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 Searches for new physics in events with a photon and $b$-quark jet at CDF

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We have searched for evidence of physics beyond the standard model in events that include an energetic photon and an energetic b-quark jet, produced in 85 pb$^{-1}$ of $p\bar{p}$ collisions at 1.8 TeV at the Tevatron Collider at Fermilab. This signature, containing at least one gauge boson and a third-generation quark, could arise in the production and decay of a pair of new particles, such as those predicted by supersymmetry, leading to a production rate exceeding standard model predictions. We also search these events for anomalous production of missing transverse energy, additional jets and leptons ($e$, $\mu$, and $\tau$), and additional b quarks. We find no evidence for any anomalous production of $\gamma b$ or $\gamma b + X$ events. We present limits on two supersymmetric models: a model where the photon is produced in the decay $\chi^+_1 \to \gamma \chi^0_1$, and a model where the photon is produced in the neutralino decay into the gravitino LSP, $\chi^0_1 \to \gamma G$. We also present our limits in a model-independent form and test methods of applying model-independent limits.

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1. INTRODUCTION

As the world’s highest-energy accelerator, the Fermilab Tevatron collider provides a unique opportunity to search for evidence of physics beyond the standard model. There are many possible additions to the standard model, such as extra spatial dimensions, additional quark generations, additional gauge bosons, quark and lepton substructure, weak-scale gravitational effects, new strong forces, and/or supersymmetry, which may be accessible at the TeV mass scale. In addition, the source of electroweak symmetry breaking, also below this mass scale, could well be more complicated than the standard model Higgs mechanism.

New physics processes are expected to involve the production of heavy particles, which can decay into standard model constituents (quarks, gluons, and electroweak bosons) which in turn decay to hadrons and leptons. Because of the large mass of the new parent particles, the decay products will be observed with large momentum transverse to the beam ($p_T$), where the rate for standard model particle production is suppressed. In addition, in many models these hypothetical particles have large branching ratios into photons, leptons, heavy quarks or neutral non-interacting particles, which are relatively rare at large values of $p_T$ in ordinary proton-antiproton collisions.

In this paper we present a broad search for phenomena beyond those expected in the standard model by measuring the production rate of events containing at least one gauge boson, in this case the photon, and a third-generation quark, the $b$-quark, both with and without additional characteristics such as missing transverse energy ($E_T$). Accompanying searches are made within these samples for anomalous production of jets, leptons, and additional $b$-quarks, which are predicted in models of new physics. In addition, the signature of one gauge boson plus a third-generation quark is rare in the standard model, and thus provides an excellent channel in which to search for new production mechanisms.

The initial motivation of this analysis was a search for the stop squark ($\tilde{t}$) stemming from the unusual $ee\gamma\gamma E_T$ event observed at the Collider Detector at Fermilab (CDF) [1]. A model was proposed [2] that produces the photon from the radiative decay of the $\chi^0_1$ neutralino, selected to be the photino, into the $\chi^0_1$, selected to be the orthogonal state of purely higgsino, and a photon. The production of a chargino-neutralino pair, $\tilde{\chi}^+\tilde{\chi}^0_2$, could produce the $\gamma b E_T$, final state via the decay chain

$$\tilde{\chi}^+\tilde{\chi}^0_2 \to (\tilde{t}b)(\gamma\chi^0_1) \to (bE_T)(\gamma\chi^0_1).$$

(1)

This model, however, represents only a small part of the available parameter space for models of new physics. Technicolor models, supersymmetric models in which supersymmetry is broken by gauge interactions, models of new heavy quarks, and models of compositness predicting an excited $b$ quark which decays to $\gamma b$, for example, would also create this signature. We have consequently generalized the search, emphasizing the signature ($\gamma b$ or $\gamma bE_T$) rather than this specific model. We present generalized, model-independent limits. Ideally, these generic limits could be applied to actual models of new physics to provide the information on whether models are excluded or allowed by the data. Other procedures for signature-based limits have been presented recently [1,3,4].

In Sec. II we begin with a description of the data selection followed by a description of the calculation of backgrounds and observations of the data. In Sec. III we present rigorously–derived limits on both minimal supersymmetric standard model (MSSM) and gauge-mediated supersymmetry breaking (GMSB) models. Sections IV–VI present the model-independent limits. Finally, in the Appendix we present tests of the application of model-independent limits to a variety of models that generate this signature.

A search for the heavy techni-omega, $\omega_T$, in the final state $\gamma + b + \text{jet}$, derived from the same data sample, has already been published [5].

II. DATA SELECTION

The data used here correspond to 85 pb$^{-1}$ of $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV. The data sample was collected by triggering on the electromagnetic cluster caused by the photon in the central calorimeter. We use “standard” photon identification cuts developed for previous photon analyses [1], which are similar to standard electron requirements except that
there is a restriction on any tracks near the cluster. The events are required to have at least one jet with a secondary vertex found by the standard silicon detector $b$-quark identification algorithm. Finally, we apply missing transverse energy requirements and other selections to examine subsamples. We discuss the selection in detail below.

### A. The CDF detector

We briefly describe the relevant aspects of the CDF detector [6]. A superconducting solenoidal magnet provides a 1.4 T magnetic field in a volume 3 m in diameter and 5 m long, containing three tracking devices. Closest to the beamline is a 4-layer silicon microstrip detector (SVX) [7] used to identify the secondary vertices from $b$-hadron decays. A track reconstructed in the SVX has an impact parameter resolution of 19 $\mu$m at high momentum to approximately 25 $\mu$m at 2 GeV/c of track momentum. Outside the SVX, a time projection chamber (VTX) locates the $z$ position of the interaction. In the region with the radius from 30 cm to 132 cm, the central tracking chamber (CTC) measures charged-particle momenta. Surrounding the magnet coil is the electromagnetic calorimeter, which is in turn surrounded by the hadronic calorimeter. These calorimeters are constructed of towers, subdividing $15^\circ$ in $\phi$ and 0.1 in $\eta$ [8], pointing to the interaction region. The central preradiator wire chamber (CPR) is located on the inner face of the calorimeter in the central region ($|\eta|<1.1$). This device is used to determine if the origin of an electromagnetic shower from a photon was in the magnet coil. At a depth of six radiation lengths into the electromagnetic calorimeter (and 184 cm from the beamline), wire chambers with additional cathode strip readout [central electromagnetic strip chambers (CES)] measure two orthogonal profiles of showers.

For convenience we report all energies in GeV, all momenta as momentum times $c$ in GeV, and all masses as mass times $c^2$ in GeV. Transverse energy ($E_t$) is the energy deposited in the calorimeter multiplied by $\sin \theta$.

### B. Event selection

Collisions that produce a photon candidate are selected by at least one of a pair of three-level triggers, each of which requires a central electromagnetic cluster. The dominant high-$E_t$ photon trigger requires a 23 GeV cluster with less than approximately 5 GeV additional energy in the region of the calorimeter surrounding the cluster [9]. A second trigger, designed to have high efficiency at large values of $E_t$, requires a 50 GeV cluster, but has no requirement on the isolation energy.

These events are required to have no energy deposited in the hadronic calorimeter outside of the time window that corresponds to the beam crossing. This rejects events where the electromagnetic cluster was caused by a cosmic ray muon which scatters and emits bremsstrahlung in the calorimeter.

Primary vertices for the $\bar{p}p$ collisions are reconstructed in the VTX system. A primary vertex is selected as the one with the largest total $|p_t|$ attached to it, followed by adding silicon tracks for greater precision. This vertex is required to be less than 60 cm from the center of the detector along the beamline, so that the jet is well contained and the projective nature of the calorimeters is preserved.

### C. Photon

To purify the photon sample in the offline analysis, we select events with an electromagnetic cluster with $E_t > 25$ GeV and $|\eta|<1.0$. To provide for a reliable energy measurement we require the cluster to be away from cracks in the calorimeter. To remove backgrounds from jets and electrons, we require the electromagnetic cluster to be isolated. Specifically, we require that the shower shape in the CES chambers at shower maximum be consistent with that of a single photon, that there are no other clusters nearby in the CES, and that there is little energy in the hadronic calorimeter towers associated with (i.e., directly behind) the electromagnetic towers of the cluster.

We allow no tracks with $p_t>1$ GeV to point at the cluster, and at most one track with $p_t<1$ GeV. We require that the sum of the $p_t$ of all tracks within a cone of $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} = 0.4$ around the cluster be less than 5 GeV.

If the photon cluster has $E_t<50$ GeV, we require the energy in a $3 \times 3$ array of trigger towers (trigger towers are made of two consecutive physical towers in $\eta$) to be less than 4 GeV. This isolation energy sum excludes the energy in the electromagnetic calorimeter trigger tower with the largest energy. This requirement is more restrictive than the hardware trigger isolation requirement, which is approximately 5 GeV on the same quantity. In some cases the photon shower leaks into adjacent towers and the leaked photon shower energy is included in the isolation energy sum. This effect leads to an approximately 20% inefficiency for this trigger. When the cluster $E_t$ is above 50 GeV, a second trigger with no isolation requirement accepts the event. For these events, we require the transverse energy found in the calorimeter in a cone of $R=0.4$ around the cluster to be less than 10% of the cluster’s energy.

These requirements yield a data sample of 511 335 events in an exposure of 85 pb$^{-1}$ of integrated luminosity.

### D. $b$-quark identification

Jets in the events are clustered with a cone of 0.4 in $\eta - \phi$ space using the standard CDF algorithm [10]. One of the jets with $|\eta|<2$ is required to be identified as a $b$-quark jet by the displaced-vertex algorithm used in the top-quark analysis [11]. This algorithm searches for tracks in the SVX that are associated with the jet but not associated with the primary vertex, indicating they come from the decay of a long-lived particle. We require that the track, extrapolated to the interaction vertex, has a distance of closest approach greater than 2.5 times its uncertainty and pass loose requirements on $p_t$ and hit quality. The tracks passing these cuts are used to search for a vertex with three or more tracks. If no vertex is found, additional requirements are placed on the tracks, and this new list is used to search for a two-track vertex. The transverse decay length, $L_{xy}$, is defined in the transverse plane as the projection of the vector pointing from
the primary vertex to the secondary vertex on a unit vector along the jet axis. We require \(|L_{xy}|/\sigma > 3\), where \(\sigma\) is the uncertainty on \(L_{xy}\). These requirements constitute a "tag." In the data sample the tag is required to be positive, with \(L_{xy} > 0\). The photon cluster can have tracks accidentally associated with it and could possibly be tagged; we remove these events. This selection reduces the dataset to 1487 events.

The jet energies are corrected for calorimeter gaps and nonlinear response, energy not contained in the jet cone, and underlying event energy [10]. For each jet the resulting corrected \(E_t\) is the best estimate of the underlying true quark or gluon transverse energy, and is used for all jet requirements in this analysis. We require the \(E_t\) of the tagged jet in the initial \(b\gamma\) event selection to be greater than 30 GeV; this reduces the data set to 1175 events.

E. Other event selection

While the photon and \(b\)-tagged jet constitute the core of the signature we investigate, supersymmetry and other new physics could be manifested in any number of different signatures. Because of the strong dependence of signature on the many parameters in supersymmetry, one signature is (arguably) not obviously more likely than any other. For these reasons we search for events with unusual properties such as very large missing \(E_t\) or additional reconstructed objects. These objects may be jets, leptons, additional photons or \(b\) tags. This method of sifting events was employed in a previous analysis [1]. We restrict ourselves to objects with large \(E_t\) since this process is serving as a sieve of the events for obvious anomalies. In addition, in the lower \(E_t\) regime the backgrounds are larger and more difficult to calculate. In this section we summarize the requirements that define these objects.

