nu} \leq \frac{2 \gamma}{\varepsilon h_f}. \tag{3} $$

Substituting Eq. (3) into Eq. (1) yields

$$ \frac{\lambda^2 \gamma}{\pi^2 h_f (A^2 + h_f^2)} \leq \frac{E}{1 - \nu} \leq \frac{2 \lambda^2 \gamma}{\pi^2 h_f (A^2 + h_f^2)}. \tag{4} $$

Here, we treat the film as incompressible or in other words, $\nu = 0.5$. In addition, due to the monolayer covering on the water surface, the surface tension $\gamma$ is 0.025 N/m.

While above analysis predicts constant amplitude ($A$) and wavelength ($\lambda$) throughout the buckling features, our measured amplitudes and wavelengths varied over the entire nanoparticles surfaces due to the nonuniform water gap between the upper surfactant layer and the underneath nanoparticles bank, generally a decreasing $A$ and an increasing $\lambda$ from the edge of the droplet to the center. We chose 80 nm, which is the largest amplitude from the AFM measurements on nanoparticle surfaces, as the amplitude for the buckled surfactant layers. In this case, the modulus, i.e., $4 \, \text{GPa}$, is the modulus of the surfactant layer, similar to the reported modulus of an ultrathin polystyrene (PS) film. Essentially, not only do surfactant and PS share similar atomic compositions but their similar molecular packing at the nanometer scale have downplayed their original difference in molecular weight to the observed mechanical properties. Moreover, this aforementioned buckling model is suitable for all two dimensional problems. For a herringbone-type buckling, Audoly and Boudaoud have had an asymptotic solution. From their solution, the kink angle of a herringbone pattern, which is $\theta$ in Fig. 2(a), should be determined by the ratio of axial and tangential compressive strains or $\tan(\theta/2) = \varepsilon_1 / \varepsilon_2$. Therefore, when the drying front is a circle shape, the kink angle is $90^\circ$ as what we observed.

In summary, we discovered a buckling phenomenon occurred during the evaporation of an aqueous droplet containing surfactant molecules and nanoparticles. We further hypothesized that transient surface force at the triple interfaces of air-water-nanoparticles to be responsible for the observed 2D zig-zag patterns. Using solid mechanics theory, we analyzed the buckled features by suggesting an elastic modulus of 4 GPa for the surfactant monolayer. We envision a deep understanding of the evaporation process before the cracking of a drying droplet is fundamentally important since it may shed light to crack growth mechanism and can lead to efforts eliminating or utilizing material failure. Moreover, this work offers an alternative means to measure mechanical properties of ultrathin films with great simplicity.

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**FIG. 3.** Modulus of the surfactant monolayer as a function of wavelength. Wavelength and amplitude were measured by AFM. Due to different gap between the particle and the liquid surface and the variable arrangement of the particle-assembly within the liquid surface, the wavelengths are not constant and a range of wavelengths is shown in the $x$-axis.