Missing \(E_t\) (\(E_t\)) is the magnitude of the negative two-dimensional vector sum of the measured \(E_t\) in each calorimeter tower with energy above a low threshold in the region \(|\eta| < 3.6\). All jets in the event with uncorrected \(E_t\) greater than 5 GeV and \(|\eta| < 2\) are corrected appropriately for known systematic detector mismeasurements; these corrections are propagated into the missing \(E_t\). Missing \(E_t\) is also corrected using the measured momentum of muons, which do not deposit much of their energy in the calorimeter.

We apply a requirement of 20 GeV on missing \(E_t\), and observe that a common topology of the events is a photon opposite in azimuth from the missing \(E_t\), (see Fig. 2). We conclude that a common source of missing \(E_t\), occurs when the basic event topology is a photon recoiling against a jet. This topology is likely to be selected by the \(E_t\) cut because the fluctuations in the measurement of jet energy favor small jet energy over large. To remove this background, we remove events in the angular bin \(\Delta \phi (\gamma - \vec{E}_t) > 168^\circ\) for the sample, where we have raised the missing \(E_t\) requirement to 40 GeV.

We define \(H_t\) as the scalar sum of the \(E_t\) in the calorimeter added to the missing \(E_t\) and the \(p_t\) of any muons in the event. This would serve as a measure of the mass scale of new objects that might be produced.

To be recognized as an additional jet in the event, a calorimeter cluster must have corrected \(E_t > 15\) GeV and \(|\eta| < 2\). To count as an additional \(b\) tag, a jet must be identified as a \(b\) candidate by the same algorithm as the primary \(b\) jet, and have \(E_t > 30\) GeV and \(|\eta| < 2\). To be counted as an additional photon, an electromagnetic cluster is required to have \(E_t > 25\) GeV, \(|\eta| < 1.0\), and to pass all the same identification requirements as the primary photon.

For lepton identification, we use the cuts defined for the primary leptons in the top quark searches [11,12]. We search for electrons in the central calorimeter and for muons in the central muon detectors. Candidates for \(\tau\) leptons are identified only by their hadronic decays—as a jet with one or three high-\(p_t\) charged tracks, isolated from other tracks and with calorimeter energy cluster shapes consistent with the \(\tau\) hypothesis [12]. Electrons and \(\tau\) ’s must have \(E_t > 25\) GeV as measured in the calorimeter; muons must have \(p_t > 25\) GeV. Electrons and muons must have \(|\eta| < 1.0\) while \(\tau\)’s must have \(|\eta| < 1.2\). We summarize the kinematic selections in Table I.

III. BACKGROUND ESTIMATES

The backgrounds to the \(b\gamma\) sample are combinations of the standard model production of photons and \(b\) quarks and also jets misidentified as a photon ("fake" photons) or as a \(b\)-quark jet ("fake" tags or mistags). A jet may be misidentified as a photon by fragmenting to a hard leading \(\pi^0\). Other jets may fake a \(b\)-quark jet through simple mismeasurement of the tracks leading to a false secondary vertex.

We list these backgrounds and a few other smaller backgrounds in Table II. The methods referred to in this table are explained in the following sections.

The following sections begin with a discussion of the tools used to calculate backgrounds. Section III C explains why the method presented is necessary. The subsequent sections provide details of the calculation of each background in turn.

A. Photon background tools

There are two methods we use to calculate photon backgrounds, each used in a different energy region. The first employs the CES detector embedded at shower maximum in the central electromagnetic calorimeter [13]. This method is based on the fact that the two adjacent photons from a high-\(p_t\), \(\pi^0\) will tend to create a wide CES cluster, with a larger CES \(\chi^2\), when compared to the single photon expectation. The method produces an event-by-event weight based on the \(\chi^2\) of the cluster and the respective probabilities to find this \(\chi^2\) for a \(\pi^0\) versus a photon. In the decay of very high energy \(\pi^0\)'s the two photons will overlap, and the \(\pi^0\) will become indistinguishable from a single photon in the CES by the shape of the cluster. From studies of \(\pi^0\)'s from \(\rho\) decay we have found that for \(E_t > 35\) GeV the two photons coalesce and we must use a second method of discrimination that relies on the central preradiator system (CPR) [13]. This background estimator is based on the fact that the two photons from a \(\pi^0\) have two chances to convert to an electron-
TABLE I. Summary of the kinematic selection criteria for the $b\gamma + X$ sample that contains 1175 events. Also shown are the kinematic criteria for the identification of other objects, such as missing $E_t$, jets, additional $b$ jets, and leptons. The lepton identification criteria are the same as used in the top discovery.

<table>
<thead>
<tr>
<th>Object</th>
<th>Selection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isolated photon</td>
<td>$E_t &gt; 25$ GeV, $</td>
</tr>
<tr>
<td>$b$-quark jet (SVX $b$ tag)</td>
<td>$E_t &gt; 30$ GeV, $</td>
</tr>
<tr>
<td>$\Delta \phi(\gamma - E_t)$</td>
<td>$&gt;40$ GeV</td>
</tr>
<tr>
<td>Optional missing $E_t$ requirements</td>
<td>$&lt;168^\circ$</td>
</tr>
<tr>
<td>Optional other objects</td>
<td>$E_t &gt; 15$ GeV, $</td>
</tr>
<tr>
<td>Jets</td>
<td>$E_t &gt; 25$ GeV, $</td>
</tr>
<tr>
<td>Additional photons</td>
<td>$E_t &gt; 30$ GeV, SVX $b$ tag</td>
</tr>
<tr>
<td>Additional $b$-quark jets</td>
<td>$E_t &gt; 25$ GeV, $</td>
</tr>
<tr>
<td>Electrons</td>
<td>$p_t &gt; 25$ GeV, $</td>
</tr>
<tr>
<td>Muons</td>
<td>$E_t &gt; 25$ GeV, $</td>
</tr>
<tr>
<td>Tau leptons</td>
<td></td>
</tr>
</tbody>
</table>

Both these photon background methods have low discrimination power at high photon $E_t$. This occurs because the weights for a single photon and a (background) $\pi^0$ are not very different. For example, in the CES method, at an $E_t$ of 25 GeV, the probability for a photon to have a large $\chi^2$ is on the order of 20% while the background has a probability of approximately 45%. For the CPR method, typical values for a 25 GeV photon are 83% conversion probability for background and 60% for a single photon.

B. $b$-quark tagging background tools

A control sample of QCD multi-jet events is used to study the backgrounds to the identification of $b$-quark jets [14]. For each jet in this sample, the $E_t$ of the jet, the number of SVX tracks associated with the jet, and the scalar sum of the $E_t$ in the event are recorded. The probability of tagging the jet is determined as a function of these variables for both positive ($L_{xy}>0$) and negative tags ($L_{xy}<0$).

Negative tags occur due to measurement resolution and errors in reconstruction. Since these effects produce negative and positive tags with equal probability, the negative tagging probability can be used as the probability of finding a positive tag due to mismeasurement (mistags).

C. Background method

We construct a total background estimate from summing the individual sources of backgrounds, each found by different methods. In the CDF top analysis [11] one of the tagging background procedures was to apply the positive tagging probability to the jets in the untagged sample to arrive at a total tagging background estimate. A similar procedure could be considered for our sample.

However, in this analysis, a more complex background calculation is necessary for two reasons. First, the parameterized tagging background described above is derived from a sample of jets from QCD events [11] which have a different fraction of $b$-quark jets than do jets in a photon-plus-jets sample. This effect is caused by the coupling of the photon to the quark charge. Second, $b$ quarks produce B mesons which have a large branching ratio to semileptonic states that include neutrinos, producing real missing $E_t$ more often than generic jets. When a $E_t$ cut is applied, the $b$ fraction tends to increase. This effect is averaged over in the positive background parametrization so the background prediction will tend to be high at small $E_t$ and low at large $E_t$.

For these reasons, the positive tagging rate is correlated to the existence of a photon and also the missing $E_t$, when that is required. In contrast, the negative tagging rate is found not to be significantly correlated with the presence of real $b$ quarks. This is because the negative tagging rate is due only to mismeasurement of charged tracks which should not be sensitive to the flavor of the quarks.
The next sections list the details of the calculations of the individual sources of the backgrounds. Both photons and \( b \)-tagged jets have significant backgrounds so we consider sources with real photons and \( b \) tags or jets misidentified as photons or \( b \) jets ("fakes").

D. Heavy flavor Monte Carlo program

The background consisting of correctly identified photons and \( b \)-quark jets is computed with an absolutely normalized Monte Carlo program [15]. The calculation is leading order, based on \( q\bar{q} \) and \( gg \) initial states and a finite \( b \)-quark mass. The \( Q^2 \) scale is taken to be the square of the photon \( E_t \) plus the square of the \( b\bar{b} \) or \( c\bar{c} \) pair mass, \( Q^2 = E_t^2 + M^2 \). A systematic uncertainty of 30\% is found by scaling \( Q \) by a factor of two and the quark masses by 10\%. An additional 20\% uncertainty allows for additional effects which cannot be determined by simply changing the scale dependence [15].

In addition, we rely on the detector simulation of the Monte Carlo program to predict the tail of the rapidly falling \( E_t \) spectrum. The Monte Carlo program does not always predict this tail well. For example, a Monte Carlo program of \( Z \rightarrow e^+e^- \) production predicts only half the observed rate for events passing the missing \( E_t \) cut used in this analysis. We thus include an uncertainty of 100\% on the rate that events in the \( b\gamma \) sample pass the \( E_t \) cut. We combine the Monte Carlo production and \( E_t \) sources of uncertainty in quadrature. However, when the \( \gamma b\bar{b} \) and \( \gamma c\bar{c} \) backgrounds are totaled, these common uncertainties are treated as completely correlated.

E. Fake photons

The total of all backgrounds with fake photons can be measured using the CES and CPR detectors. These backgrounds, dominated by jets that fragment to an energetic \( \pi^0 \rightarrow \gamma\gamma \) and consequently are misidentified as a single photon, are measured using the shower shape in the CES system for photon \( E_t < 35 \) GeV and the probability of a conversion before the CPR for \( E_t > 35 \) GeV [16]. We find 55\% \pm 15\% [17] of these photon candidates are actually jets misidentified as photons.

For many of our subsamples we find this method is not useful due to the large statistical dilution as explained in Sec. III. This occurs because, for example, the probabilities for background (\( \pi^0 \)'s) and for signal (\( \gamma \)'s) to convert before the CPR are not too different. This results in a weak separation and a poor statistical uncertainty. We find the method returns 100\% statistical uncertainties for samples of less than approximately 25 photon candidates.

F. Real photon, fake tags

To estimate this background we start with the untagged sample, and weight it with both the CES-CPR real photon weight and the negative tagging (background) weight. This results in the number of true photons with mistags in the final sample. As discussed above, the negative tagging prediction does not have the correlation to quark flavor and missing \( E_t \) as does the positive tagging prediction.

As a check, we can look at the sample before the tagging and \( E_t \) requirements. In this sample we find 197 negative tags while the estimate from the negative tagging prediction is 312. This discrepancy could be due to the topology of the events—unlike generic jets, the photon provides no tracks to help define the primary vertex. The primary vertex could be systematically mismeasured leading to mismeasurement of the transverse decay length \( L_{xy} \) for some events. We include a 50\% uncertainty on this background due to this effect.

G. Estimate of remaining backgrounds

There are several additional backgrounds which we have calculated and found to be very small. The production of \( W\gamma \) and \( Z\gamma \) events may provide background events since they produce real photons and \( b \) or \( c \) quarks from the boson decay (\( W^\pm \rightarrow cs, Z \rightarrow b\bar{b} \)). The \( E_t \) would have to be fake, due to mismeasurement in the calorimeter. We find \( W/Z\gamma \) events in the CDF data using the same photon requirements as the search. The \( W/Z \) is required to decay leptonically for good identification. We then use a Monte Carlo program to measure the ratio of the number of these events to the number of events passing the full \( yb\bar{E}t \) search cuts. The product of these two numbers predicts this background to be less than 0.1 events.

The next small background is \( W \rightarrow e\nu \) plus jets where the electron track is not reconstructed, due either to bremsstrahlung or to pattern-recognition failure. Using \( Z \rightarrow e^+e^- \) events, we find this probability is small, about 0.5\%. Applying this rate to the number of observed events with an electron, \( b \) tag and missing \( E_t \), we find the number of events expected in our sample to be negligible.

The last small background calculation is the rate for cosmic ray events. In this case there would have to be a QCD \( b \)-quark event with a cosmic ray bremsstrahlung in time with the event. The missing \( E_t \) comes with the unbalanced energy deposited by the cosmic ray. We use the probability that a cosmic ray leaves an unattached stub in the muon chambers to estimate that the number of events in this category is also negligible.

The total of all background sources is summarized in Table III. The number of observed events is consistent with the calculation of the background for both the \( yb \) sample and the subsamples with \( E_t \).

IV. DATA OBSERVATIONS

In this section we report the results of applying the final event selection to the data. First we compare the total background estimate with the observed number of events in the \( b\gamma \) sample, which requires only a photon with \( E_t > 25 \) GeV and a \( b \)-tagged jet with \( E_t > 30 \) GeV. Since most models of supersymmetry predict missing \( E_t \), we also tabulate the backgrounds for that subsample.

Table III summarizes the data samples and the predicted backgrounds. We find 98 events have missing \( E_t > 20 \) GeV. Six events have missing \( E_t > 40 \) GeV, and only two of those
TABLE III. Summary of the primary background calculation. The $\gamma b\bar{b}$ and $\gamma c\bar{c}$ systematic uncertainties are considered 100% correlated. The column labeled $E_t>40$ GeV also includes the requirement that $\Delta \phi(\gamma-E_t)<168^\circ$. The entry for fake photons in the column labeled $E_t>40$ GeV is not measured but is estimated using the assumption that 50% of photons are fakes. This number is assigned a 100% uncertainty.

<table>
<thead>
<tr>
<th>Source</th>
<th>Events</th>
<th>Events $E_t&gt;20$</th>
<th>Events $E_t&gt;40$, $\Delta \phi$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\gamma b\bar{b}$</td>
<td>99±5.50</td>
<td>9±1.10</td>
<td>0.4±0.3±0.4</td>
</tr>
<tr>
<td>$\gamma c\bar{c}$</td>
<td>161±9.81</td>
<td>7±2.8</td>
<td>0.0±0.5±0.5</td>
</tr>
<tr>
<td>$\gamma$ + mistag</td>
<td>124±1.62</td>
<td>10±0.3±5.2</td>
<td>0.7±0.05±0.5</td>
</tr>
<tr>
<td>fake $\gamma$</td>
<td>648±69.94</td>
<td>49±22.7</td>
<td>1.0±1.0±0.2</td>
</tr>
<tr>
<td>$W\gamma$</td>
<td>6±4</td>
<td>0.8±0.6±0.8</td>
<td>0.08±0.06±0.08</td>
</tr>
<tr>
<td>$e\rightarrow\gamma$</td>
<td>0.4±0.1</td>
<td>0.4±0.1</td>
<td>0.1±0.03</td>
</tr>
<tr>
<td>cosmics</td>
<td>0±16</td>
<td>0±5</td>
<td>0</td>
</tr>
<tr>
<td>total background</td>
<td>1040±72±172</td>
<td>77±23±20</td>
<td>2.3±1.2±1.1</td>
</tr>
<tr>
<td>data</td>
<td>1175</td>
<td>98</td>
<td>2</td>
</tr>
</tbody>
</table>

FIG. 1. Comparison of the data to the background prediction (dashed line), and the baseline supersymmetry (SUSY) model of Sec. V A 2 (dotted line). The data consist of the 98 events of the $\gamma b$ data with $E_t>20$ GeV, except in (b) which contains no $E_t$ requirement. In each case the predictions have been normalized to the data. The distributions are as follows: (a) the photon $E_t$, (b) the missing $E_t$, (c) the $b$-tagged jet $E_t$, and (d) the $E_t$ of the second jet with $E_t>15$ GeV, if there is one. For display, the SUSY model event yield is scaled up by a factor of 4 for (a), (c) and (d) and a factor of 40 for (b).

FIG. 2. Comparison of the data to the background prediction (dashed line), and the the baseline SUSY model of Sec. V A 2 (dotted line), each normalized to the 98 events of the $\gamma b$ data with $E_t>20$ GeV. The distributions are as follows: (a) $H_t$ (total energy), (b) $\Delta \phi$ between the photon and the $E_t$, (c) number of jets with $E_t>15$ GeV, and (d) $\Delta \phi$ between the missing $E_t$ and the nearest jet. For display, the SUSY model event yield is scaled up by a factor of 4.
not warrant much interest unless they have many characteristics in common or they have additional unusual properties. We find two events pass the largest missing $E_t$ cut of 40 GeV; we examine those events more closely below. We also observe there are five events with large dijet mass combinations and we also look at those more closely below. In Sec. IV C we search for other anomalies in our sample.

**A. Analysis of events with large missing $E_t$**

Six events pass the *a priori* selection criteria requiring a photon, $b$ tag, and $E_t > 40$ GeV. (See Table IV.) Two of these events also pass the $\Delta \phi(\gamma - E_t) < 168^\circ$ requirement. We have examined these two events to see if there are indications of anything else unusual about them (for example, a high-$p_T$, lepton, or a second jet which forms a large invariant mass with the first $b$ jet, to take signals of GMSB and Higgsino models, respectively).

The first event (67537/59517) does not have the characteristics of a typical $b$ tag. It is a two-track tag (which has a worse signal-to-noise ratio) with the secondary vertex consistent with the beam pipe radius (typical of an interaction in the beam pipe). The two tracks have a $p_T$ of 2 and 60 GeV,

<table>
<thead>
<tr>
<th>Run/Event</th>
<th>$\gamma E_t$</th>
<th>$E_t$</th>
<th>$M(b, jet)$</th>
<th>$b E_t$</th>
<th>jets $E_t$</th>
<th>$\Delta \phi(\gamma - E_t)$</th>
<th>$\Delta \phi(j_{max} - E_t)$</th>
<th>$H_t$</th>
</tr>
</thead>
<tbody>
<tr>
<td>60951/189718</td>
<td>121</td>
<td>42</td>
<td>57</td>
<td>61</td>
<td>67,26,15</td>
<td>177</td>
<td>11</td>
<td>342</td>
</tr>
<tr>
<td>64997/119085</td>
<td>222</td>
<td>44</td>
<td>97</td>
<td>173</td>
<td>47</td>
<td>170</td>
<td>1</td>
<td>495</td>
</tr>
<tr>
<td>63684/15166</td>
<td>140</td>
<td>57</td>
<td>63</td>
<td>35</td>
<td>25,20,15</td>
<td>175</td>
<td>6</td>
<td>388</td>
</tr>
<tr>
<td>67537/59517$^*$</td>
<td>36</td>
<td>73</td>
<td>399</td>
<td>195</td>
<td>141,113,46,17</td>
<td>124</td>
<td>20</td>
<td>595</td>
</tr>
<tr>
<td>69426/104696</td>
<td>33</td>
<td>58</td>
<td>266</td>
<td>143</td>
<td>119</td>
<td>180</td>
<td>3</td>
<td>344</td>
</tr>
<tr>
<td>68464/291827$^*$</td>
<td>93</td>
<td>57</td>
<td>467</td>
<td>128</td>
<td>155,69</td>
<td>139</td>
<td>16</td>
<td>405</td>
</tr>
</tbody>
</table>

respectively; this highly asymmetric configuration is unlikely if the source is a $b$ jet. There are several other tracks at the same $\phi$ as the jet that are inconsistent with either the primary or secondary vertex. We conclude the $b$-tag jet in this event is most likely to be a fake, coming from an interaction in the beam pipe.

The second event has a typical $b$ tag but there are three jets, and all three straddle cracks in the calorimeter ($\eta = 0.97, -1.19, -0.09$), implying the $E_t$ is very likely to be mismeasured.

In both events we judge by scanning that the primary vertex is the correct choice so that a mismeasurement of the $E_t$ due to selecting the wrong vertex is unlikely. While we have scanned these two events and find they are most likely not true $\gamma b E_t$ events, we do not exclude them from the event sample as the background calculations include these sources of mismeasured events. (See Fig. 3.)

![FIG. 3. Comparison of the $\gamma b$ mass in the data to the background prediction (dashed line), normalized to the 1175 events of the $\gamma b$ data.](image)

**FIG. 4.** The distributions for (a) $M(b,j)$ and (b) $M(\gamma,b,j)$ for the $E_t > 20$ GeV events as shown in Fig. 5. Only 63 of the 98 events have a second jet and make it into this plot. The data are compared to a background prediction (dashed line), and the baseline SUSY model of Sec. V A 2 (dotted line), each normalized to the data. The Monte Carlo prediction is scaled up by a factor of 3.
TABLE V. Characteristics of events with \(M(b, j) > 300\) GeV. For a complete description of the quantities, see Table IV.

<table>
<thead>
<tr>
<th>Run/Event</th>
<th>(\gamma E_t)</th>
<th>(E_t)</th>
<th>(M(b, j))</th>
<th>(b E_t)</th>
<th>(\text{jet } E_t)'s</th>
<th>(\Delta \phi(\gamma - E_t))</th>
<th>(\Delta \phi(j_{\text{near}} - E_t))</th>
<th>(H_t)</th>
</tr>
</thead>
<tbody>
<tr>
<td>66103/52684</td>
<td>106</td>
<td>24</td>
<td>433</td>
<td>170</td>
<td>135,57</td>
<td>152</td>
<td>29</td>
<td>517</td>
</tr>
<tr>
<td>66347/273704</td>
<td>122</td>
<td>32</td>
<td>369</td>
<td>268</td>
<td>125,42</td>
<td>101</td>
<td>14</td>
<td>605</td>
</tr>
<tr>
<td>67537/59517</td>
<td>36</td>
<td>73</td>
<td>399</td>
<td>195</td>
<td>141,113,46,17</td>
<td>124</td>
<td>20</td>
<td>595</td>
</tr>
<tr>
<td>68333/233128</td>
<td>38</td>
<td>39</td>
<td>395</td>
<td>99</td>
<td>282,212</td>
<td>121</td>
<td>3</td>
<td>600</td>
</tr>
<tr>
<td>68464/291827</td>
<td>93</td>
<td>57</td>
<td>467</td>
<td>128</td>
<td>155,69</td>
<td>139</td>
<td>16</td>
<td>405</td>
</tr>
</tbody>
</table>

B. Analysis of five high-mass events

If the events include production of new, heavy particles, we might observe peaks, or more likely, distortions in the distributions of the masses formed from combinations of objects. To investigate this, we create a scatter plot of the mass of the \(b\)-quark jet and the second highest \(E_t\) jet versus the mass of the photon, \(b\)-quark jet and second highest jet in Figs. 4 and 5.

As seen in the figures, the five events at highest \(M(b, j)\) seem to form a cluster on the tail of the distribution. There are 63 events in the scatter plot which are the subset of the 98 events with \(E_t > 20\) GeV which contain a second jet. The five events include the two (probable background) events with \(E_t > 40\) GeV and \(\Delta \phi(\gamma - E_t) < 168^\circ\) and three events with large \(H_t\) (> 400 GeV). Since these events were selected for their high mass, we expect they would appear in the tails of several of the distributions such as \(H_t\). Table V shows the characteristics of these five events.

In order to see if these events are significant, we need to make an estimate of the expected background. We define the two regions indicated in Fig. 5. The small box is placed so that it is close to the five events. This is intended to maximize the significance of the excess. The large box is placed so that it is as far from the five events as possible without including any more data events. This will minimize the significance. The two boxes can serve as informal upper and lower bounds on the significance. Since these regions were chosen based on the data, the excess over background cannot be used to prove the significance of these events. These estimates are intended only to give a guideline for the significance.

We cannot estimate the background to these five events using the CES and CPR methods described in Sec. III A due to the large inherent statistical uncertainties in these techniques. We instead use the following procedure. The list of backgrounds in Sec. III defines the number of events from each source with no restriction on \(M(b, j)\). We normalize these numbers to the 63 events in the scatter plot. We next derive the fraction of each of these sources we expect at high \(M(b, j)\). We multiply the background estimates by the fractions. The result is a background estimate for the high-mass regions.

To derive the fractions of background sources expected at high \(M(b, j)\) we look at each background in turn. The fake photons are QCD events where a jet has fluctuated into mostly electromagnetic energy. For this source we use the positive \(L_{\gamma\gamma}\) background prediction [11] to provide the fraction. This prediction is derived from a QCD jet sample by parametrizing the positive tagging probability as a function of several jet variables. The probability for each jet is summed over all jets for the untagged sample to arrive at a tagging prediction. Since the prediction is derived from QCD jets we expect it to be reliable for these QCD jets also. Running this algorithm (called “Method 1” [11]) on the untagged photon and \(E_t\) sample yields the fraction of expected events in each of the two boxes. The fractions are summarized in Table VI.

The second background source considered consists of real photons with fake tags. We calculate this contribution using the measured negative tagging rate applied to all jets (i.e. before \(b\) tagging) in the sample. Finally, the real photon and heavy flavor backgrounds are calculated based on the Monte Carlo calculation. The results from estimating the fractions are shown in Table VI.

The estimates of the sources of background for the 63 events all \(M(b, j)\) have statistical uncertainties, as do the

![FIG. 5. \(M(b, j)\) versus \(M(\gamma, b, j)\) for the events with \(E_t > 20\) GeV as shown in Fig. 5. Only 63 of the 98 events have a second jet and make it into this plot. The small dots are the result of making the scatter plot for the untagged data (passing all other cuts) and weighing it with the positive tagging prediction. The estimates of background expected in the boxes are found by the method described in the text.](image)
TABLE VI. The fraction of the 63γbjEγ events for each background expected to fall into the high-M(b,j) boxes defined in Fig. 5.

<table>
<thead>
<tr>
<th>Source</th>
<th>Big box</th>
<th>Small box</th>
</tr>
</thead>
<tbody>
<tr>
<td>fake γ</td>
<td>0.080±0.007</td>
<td>0.017±0.003</td>
</tr>
<tr>
<td>γ, fake tag</td>
<td>0.112±0.009</td>
<td>0.032±0.005</td>
</tr>
<tr>
<td>γbb</td>
<td>0.10±0.03</td>
<td>0.022±0.007</td>
</tr>
<tr>
<td>γcc</td>
<td>0.08±0.04</td>
<td>0.018±0.008</td>
</tr>
</tbody>
</table>

fractions in Table VI; we include both in the uncertainty in the number of events in the high-mass boxes. We propagate the systematic uncertainties on the backgrounds to the 63 events at all M(b,j) and include the following systematics due to the fractions:

1. 50% of the real photons and mistag background calculations for the possibility that the quark and gluon content, as well as the heavy flavor fraction, in photon events may differ from the content in QCD jets.

2. 50% of the real photons and mistag background calculations for the possibility that using the positive tagging prediction to correct the Monte Carlo calculation for the Eγ cut may have a bias.

3. 100% of the real photon and real heavy flavor background calculations for the possibility that the tails in the Monte Carlo M(b,j) distribution may not be reliable.

The results of multiplying the backgrounds at all M(b,j) with the fractions expected at high M(b,j) are shown in Table VII.

The result is that we expect 5.5±1.5±1.6 events in the big box, completely consistent with the five observed. We expect 1.2±0.35±0.38 events in the small box. The probability of observing five in the small box is 1.6%, a 2.7σ effect, a posteriori.

We next address a method for avoiding the bias in deciding where to place a cut when estimating backgrounds to events on the tail of a distribution. This method was developed by the Zeus collaboration for the analysis of the significance of the tail of the Q^2 distribution [18]. Figure 6 summarizes this method. The Poisson probability that the background fluctuated to the observed number of events (including uncertainties on the background estimate) is plotted for different cut values. We use the projection of the scatter plot onto the M(b,j) axis and make the cut on this variable since this is where the effect is largest. We find the minimum probability is 1.4×10^{-3}, which occurs for a cut of M(b,j) >400 GeV. We then perform 10 000 “pseudo-experiments” where we draw the data according to the background distribution derived above and find the minimum probability each time. We find 1.2% of these experiments have a minimum probability lower than the data, corresponding to a 2.7σ fluctuation. Including the effect of the uncertainties in the background estimate does not significantly change the answer.

We note that this method is one way of avoiding the bias from deciding in what region to compare data and backgrounds after seeing the data distributions. It does not, however, remove the bias from the fact that we are investigating this plot, over all others, because it looks potentially inconsistent with the background. If we make enough plots one of them will have a noticeable fluctuation. We conclude that the five events on the tail represent something less than a 2.7σ effect.

TABLE VII. Summary of the estimates of the background at high M(b,j) in the boxes in the M(γ,b,j)-M(b,j) plane defined in Fig. 5.

<table>
<thead>
<tr>
<th>Source</th>
<th>Big box</th>
<th>Small box</th>
</tr>
</thead>
<tbody>
<tr>
<td>fake γ</td>
<td>3.3±1.5±0.5</td>
<td>0.70±0.33±0.10</td>
</tr>
<tr>
<td>γ, fake tag</td>
<td>0.97±0.09±0.69</td>
<td>0.28±0.05±0.20</td>
</tr>
<tr>
<td>γbb</td>
<td>0.75±0.26±1.18</td>
<td>0.16±0.06±0.26</td>
</tr>
<tr>
<td>γcc</td>
<td>0.44±0.26±0.79</td>
<td>0.11±0.06±0.17</td>
</tr>
<tr>
<td>total</td>
<td>5.5±1.5±1.6</td>
<td>1.24±0.35±0.38</td>
</tr>
</tbody>
</table>
A second photon. We find no events containing a hadronic decay or a muon. We find one event with an electron; its characteristics are listed in Table IX. In scanning this event, we note nothing else unusual about it.

We find 8 events of the 1175 which have a photon and $b$-tagged jet containing a second $b$-tagged jet with $E_t > 30$ GeV. (Out of the 1175, only 200 events have a second jet with $E_t > 30$ GeV.) Unfortunately, this is such a small sample that we cannot use the background calculation to find the expected number of these events (the photon background CES-CPR method returns 100% statistical uncertainties). One of the events with two tags has 30 GeV of missing $E_t$, so it is in the 98-event $E_t > 20$ GeV sample.

V. LIMITS ON MODELS OF SUPERSYMMETRY

In the following sections we present limits on three specific models of supersymmetry [19]. Each of these models predicts significant numbers of events with a photon, a $b$-quark jet and missing transverse energy (i.e. $\gamma bE_t$).

As is typical for supersymmetry models, each of these shows the problems in the process of choosing a model and presenting limits on it. Each of these models is very specific and thus represents a very small area in a very large parameter space. Consequently the odds that any of these is the correct picture of nature is small. They are current theories devised to address current concerns and may appear dated in the future. (This aspect is particularly relevant to the experimentalists, who often publish their data simultaneously with an analysis depending on a current model.) In addition these models can show sensitivitiy to small changes in the parameters.

The first model is based on a particular location in MSSM parameter space which produces the signature of $\gamma bE_t + X$. We consider both direct production of charginos and neutralinos and, as a second model, indirect production of charginos and neutralinos through squarks and gluinos. The third model is based on the gauge-mediated concept, discussed further below.

A. $\tilde{\chi}_1^{0} \rightarrow \gamma\tilde{\chi}_1^{0}$ model

This theoretical model was originally proposed in the context of the anomalous CDF $ee\gamma\gamma E_t$ event [1,2]. Here, however, we go beyond the constraints of this single event and only retain the essential elements of the model, optimized for CDF detector acceptance and efficiency. This is a MSSM

<table>
<thead>
<tr>
<th>$\text{Min } N_{\text{jet}}$</th>
<th>$\text{Observed, } E_t &gt; 0 \text{ GeV}$</th>
<th>$\text{Expected, } E_t &gt; 0 \text{ GeV}$</th>
<th>$\text{Observed, } E_t &gt; 20 \text{ GeV}$</th>
<th>$\text{Expected, } E_t &gt; 20 \text{ GeV}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1175</td>
<td>$1040 \pm 72 \pm 172$</td>
<td>98</td>
<td>$77 \pm 23 \pm 20$</td>
</tr>
<tr>
<td>2</td>
<td>464</td>
<td>$394 \pm 44 \pm 63$</td>
<td>63</td>
<td>$39 \pm 18 \pm 12$</td>
</tr>
<tr>
<td>3</td>
<td>144</td>
<td>$82 \pm 24 \pm 14$</td>
<td>25</td>
<td>$-8 \pm 12 \pm 3$</td>
</tr>
<tr>
<td>4</td>
<td>36</td>
<td>$17 \pm 11 \pm 3$</td>
<td>7</td>
<td>$-$</td>
</tr>
<tr>
<td>5</td>
<td>10</td>
<td>$-$</td>
<td>3</td>
<td>$-$</td>
</tr>
<tr>
<td>6</td>
<td>5</td>
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</tr>
<tr>
<td>7</td>
<td>2</td>
<td>$-$</td>
<td>0</td>
<td>$-$</td>
</tr>
<tr>
<td>8</td>
<td>1</td>
<td>$-$</td>
<td>0</td>
<td>$-$</td>
</tr>
</tbody>
</table>
model without any specific relation to a high-energy theory. It does not assume high-energy constraints such as the unification of the sfermion or scalar masses as is assumed in the models inspired by supergravity (SUGRA) [19]. In this section and the following section we develop a baseline model point in parameter space. The final limits on this model will be found for this point and for some variations around this point.

1. Direct gaugino production in the \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) model

The first part of the model [2] is a light stop squark \( \tilde{t}_1 \), the superpartner to the top quark. In this model the \( \tilde{\chi}_1^\pm \) then decays to \( \tilde{t}_2 b \) and the \( \tilde{t}_1 \) decays to \( \tilde{\chi}_1^0 c \). The second important feature of the model is the decay \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) which dominates in a particular region of MSSM parameter space. With these decays dominating, any event where a \( \tilde{t}_1 \) and a \( \tilde{\chi}_1^0 \) is produced, either directly or indirectly through the strong production and decays of squarks and gluinos, will contain a photon, a \( b \)-quark jet and missing \( E_T \).

The heart of the model [2] is the decay \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) so we examine in detail the parameter space where this decay dominates. The branching ratio of this decay is large when one of the neutralinos is a pure photino and one is pure Higgsino. To make a pure photino, we set \( M_1 = M_2 \). The photino mass is then equal to \( M_2 \). To make a pure Higgsino we set \( \tan \beta = 1 \). To avoid the theoretical bias against a very small \( \tan \beta \) [which makes the top Yukawa coupling go to infinity before the grand unified theory (GUT) scale] we will use \( \tan \beta = 1.2 \). In this case, the Higgsino mass is approximately equal to \( |\mu| \). The above is purely a result of the form of the neutralino mass matrix. For definitions of these model parameters and discussions of their roles in SUSY models please see [19].

This leaves two free parameters to define the charginos and neutralinos, \( M_2 \) and \( \mu \). Figure 8 shows five regions in the \( \mu-M_2 \) plane; Table X summarizes the regions. First we note that in region 5 (\( \mu > 0 \)) we do not observe the decay \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) because typically \( \tilde{\chi}_1^0 < \tilde{\chi}_2^0 \) and \( \tilde{\chi}_2^0 \to \tilde{Z}_1 \tilde{\chi}_1^0 \).

For \( \mu < 0 \), there are four regions. In region 2, which is the region suggested in [2], the \( \tilde{\chi}_1^0 \) is the photino, \( \tilde{\chi}_2^0 \) is the Higgsino, and the decay \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) dominates. In region 3, \( \tilde{\chi}_2^0 \) is the Higgsino and \( \tilde{\chi}_1^0 \) is the photino and the photon decay still dominates. In region 1 the photon has become so heavy it is now the \( \tilde{\chi}_3^0 \). In region 4, the Higgsino has become the \( \tilde{\chi}_3^0 \). In regions 3 and 4 it is still possible to get photon decays, sometimes even \( \tilde{\chi}_1^0 \to \gamma \tilde{\chi}_2^0 \).

We choose to concentrate on region 2 where the photon plus \( b \) decay signature can be reliably estimated by the Monte Carlo event generator PYTHIA [20]. The \( \tilde{\chi}_2^0 \to \gamma \tilde{\chi}_1^0 \) decay dominates here. We also note that in this region the cross section for \( \tilde{\chi}_2^0 \tilde{\chi}_2^0 \) is \( 3-10 \) times larger than the cross section for \( \tilde{\chi}_2^0 \tilde{\chi}_2^0 \) even though the \( \tilde{\chi}_2^0 \) is significantly heavier than the \( \tilde{\chi}_1^0 \). This is due to the large \( \tilde{W} \) component of the \( \tilde{\chi}_2^0 \).

Since region 2 is approximately one dimensional, we scan in only one dimension, along the diagonal, when setting limits on \( \tilde{\chi}_2^0 \tilde{\chi}_2^0 \) production. To decide where in the region to place the model, we note that the mass of \( \tilde{\chi}_3^0 \) equals \( M_2 \) and the mass of \( \tilde{\chi}_1^0 = |\mu| \) in this region. To give the photon added boost for a greater sensitivity, we will set \( M_2 \) significantly larger than \( |\mu| \). This restricts us to the upper part of region 2. The dotted line in Fig. 8 is the set of points defined by all these criteria and is given by \( M_2 = 0.89|\mu| + 39 \) GeV.

### TABLE IX. Characteristics of the one event with a photon, tagged jet, and an electron.

<table>
<thead>
<tr>
<th>Run/Event</th>
<th>( E_T )</th>
<th>( \mathcal{E}_T )</th>
<th>( M(\gamma, \mathcal{E}_T) )</th>
<th>( \Delta \phi(\gamma - \mathcal{E}_T) )</th>
<th>( H_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>63149/4148</td>
<td>42</td>
<td>17</td>
<td>21</td>
<td>106</td>
<td>43</td>
</tr>
</tbody>
</table>

![Fig. 8](image-url)
The next step is to choose a $\tilde{t}$ mass. It is necessary that $\tilde{\chi}_1^0 < \tilde{t} < \tilde{\chi}_1^-$ for the decay $\tilde{\chi}_1^+ \rightarrow t\tilde{\chi}_1^0$ to dominate. We find that in region 2, $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$. If the $\tilde{t}$ mass is near the $\tilde{\chi}_1^-$, the $b$ will only have a small boost, but the $\tilde{\chi}_1^0$ in the decay $\tilde{t} \rightarrow c\tilde{\chi}_1^-$ will have a greater boost, giving greater $E_t$. If the $\tilde{t}$ mass is near the $\tilde{\chi}_1^-$, the opposite occurs. In Monte Carlo studies, we find considerably more sensitivity if the $\tilde{t}$ mass is near the $\tilde{\chi}_1^0$. We set the $\tilde{t}$ mass to be $M_{\tilde{t}^0} = 5 \text{ GeV}$. Since the $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0$ production cross section is larger than $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ and will be detected with better efficiency, when we simulate direct production we set the Monte Carlo program to produce only $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0$ pairs. The final limit is expressed as a cross section limit plotted versus the $\tilde{\chi}_1^0$ mass (which is very similar to the $\tilde{\chi}_2^0$ mass). This model is designed to provide a simple, intuitive signature that is not complicated by branching ratios and many modes of production.

For the baseline model, we chose a value of $\mu$ near the exclusion boundary of current limits [21] on a $\tilde{t}$ which decays to $c\tilde{\chi}_1^0$. The point we chose is $M_{\tilde{\chi}_1^0} = 80 \text{ GeV}$. From the above prescription, this corresponds to $M_{\tilde{\chi}_1^0} = \mu = 80 \text{ GeV}$, $M_{\tilde{\chi}_2^0} = M_{\tilde{\chi}_1^0} = 110 \text{ GeV}$, and $M_{\tilde{\chi}_1^0} = 85 \text{ GeV}$. This point, indicated by the dot in Fig. 8, gives the lightest mass spectrum with good mass splittings that is also near the exclusion boundary from the CERN $e^+e^-$ collider LEP and DO Collaborations.

2. Squarks and gluinos

Now we address the squarks and gluinos, which can produce $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ in their decays, and sleptons, which can appear in the decays of charginos and neutralinos. We will set the squarks (the lighter $\tilde{t}$ and both left and right $\tilde{u}$, $\tilde{d}$, $\tilde{s}$ and $\tilde{c}$) to 200 GeV and the gluino to 210 GeV. The heavier $\tilde{t}$ and $\tilde{b}$ are above 1 TeV. The gluino will decay to the squarks and their respective quarks. The squarks will decay to charginos or neutralinos and jets. This will maximize the production of $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ and therefore the sensitivity.

This brings us to the limit on indirect production in the $\tilde{\chi}_2^0 \rightarrow \gamma\tilde{\chi}_1^0$ model. The chargino and neutralino parameters are fixed at the baseline model parameters. We then vary the gluino mass and set the squark mass according to $M_{\tilde{g}} = M_{\tilde{Q}} + 10 \text{ GeV}$. The limit is presented as a limit on the cross section plotted versus the gluino mass. When the gluino mass crosses the $t\bar{t}$ threshold at 260 GeV, the gluino can decay to $t\bar{t}$ and production of $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ decreases. However, since all squarks are lighter than the gluino, the branching ratio to the $\tilde{t}$ is limited and production will not fall dramatically.

Some remaining parameters of the model are now addressed. Sleptons could play a role in this model. They have small cross sections so they are not often directly produced, but if the sleptons are lighter than the charginos, the charginos can decay into the sleptons. In particular, the chargino decay $\tilde{c}\tilde{b}$ may be strongly suppressed if it competes with a slepton decay. We therefore set the sleptons to be very heavy so they do not compete for branching ratios. We set $M_A$ large. The lightest Higgs boson turns out to be only 87 GeV due to the corrections from the light third-generation squarks. This is below current limits so we attempted to tune the mass to be heavier and found it was difficult to achieve, given the light $\tilde{t}$ and low tan $\beta$.

Using the PYTHIA Monte Carlo program, we find that 69% of all events generated with squarks and gluinos have the decay $\tilde{\chi}_2^0 \rightarrow \gamma\tilde{\chi}_1^0$, 58% have the decay $\tilde{\chi}_1^\pm \rightarrow \tilde{b}$, and 30% have both. (To be precise, the light stop squark was excluded from this exercise, as it decays only to $c\tilde{\chi}_1^0$. A light stop pair thus gives the signature $c\bar{c} + E_t$, one of the signatures used to search for it, [21,22] but it is not of interest here.)

### 3. Acceptances and efficiencies

This section describes the evaluation of the acceptance and efficiency for the indirect production of $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ through squarks and gluinos and the direct production of $\tilde{\chi}_2^0 \rightarrow \gamma\tilde{\chi}_2^0$ in the MSSM model of $\tilde{\chi}_2^0 \rightarrow \gamma\tilde{\chi}_1^0$. We use the PYTHIA Monte Carlo program with the CTEQ4L parton distribution functions (PDFs) [23]. The efficiencies for squark and gluino production at the baseline point are listed in Table XI.

The total efficiencies, which will be used to set production limits below, are listed in Table XII for the production of $\tilde{\chi}_1^\pm \rightarrow t\tilde{\chi}_1^0$ through squarks and gluinos, and in Table XIII for direction production. Typical efficiencies are 2–3% in the former case, and 1% in the latter.

### 4. Systematic uncertainty

Some systematics are common to the indirect production and the direct production. The efficiencies of the isolation requirement in the Monte Carlo calculation and $Z \rightarrow e^+e^-$ control sample cannot be compared directly due to differences in the $E_t$ spectra of the electromagnetic cluster, and the
TABLE XII. Efficiency times acceptance and limits on indirect production of $\tilde{\chi}_0^0 \tilde{\chi}_1^0$ though squarks and gluinos. Approximately 30\% of events contain the decays $\tilde{\chi}_1^0 \rightarrow \gamma \tilde{\chi}_0^0$ and $\tilde{\chi}_i^0 \rightarrow \bar{b}b$. The efficiencies in this table are found as the number of events passing all cuts divided by the number of events that contain both of these decays. The product of the cross section times the branching ratio listed in each case is for all open channels of SUSY production. Masses are given in GeV (following our convention of quoting $M \times c^2$) and cross sections are in pb. The second row is the baseline point.

<table>
<thead>
<tr>
<th>$M_{\tilde{\chi}_1}^0$ (GeV)</th>
<th>$M_{\tilde{\chi}_2}^0$ (GeV)</th>
<th>$\sigma_{th} \times BR$ (pb)</th>
<th>$A \epsilon$ (%)</th>
<th>$\sigma_{95% , lim} \times BR$ (pb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>185</td>
<td>175</td>
<td>16.8</td>
<td>1.97</td>
<td>3.76</td>
</tr>
<tr>
<td>210</td>
<td>200</td>
<td>7.25</td>
<td>2.98</td>
<td>2.49</td>
</tr>
<tr>
<td>235</td>
<td>225</td>
<td>3.49</td>
<td>3.23</td>
<td>2.30</td>
</tr>
<tr>
<td>260</td>
<td>250</td>
<td>1.94</td>
<td>2.69</td>
<td>2.76</td>
</tr>
<tr>
<td>285</td>
<td>275</td>
<td>1.24</td>
<td>2.16</td>
<td>3.45</td>
</tr>
</tbody>
</table>

multiplicity and $E_t$, spectra of associated jets. The difference (14\%) is taken to be the uncertainty in the efficiency of the photon identification cuts. The systematic uncertainty on the $b$-tagging efficiency (9\%) is the statistical uncertainty in comparisons of the Monte Carlo calculation and data. The systematic uncertainty on the luminosity (4\%) reflects the stability of luminosity measurements.

We next evaluate systematics specifically for the indirect production. The baseline parton distribution function is CTEQ4L. Comparing the efficiency with this PDF to the production. The baseline parton distribution function is CTEQ4L. Comparing the efficiency with this PDF to the production. The baseline parton distribution function is CTEQ4L.

Evaluating the same systematics for the direct production, we find the uncertainty from the choice of the PDF is 5\%, from the ISR/FSR is 2\%/9\%, and from the jet energy scale is 4\%. In quadrature, the total systematic uncertainty for the direct production is 18\%.

Evaluating the same systematics for the direct production, we find the uncertainty from the choice of the PDF is 5\%, from the ISR/FSR is 2\%/9\%, and from the jet energy scale is 4\%. In quadrature, the total systematic uncertainty for the direct production is 18\%.

5. Limits on the $\tilde{\chi}_0^0 \rightarrow \gamma \tilde{\chi}_1^0$ model, indirect production

To calculate an approximate upper limit on the number of $\gamma b E_t$ events from squark and gluino production, we use the limit implied from the observed two events, including the effect of the systematic uncertainties [26,27]. We divide the Poisson probability for observing $\leq 2$ events for a given expected signal and background, convoluted with the uncertainties, by the Poisson probability for observing $\leq 2$ events for a given background only, also convoluted with the uncertainties. The number of expected signal events is increased until the ratio falls below 5\%, leading to an approximate 95\% confidence level limit of 6.3 events. Other limits in this paper are computed similarly.

This upper limit, the efficiency described above (also see Table XII), and the luminosity, 85 pb$^{-1}$, are combined to find the cross section limit for this model. The theoretical cross section is calculated at NLO using the PROSPINO program [28]. The effect is to uniformly increase the strong interaction production cross sections by 30\% (improving the limit). At the baseline point (including squarks and gluinos) described above, we expect 18.5 events, so this point is excluded. Next we find the limit as a function of the gluino mass. The squark mass is 10 GeV below the gluino mass and the rest of the sparticles are as in the baseline point. We can exclude gluinos out to a mass of 245 GeV in this model. The limits are displayed in Table XII and Fig. 9.

6. Limits on the $\tilde{\chi}_3^0 \rightarrow \gamma \tilde{\chi}_1^0$ model, direct production

In this case the number of observed events (two) is convoluted with the systematic uncertainty to obtain an upper limit of 6.4 events (95\% C.L.). To calculate the expected number of events from the direct production of $\tilde{\chi}_3^0 \rightarrow \gamma \tilde{\chi}_1^0$ we vary $\mu$, and calculate the $M_1$ and $M_2$ as prescribed above. The results are shown in Table XIII and Fig. 10. For these values of the model parameters, the branching ratios $\tilde{\chi}_3^0 \rightarrow \bar{b}b$ and $\tilde{\chi}_2^0 \rightarrow \gamma \tilde{\chi}_1^0$ are 100\%.

TABLE XIII. Efficiencies and limits on direct production of $\tilde{\chi}_3^0 \rightarrow \gamma \tilde{\chi}_1^0$. Branching ratios $\tilde{\chi}_3^0 \rightarrow \gamma \tilde{\chi}_1^0$ and $\tilde{\chi}_1^0 \rightarrow \bar{b}b$ are 100\%. Masses are in GeV and the cross sections are in pb. The third row is the baseline point.

<table>
<thead>
<tr>
<th>$M_{\tilde{\chi}_1}^0 = \mu$</th>
<th>$M_{\tilde{\chi}<em>2}^0 = M</em>{\tilde{\chi}_3}^0$</th>
<th>$M_{\tilde{\chi}_4}^0$</th>
<th>$M_{\tilde{\chi}_5}^0$</th>
<th>$M_{\tilde{\chi}_6}^0$</th>
<th>$\sigma_{th}$</th>
<th>$A \epsilon$ (%)</th>
<th>$\sigma_{95% , lim}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>61</td>
<td>71</td>
<td>110</td>
<td>30</td>
<td>0.23</td>
<td>0.93</td>
<td>8.06</td>
</tr>
<tr>
<td>62</td>
<td>95</td>
<td>94</td>
<td>130</td>
<td>67</td>
<td>0.034</td>
<td>1.41</td>
<td>5.33</td>
</tr>
<tr>
<td>79</td>
<td>110</td>
<td>108</td>
<td>140</td>
<td>85</td>
<td>0.018</td>
<td>1.29</td>
<td>5.85</td>
</tr>
<tr>
<td>93</td>
<td>123</td>
<td>118</td>
<td>150</td>
<td>98</td>
<td>0.0075</td>
<td>1.34</td>
<td>5.58</td>
</tr>
<tr>
<td>118</td>
<td>146</td>
<td>140</td>
<td>170</td>
<td>123</td>
<td>0.0022</td>
<td>1.27</td>
<td>5.94</td>
</tr>
</tbody>
</table>
SUSY model. The branching ratios are smaller than the measured limits by 1–3 orders of magnitude, and no mass limit on the squarks and gluinos which decay to charginos and neutralinos. The overall branching ratio to the $\chi^0_1$ topology is approximately 30%.

As can be seen from Fig. 10, the predicted rates from direct production are smaller than the measured limits by 1–3 orders of magnitude, and no mass limit on the $\chi^+_2$ mass can be set.

B. Gauge-mediated model

This is the second SUSY model [19] which can give substantial production of the signature $\gamma bE_t$. In this model the length Higgs boson is 100 GeV. The masses are in GeV.

![Graph](image-url)

**FIG. 9.** The limits on the cross section times the branching ratio for SUSY production of $\gamma bE_t$ events in the $\chi^0_1 \rightarrow \gamma \chi^0_1$ model. All production processes have been included; the dominant mode is the production of squarks and gluinos which decay to charginos and neutralinos. The overall branching ratio to the $\gamma bE_t$ topology is approximately 30%.

![Graph](image-url)

**FIG. 10.** The limits on the $\chi^0_2 \rightarrow \chi^0_1 \chi^+_1$ cross section in the $\chi^0_2 \rightarrow \chi^0_1 \gamma$ SUSY model. The branching ratios $\chi^0_2 \rightarrow \gamma \chi^0_1$ and $\chi^+_1 \rightarrow t b \rightarrow (\chi^0_1 c) b$ are taken to be 100%.

The first point appears to have an unusually large efficiency difference between the mass of the standard model particles and their SUSY partners is mediated by gauge (the usual electromagnetic, weak, and strong) interactions [29] instead of gravitational interactions as in SUGRA models. The SUSY model is assumed broken in a hidden sector. Messenger particles gain mass through renormalization loop diagrams which include the hidden sector. SUSY particles gain their mass through loops which include the messenger particles.

This concept has the consequence that the strongly interacting squarks and gluinos are heavy and the right-handed sleptons are at the same mass scale as the lighter gauginos. A second major consequence is that the gravitino is very light (eV scale) and becomes the LSP. The source of the $b$ quarks is no longer the third generation squarks, but the decays of the lightest Higgs boson. If the lightest neutralino is mostly Higgsino, the decay $\chi^0_1 \rightarrow h G$ can compete with the decays $\chi^0_1 \rightarrow ZG$ and $\chi^0_1 \rightarrow \gamma G$. The Higgs boson decays to $b \bar{b}$ as usual. Since SUSY particles are produced in pairs, each event will contain two cascades of decays down to two $\chi^0_1$s, each of which in turn will decay by one of these modes. If one decays to a Higgs boson and one decays to a photon, the event will have the signature of a photon, at least one $b$-quark jet, and missing $E_t$.

We will use a minimal gauge-mediated model with one exception. This MGMSB model has five parameters, with the following values:

- $\Lambda = 61–90$ TeV, the effective SUSY-breaking scale;
- $M/\Lambda = 3$, where $M$ is the messenger scale;
- $N=2$ the number of messenger multiplets;
- $\tan \beta = 3$;
- the sign of $\mu < 0$.

We will compute the MGMSB model using the GMSB option of ISAJET [30]. We then reenter the model using the MSSM options so that we can make one change: we set $\mu = -0.75M_1$. This makes the lightest neutralino a Higgsino so the branching ratio for $\chi^0_1 \rightarrow h G$ will be competitive with $\chi^0_1 \rightarrow \gamma G$. We produce all combinations of $\chi^+_1$ and $\chi^0_1$, which are the only significant cross sections. We vary $\Lambda$ which varies the overall mass scale of the supersymmetric particles.

The model masses and branching ratios are given in Table XIV. The branching ratio is defined as the number of events with $\chi^0_1 \rightarrow \gamma G$ and $\chi^0_1 \rightarrow h G$ divided by the number of events produced from all sources predicted by the model. We are using ISAJET with the CTEQ4L parton distribution function.

**TABLE XIV.** The models used in the limits on the GMSB scenario. The lightest Higgs boson is 100 GeV. The masses are in GeV and the branching ratios are in %.

<table>
<thead>
<tr>
<th>$M^0_{\chi^0_1}$</th>
<th>$M^0_{\chi^0_2}$</th>
<th>$M^+_{\chi^+_1}$</th>
<th>$BR(\chi^0_1 \rightarrow \gamma G)$</th>
<th>$BR(\chi^0_1 \rightarrow h G)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>113</td>
<td>141</td>
<td>130</td>
<td>90</td>
<td>2</td>
</tr>
<tr>
<td>132</td>
<td>157</td>
<td>147</td>
<td>62</td>
<td>18</td>
</tr>
<tr>
<td>156</td>
<td>178</td>
<td>170</td>
<td>33</td>
<td>40</td>
</tr>
<tr>
<td>174</td>
<td>194</td>
<td>186</td>
<td>22</td>
<td>50</td>
</tr>
</tbody>
</table>

052006-16
TABLE XV. Efficiencies and limits on direct production of $\chi'^{+}_1\chi'^{0}_1$ in the GMSB scenario. Branching ratios are not included in these efficiencies. The first row has an inflated efficiency due to the definition of the branching ratio. The units of $A\varepsilon$ and the branching ratio are % and the cross sections are in pb.

<table>
<thead>
<tr>
<th>$A\varepsilon$</th>
<th>BR</th>
<th>$\sigma_{\alpha}\times BR$</th>
<th>$\sigma_{\alpha 5% lim}\times BR$</th>
</tr>
</thead>
<tbody>
<tr>
<td>27.4</td>
<td>3</td>
<td>0.010</td>
<td>0.27</td>
</tr>
<tr>
<td>7.5</td>
<td>20</td>
<td>0.0402</td>
<td>1.00</td>
</tr>
<tr>
<td>8.4</td>
<td>23</td>
<td>0.0230</td>
<td>0.89</td>
</tr>
<tr>
<td>11.4</td>
<td>18</td>
<td>0.0111</td>
<td>0.66</td>
</tr>
</tbody>
</table>

because of other sources for $b$ quarks which are not reflected in the definition of the signal branching ratio. We use the systematic uncertainties evaluated using the direct production of the $\chi'^{0}_2\to\gamma\chi'^{0}_1$ model. Taking the two events observed, and convoluting with a 20% systematic uncertainty gives an upper limit of 6.4 events observed at 95% C.L. The final limits on this model are presented in Table XV and are displayed in Fig. 11. Again, one can see that the experimental sensitivity is not adequate to set a mass limit (this time on the $\tilde{\chi}_1^0$ mass) by several orders of magnitude.

VI. MODEL-INDEPENDENT LIMITS

As described in the Introduction, there are several advantages to presenting limits of searches in a model-independent form. In the previous sections we derived limits on models of supersymmetry and presented the results as a limit on a cross section times branching ratio for a specific model, $(\sigma \times BR)_{\alpha 5\% lim} = N_{\alpha 5\% lim}/L A\varepsilon$, where $N_{\alpha 5\% lim}$ is the 95% confidence level on the number of events of anomalous production and $L$ is the integrated luminosity. We make a distinction between the acceptance, $A$, which is defined as the probability that an object passes $E_t$, $\eta$, and $\Delta\Phi$ cuts, and the efficiency, $\varepsilon$, which is the probability of events surviving all other sources of inefficiencies, such as photon identification cuts or $b$-tagging requirements, which is detector-specific. The acceptance may be calculated from kinematic and geometric criteria alone, so an experienced worker in the field can compute it using only a Monte Carlo event generator program, while the efficiency requires access to the full detector simulation and, typically, multiple control samples. In our formulation, $N_{\alpha 5\% lim}$ includes the degradation in sensitivity due to uncertainties on $A\varepsilon$, luminosity, and background subtractions, when they are included, as well as the statistical upper limit on the number of events.

In the case of model-independent limits, there is no model to determine the efficiency and therefore we report a limit on $(\sigma \times BR \times A\varepsilon)_{\alpha 5\% lim} = N_{\alpha 5\% lim}/L$. These limits, which are presented in the next section, do not have an immediate interpretation. (They do imply, however, a cross section range that we are not sensitive to, even with perfect efficiency.) In order to determine the meaning of these limits, in particular if a model is excluded or not, there must still be a mechanism for an interested physicist to calculate $A\varepsilon$ for the model, and we develop three methods in the Appendix.

A. Model-independent limits on $ybX$ signatures

The limit on $(\sigma \times BR \times A\varepsilon)_{\alpha 5\% lim}$ for the $ybE_t$ signature is then 0.069 pb. Adding the 4% luminosity uncertainty we find the cross section limit increases to 0.070 pb. If we also add the 22% uncertainty in $A\varepsilon$ from the WW limits (a typical uncertainty on an efficiency for this signature) discussed in the Appendix, we find the cross section limit increases 10% to 0.077 pb. This is the final model-independent limit on the signature $ybE_t$. The limit on the $yb$ signature before any $E_t$ requirement is 5.9 pb and the limit from the $ybE_t$ signature from the 98-event sample with $E_t>20$ GeV is 0.99 pb.

The search for other objects in these events is described in Secs. II E and IV C. When we find no events, we can set a 95% confidence level limit on $(\sigma \times BR \times A\varepsilon)_{\alpha 5\% lim}$ of 0.038 pb assuming 4% uncertainty in the luminosity and 22% uncertainty in the efficiency. This would apply to the searches for events with an additional photon, a muon or tau. For events with an additional electron, we observe one event and our limit becomes 0.057 pb.

For events with $N$ or more jets as shown in Fig. 7, we find the limits listed in Table XVI.

VII. CONCLUSIONS

We have searched in 85 pb$^{-1}$ of CDF data for anomalous production of events with a high-$E_t$ photon and a $b$-tagged
jet. We find 1175 events with a photon with $E_t > 25$ GeV and a $b$-tagged jet with $E_t > 30$ GeV, versus 1040 ± 186 expected from standard model backgrounds. Further requiring missing transverse energy $E_T > 40$ GeV, in a direction not back-to-back with the photon ($\Delta \phi < 168^\circ$), we observed two events versus $2.3 \pm 1.6$ events expected. In addition we search in subsamples of these events for electrons, muons, and tau-leptons, additional photons, jets and $b$-quark jets. We conclude that the data are consistent with standard model expectations.

We present limits on three current models of supersymmetry. The first is indirect production of chargino-neutralino pairs through squark and gluino production, where the photon is produced in $\tilde{\chi}^0_2 \rightarrow \gamma \tilde{\chi}^0_1$ and the $b$-quark comes from the chargino decay into the light stop squark $\tilde{t}_1 \rightarrow \tilde{t} b$. A choice of favorable values of the parameters allows setting a lower mass limit on the gluino mass of 250 GeV. The second model is similar, but we look only at direct production of the $\tilde{\chi}^0_1 \tilde{\chi}^0_2$ pair. A cross section limit of $\sim 7-10$ pb is set, but is above the predictions for all $\tilde{\chi}^0_2$ masses so that no mass limit can be set. Lastly, a GMSB model is considered in which the photon comes from the decay $\tilde{\chi}^0_1 \rightarrow \gamma \tilde{G}$. Limits in the range 0.3–1.0 pb are set versus the mass of the $\tilde{\chi}^0_1$, but again no mass limit can be set as the cross section predictions are lower than the limit.

Finally, we present a model-independent limit of 0.077 pb on the production of events containing the signature $\gamma b E_t$, and we propose new methods for applying model-independent limits to models that predict similar broad signatures. We conclude that an experienced model builder can evaluate whether model-independent limits apply to a particular model with an uncertainty of approximately 30%.

### ACKNOWLEDGMENTS

We thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Science, Sports and Culture of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation; the A. P. Sloan Foundation; the Bundesministerium fuer Bildung und Forschung, Germany; the Korea Science and Engineering Foundation (KoSEF); the Korea Research Foundation; and the Comision Interministerial de Ciencia y Tecnologia, Spain.

### APPENDIX: APPLICATION OF MODEL-INDEPENDENT LIMITS

In the body of this paper, we present the limits on specific models of new physics that predict the $\gamma b E_t$ signature, then rigorously calculate $A e$ for that model by using a Monte Carlo program with a full detector simulation. We present our limits on $(\sigma \times BR)^{lim} = N^{lim} \mathcal{L} A e$, or a parameter of the model such as the mass of a supersymmetric particle.

A new paradigm, the signature-based or, equivalently, model-independent search may be an effective method for reporting the results of searches in the future. In this case, a signature, such as the photon and $b$-quark jet addressed in this paper, is the focus of the search rather than the predictions of a particular model.

There are several advantages to this approach [1,3,4].

(1) The results are not dated by our current theoretical understanding.

(2) No a priori judgment is necessary to determine what is an interesting model.

(3) The results more closely represent the experimental observations and results will be presented in a form that can be applied to a broad range of models including those not yet imagined.

(4) The number of signatures is more reasonably limited than the number of models and model parameters.

(5) Concentrating on a particular model can tend to focus the search very narrowly, ignoring variations on the signature which may be just as likely to yield a discovery.

(6) Time spent on studying models can be diverted to systematically searching additional signatures.

In order to reflect the data results more generally, in the body of this paper we also present a limit on $(\sigma \times BR \times A e)^{lim} = N^{lim} \mathcal{L}$ for the signatures with no calculation of $A e$. With limits presented this way, the collaboration itself, model builders and other interested workers are no longer given limits on the physics models directly but now must derive the limits themselves. This has the potential for a wider application of the limits. In a practical sense, it means the interested workers must calculate $A e$ for the model under study.

In this appendix we present three methods to calculate $A e$. These results, together with the model-independent limits, can be used to set limits on most models that predict events with the $\gamma b E_t$ signature.

The three methods are referred to as “object efficiencies,” the “standard model calibration process,” and the “public Monte Carlo Simulation.” In the sections below we describe each in turn. In the following sections, we test these methods by comparing the results of each $A e$ calculation to the rigorously derived $A e$ for the specific supersymmetry models.
1. Object efficiencies

The first method for deriving $A \varepsilon$ to use in conjunction with the model-independent limits is object efficiencies. The person investigating a model would run a Monte Carlo generator and place the acceptance cuts on the output which will determine the acceptance, $A$. The next step would be to apply efficiencies (simple scale factors) for the identification of each object in the signature, such as the photon or the $b$-quark tag. This has the advantage of being very straightforward and the disadvantage that correlations between the objects in the event are not accounted for. For example, a model with many jets would tend to have a lower efficiency for the photon isolation requirement than a model with few jets and this effect would not be reflected in this estimate of the efficiency.

Using a sample of $Z \rightarrow e^+ e^-$ events to measure the efficiencies of the global event cuts, we find the $z<60$ cm cut is 92% efficient. The probability of finding no energy out-of-time is 98%. In this case the total global efficiency would be the product of these two efficiencies. In the discussion below, the efficiency of the identification of each object is often listed as efficiencies of several separate steps which should be multiplied to find the total efficiency.

We can also use $Z \rightarrow e^+ e^-$ events to measure the efficiency of the photon identification cuts. One electron from the $Z$ is required to fire the trigger, but the second electron is unbiased with respect to the trigger. In addition the $Z$ peak indicates the number of true physics events, ideal for measuring efficiencies. Which $Z$ electron is required to pass which set of cuts (trigger or offline) must be effectively randomized to avoid correlations between the two sets of cuts. Requiring the cluster to be far from the boundary of the active area in the calorimeters is 73% efficient [31]. The trigger is 91% efficient, the identification cuts are 86% and the isolation requirement is 77% efficient.

For the $b$-quark efficiency we use a 70% probability that the jets from the event are contained in the SVX. (This would be 64% if the global event vertex was not already required to have $z<60$ cm.) We add a 90% probability that the jet was taggable (containing two reconstructed tracks in the SVX, passing $p_t$ cuts) and apply the published [32] tagging probability as a function of the jet $E_t$ which can be summarized as

\begin{align*}
0 & \quad \text{for } E_t<18 \text{ GeV} \\
0.35 + 0.00277E_t & \quad \text{for } 18<E_t<72 \text{ GeV} \\
0.6 & \quad \text{for } E_t>72 \text{ GeV}.
\end{align*}

The missing $E_t$ is found as the vector sum of the noninteracting particles in the event. As long as the missing $E_t$ is large, the resolution on the $E_t$ should not greatly effect the efficiency.

In Sec. IV C we searched the events in the $yb$ sample for additional leptons; here we present approximate object efficiencies for those cuts. These requirements and their efficiencies are borrowed from top-quark analyses [11,12] as a representative selection for high-$E_t$ leptons. The efficiencies quoted here are measured in those contexts and therefore they are approximations in a search for new physics. In particular, the isolation efficiency is likely to be dependent on the production model. For example, if a model of new physics contained no jets, then the isolation efficiency is likely to be greater than that measured in top-quark events which contain several jets on average.

For the electron search we require $E_t>25$ GeV and $|\eta|<1.0$. Given that an electron, as reported in the output of the Monte Carlo generator, passes these acceptance cuts, the probability that the electron strikes the calorimeter well away from any uninstrumented region is 87%. The probability to pass isolation cuts is 80%, and to pass isolation cuts is approximately 87% [31].

For muons we require $p_t>25$ GeV and $|\eta|<1.0$. Given that the muon, as reported in the output of the Monte Carlo generator, passes these cuts, the fiducial acceptance of the muon detectors is 48%. Once the muon is accepted, the probability to pass isolation cuts is 91%, and to pass isolation cuts is approximately 81%.

Tau leptons are identified only in their one- and three-prong hadronic decays which have a branching ratio of 65%. (Tau semileptonic decays can contribute to the electron and muon searches.) We require that the calorimeter cluster has $E_t>25$ GeV and $|\eta|<1.2$ and the object is not consistent with an electron or muon. Given that the $\tau$ decays to a one- or three-prong hadronic decay mode and passes the $E_t$ and $\eta$ requirements, the probability that the tau passes identification and isolation cuts is approximately 57%.

In Sec. IX D we apply these object efficiencies to the supersymmetry models and compare the results of the rigorously derived efficiency to test the accuracy of the results.

2. Standard model calibration process

The second method for determining $A \varepsilon$ for a model is the standard model process or efficiency model. In this method we select a simple physics model that produces the signature. The model is purely for the purpose of transmitting information about $A \varepsilon$ so it does not have any connection to a model of new physics. Since it may be considered a calibration model, it does not have to be tuned and will not become dated. The interested model builder runs a Monte Carlo simulation of the new physics and places acceptance cuts on the output, determining $A$, the same as the first step in the object efficiencies method. This result is then multiplied by the value of $\varepsilon$ which is taken to be the same as the value of $\varepsilon$ which we report here for the standard model process.

We have adopted $WW$ production as our efficiency model. One $W$ is required to decay to $e^\mu$ and we replace the electron with a photon before the detector simulation. The second $W$ is forced to decay to $bu$, so the combination yields the signature $ybE_t$. Since some efficiencies may be dependent on the $E_t$ of the objects in the event, we will vary the “$W$” mass to present this effect. A model builder would then choose the efficiency that most closely matches the mass scale of the new physics models.

The $A \varepsilon$ for this model is found using the same methods as used for the models of supersymmetry. From the difference
3. A public Monte Carlo program

A Monte Carlo event generator followed by a detector simulation is the usual method for determining the efficiency of a model of new physics. However, there is usually considerable detailed knowledge required to run the simulation programs correctly so it is not practical to allow any interested person access to it. But if the simulation is greatly simplified while still approximating the full program, it could become usable for any worker in the field. The model-builder then only has to run this simple Monte Carlo program to determine $A\epsilon$.

An example of this kind of detector simulation, called SHW, was developed for the Fermilab Run II SUSY/Higgs Workshop [33]. Generated particles are traced to a calorimeter and energy deposited according to a simple fractional acceptance and Gaussian resolution. A list of tracks is also created according to a simple efficiency and resolution model, and similarly for muon identification. The calorimeter energy is clustered to find jets. Electromagnetic clusters, together with requirements on isolation and tracking, form electron and photon objects. The tagging of $b$-quarks is done with a simple, parametrized efficiency. At points where object identification efficiencies would occur, such as a $X^2$ cut on an electron shower profile, the appropriate number of candidates are rejected to create the inefficiency. The result is a simple list of objects that are reconstructed for each event. This method of determining efficiencies addresses the largest concern not addressed in the previous methods—the correlation of the characteristics of jets in the model with isolation requirements. We note that a highly parametrized Monte Carlo program has obvious limitations.

We have used the SHW program to compute efficiencies for the three models considered above. Since the program is tuned to provide the approximate efficiency of the Run II detector, we made a few minor changes to reflect the Run I detector. In particular, we changed the photon fiducial efficiency from 85% to 73% and the offline efficiency from 85% to 60%. We reduced the SVX acceptance along the $z$ axis from 60 cm to 31 cm. Finally, we removed soft lepton $b$-tagging and added a 90% efficiency for the global event cuts.

In the next section we use the public Monte Carlo program to calculate $A\epsilon$ for the supersymmetry models and compare the results to the rigorously derived efficiency to test the accuracy of the public Monte Carlo program.

4. Tests of the model-independent efficiency methods

In the body of this paper we have provided rigorous limits on several variations of three supersymmetry physics models that produce the signature of $y\beta E_t$. In this section we apply the model-independent efficiency methods to the supersymmetry models. We can then compare the results with the rigorous limits to evaluate how effective it is to apply the model-independent limits to real physics models.

In most cases we need to distinguish between acceptance and efficiency. Acceptance, indicated by $A$, we define as the probability for generated Monte Carlo objects to pass all geometric and $E_t$ cuts. For the $y\beta E_t$ signature, with $E_t$ defined as the vector sum of neutrinos and lightest supersymmetric particle (LSP’s), the cuts defining the acceptance of the signature are listed in Table XVIII.

Table XIX and Fig. 12 list the results. The columns marked $R$ are the efficiency times acceptance done rigorously, divided by the same found using each of the model-independent methods. The difference of this ratio from 1.0 one is a measure of the accuracy of the approximate methods compared to the rigorous method.

5. Conclusions from tests

There are several notable effects apparent immediately from Table XIX and Fig. 12. The first is that the comparison of efficiencies for one model point fares especially poorly. This occurs when the branching ratio for the model is very small (2%). When the events do not contain many real photons and $b$ quarks, the small number of objects misidentified as photons and $b$ quarks becomes important. For example, jets may pass photon cuts and $c$ quarks may be $b$ tagged. When this occurs, the full simulation will be more efficient than a method which specifically requires that the Monte Carlo generate an isolated photon or $b$ quark in order to accept the event. This is true of the object efficiencies
TABLE XVIII. The list of requirements on the output of a Monte Carlo generator which define the acceptance of a signature, $A$. The requirements on the photon and $b$-quark jet above the double line are common to all signatures in this paper. When missing $E_t$ is required, as in all the supersymmetry searches and the tests of model-independent methods, both $E_t$>40 GeV and $\Delta \phi (\gamma - E_t)$ <168° are required. The $E_t$ requirement is removed and other requirements are added to make specific subsamples.

| $\gamma$   | $E_t$>25 GeV | $|\eta|<1.0$ |
|------------|------------|-------------|
| $b$ quark  | $E_t$>30 GeV | $|\eta|<2.0$ |

Additional signatures

<table>
<thead>
<tr>
<th>$\Sigma\rho_{\nu,LSP}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_t$&gt;40 GeV, $\Delta \phi (\gamma - E_t)$&lt;168°</td>
</tr>
<tr>
<td>$e$</td>
</tr>
<tr>
<td>$\mu$</td>
</tr>
<tr>
<td>$\tau$</td>
</tr>
<tr>
<td>second $\gamma$</td>
</tr>
<tr>
<td>Jets</td>
</tr>
</tbody>
</table>

In the object efficiency method, the acceptance of the signature is computed by running the Monte Carlo simulation without a detector simulation. As each object in the signature is identified and passes acceptance cuts, the individual object efficiencies which may or may not be $\bar{E}_t$ or $\eta$ dependent, are listed in Sec. IX A. In this test, these efficiencies are typically well matched to the rigorously derived efficiencies. The average of $R_{\eta b j}$ over all models except the first is 0.88±0.21, where 0.21 is the rms computed with respect to 1.0, the ideal result.

In the efficiency model method, we generate a Monte Carlo model that is not related to a search for new physics but produces the signature of interest. For the signature of $yb\bar{E}_t$, we generated $WW\rightarrow (\gamma \nu)(b\bar{u})$. The efficiency model results are also optimistic, the average is a ratio of 0.74±0.35 where again the uncertainty is actually the rms with 1.0, the ideal result. We found that the difficulty of applying this method was in choosing the mass scale. For example, we chose to match the “$W$” mass to the $\tilde{\chi}_2^0$ mass in the direct production of the $\tilde{\chi}_2^0\rightarrow \gamma \tilde{\chi}_1^0$ model. However, the photon comes from a secondary decay and the effect of the LSP mass compared to the massless neutrino causes the $E_t$ of the

TABLE XIX. The results of comparing the methods of calculating $A \epsilon$ using the model-independent methods and the rigorously derived $A \epsilon$. Each row is a variation of a model of supersymmetry as indicated by the label in the first column and the mass of a supersymmetric particle listed in column two (GeV). The column labeled $A$ is the acceptance of the model in % and the next column is the rigorously derived $A \epsilon$. The columns labeled with $R$ are the ratios of the rigorously derived $A \epsilon$ to $A \epsilon$ found using the model-independent method indicated.

<table>
<thead>
<tr>
<th>Model</th>
<th>$M_\chi$</th>
<th>BR (%)</th>
<th>$A$</th>
<th>$A \cdot \epsilon$</th>
<th>$R_{\eta bj}$</th>
<th>$R_{WW}$</th>
<th>$R_{SHW}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>GMSB</td>
<td>130</td>
<td>3</td>
<td>65.0</td>
<td>27.50</td>
<td>2.79</td>
<td>3.03</td>
<td>1.07</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_1^0}$</td>
<td>147</td>
<td>20</td>
<td>49.8</td>
<td>7.45</td>
<td>0.91</td>
<td>1.00</td>
<td>0.70</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_1^+}$</td>
<td>170</td>
<td>23</td>
<td>51.7</td>
<td>8.35</td>
<td>0.97</td>
<td>1.00</td>
<td>0.87</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^0}$</td>
<td>186</td>
<td>18</td>
<td>54.7</td>
<td>11.44</td>
<td>1.26</td>
<td>1.22</td>
<td>1.11</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^-}$</td>
<td>185</td>
<td>30</td>
<td>17.0</td>
<td>1.97</td>
<td>0.91</td>
<td>0.68</td>
<td>0.48</td>
</tr>
<tr>
<td>$\tilde{\chi}_2^0\rightarrow \gamma \tilde{\chi}_1^0$</td>
<td>210</td>
<td>30</td>
<td>22.0</td>
<td>2.98</td>
<td>1.04</td>
<td>0.73</td>
<td>0.90</td>
</tr>
<tr>
<td>$\tilde{\chi}_2^-\rightarrow \tilde{\chi}_1^-\tilde{\nu}_L$ production</td>
<td>235</td>
<td>30</td>
<td>24.0</td>
<td>3.23</td>
<td>1.01</td>
<td>1.01</td>
<td>0.90</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^-}$</td>
<td>260</td>
<td>30</td>
<td>24.5</td>
<td>2.69</td>
<td>0.82</td>
<td>0.52</td>
<td>0.75</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^0}$</td>
<td>285</td>
<td>30</td>
<td>19.7</td>
<td>2.16</td>
<td>0.84</td>
<td>0.48</td>
<td>0.72</td>
</tr>
<tr>
<td>$\tilde{\chi}_2^0\rightarrow \gamma \tilde{\chi}_1^0$</td>
<td>110</td>
<td>100</td>
<td>13.5</td>
<td>0.93</td>
<td>0.54</td>
<td>0.54</td>
<td>0.59</td>
</tr>
<tr>
<td>$\tilde{\chi}_2^-\rightarrow \tilde{\chi}_1^-\tilde{\nu}_L$ production</td>
<td>130</td>
<td>100</td>
<td>12.6</td>
<td>1.41</td>
<td>0.88</td>
<td>0.80</td>
<td>0.87</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^-}$</td>
<td>140</td>
<td>100</td>
<td>14.8</td>
<td>1.29</td>
<td>0.68</td>
<td>0.60</td>
<td>0.66</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^0}$</td>
<td>150</td>
<td>100</td>
<td>13.7</td>
<td>1.34</td>
<td>0.77</td>
<td>0.65</td>
<td>0.78</td>
</tr>
<tr>
<td>$M_1=M_{\tilde{\chi}_2^-}$</td>
<td>170</td>
<td>100</td>
<td>11.5</td>
<td>1.27</td>
<td>0.85</td>
<td>0.68</td>
<td>0.65</td>
</tr>
</tbody>
</table>

FIG. 12. The ratio of the efficiencies obtained with the full detector simulation to those obtained with the model-independent methods. The x axis is the row number from Table XIX.
\( \gamma \) and \( b \) to be poorly matched to the \( E_t \) of these objects in the WW model.

In the public Monte Carlo method, we compute the efficiency using SHW, a highly parametrized, self-contained Monte Carlo program. In general, results here are somewhat optimistic with the average ratio to the rigorous total efficiency being 0.77 ± 0.28, where the uncertainty is the rms computed with respect to 1.0, the ideal result.

For completeness we also include the ratio of the simple acceptance to the rigorous acceptance times efficiency. The average ratio is 0.12 ± 0.87.

The methods for calculating efficiency without access to the full detector simulation are accurate to approximately 30% overall. They tend to underestimate \( A_e \) by 10–25% but the result for individual comparisons varies greatly. These uncertainties are larger than, but not greatly larger than, a typical uncertainty in a rigorously derived efficiency, which is 20%.

We conclude that in order to determine if a model is easily excluded or far from being excluded by the data, the model-independent methods are sufficient. If the model is within 30% of exclusion, no conclusion can be drawn and the efficiency should be rigorously derived.

[8] The CDF coordinate system is right-handed, and has the \( z \) axis aligned with the proton beam and \( y \) vertical. The azimuthal angle is denoted as \( \phi \) and the polar angle as \( \theta \); \( \eta \) is \( -\ln(\tan(\theta/2)) \).
[17] In this paper when two uncertainties are reported, the first is statistical and the second is systematic.
[18] ZEUS Collaboration, J. Breitweg et al., Z. Phys. C 74, 207 (1997); A similar method was developed in H1 Collaboration, C. Adloff et al., ibid. 74, 191 (1997).