2015

Electronic structures and electronic spectra of all-boron fullerene $B_{40}$

Rongxing He  
*Southwest University, Chongqing, herx@swu.edu.cn*

Xiao Cheng Zeng  
*University of Nebraska-Lincoln, xzeng1@unl.edu*

Follow this and additional works at: http://digitalcommons.unl.edu/chemzeng

Part of the Analytical Chemistry Commons, Materials Chemistry Commons, and the Physical Chemistry Commons

http://digitalcommons.unl.edu/chemzeng/138

This Article is brought to you for free and open access by the Published Research - Department of Chemistry at DigitalCommons@University of Nebraska - Lincoln. It has been accepted for inclusion in Xiao Cheng Zeng Publications by an authorized administrator of DigitalCommons@University of Nebraska - Lincoln.
This study is motivated by the recent discovery of the first all-boron fullerene analogue, a B_{40} cluster with D_{2d} point-group symmetry, dubbed borospherene (Nat. Chem., 2014, 6, 727). Insight into the electronic structures and spectral properties of B_{40} is timely and important to understand the borospherene and the transition from open-ended plate or ribbon-like structures to a hollow-cage structure at B_{40}. Optimized geometries of borospherene B_{40} for both the ground state and the first excited state allow us to compute spectral properties including UV-vis absorption, infrared (IR) and Raman spectra. Highly resolved absorption and emission spectra are obtained, for the first time, for the fullerene at the time-dependent density-functional theory (TD-DFT) level within the Franck–Condon approximation and including the Herzberg–Teller effect. Assigned vibrational modes in absorption and emission spectra are readily compared with future spectroscopy measurements to distinguish the hollow-cage structure of D_{2d}-B_{40} from other quasi-planar boron structures.

Since the discovery of the buckminsterfullerene C_{60}, carbon-fullerene-like elemental hollow-cage structures have been highly sought after, particularly for nonmetal elements next to carbon in the periodic table. To date, it has been established that silicon, a nearest-neighbor of C in the periodic table, cannot form carbon fullerene-like structures, but can exhibit endohedral-like fullerene structures with an uneven surface beyond the size of 30-atom clusters. Boron, another nearest-neighbor of C in the periodic table, was initially predicted to form a fullerene-like structure at the cluster size B_{80}. But later computational studies showed that the B_{80} fullerene is a high-energy isomer. Previous experimental and theoretical studies also indicated that the all-boron fullerene analogue cannot be formed for small to medium-sized boron clusters up to the cluster size of 36. Very recently, a fascinating all-boron fullerene structure, B_{40} hollow-cage (Fig. 1a), was uncovered through a joint experimental/theoretical study. Unlike the C_{60} fullerene which is composed of pentagons and hexagons and has the I_{h} group symmetry, the box-like B_{40} fullerene is composed of hexagons and heptagons and has the D_{2d} group symmetry. As such, the

Fig. 1 Borospherene B_{40} structure (a), and the computed optical spectra: (b) vertical absorption, (c) IR, and (d) Raman.
electronic structures and spectral features of $B_{40}$ are expected to be very different from those of $C_{60}$. In light of the fact that this $D_{2d}$-$B_{40}$ structure has not been directly imaged or observed in the laboratory, it is important to compute electronic and spectral properties of the $B_{40}$ fullerene or borospherene for comparison with future spectroscopy measurements. In this communication, we present the first highly-resolved $S_0 \leftrightarrow S_1$ optical absorption and fluorescence spectra of $B_{40}$, on the basis of the Frank–Condon (FC) approximation including the Herzberg–Teller (HT) effect (intensity borrowing).\textsuperscript{b} Computed IR and Raman spectra are also presented. Although it is still a challenge to precisely simulate highly resolved electronic spectra because of the difficulty to optimize excited states, the present method has proven to be reliable as it has been benchmark tested in our previous studies.\textsuperscript{9,10}

According to the character table of the $D_{2d}$ point-group, the irreducible representations for the 114 vibrational normal modes of $B_{40}$ are given as: $T_{1g} = 16a_1 + 13a_2 + 14b_1 + 15b_2 + 28e$. The corresponding vibrational frequencies are predicted using the PBE0 and BHandLYP functionals with 6-311G* and 6-31G* basis sets, and the results are given in Table S1 in the ESI.\textsuperscript{†} The recorded vertical absorption (UV-vis) spectrum (Fig. 1b) indicates that the strong dipole allowed transitions should take place in the region below 400 nm wavelength. The lowest singlet excited state ($S_1$), having $B_2$ symmetry, is a weakly allowed absorption at $\sim 532$ nm with very small oscillator strength (denoted by an oval in Fig. 1b). The highest occupied molecular orbital (HOMO, $\pi$ orbital) and the lowest unoccupied molecular orbital (LUMO, $\pi^*$ orbital) of the ground state, computed based on the PBE0/6-31G* level, are shown in ESI,\textsuperscript{†} Fig. S1. The computed results indicate that the excitation from $S_0(\Gamma_{A_1})$ to $S_1(\Gamma_{B_2})$ is the HOMO $\rightarrow$ LUMO transition with a vertical transition energy of 2.32 eV (see Table 1). Hence, the $S_1$ state has the characteristics of $\pi \rightarrow \pi^*$ transition. Note that in ref. 5, the computed ground-state adiabatic detachment energy of the $B_{40}^{-}$ anion is 2.39 eV, which is in good agreement with the present HOMO–LUMO excitation of 2.32 eV.

Compared with the $I_4/C_{mm}$ fullerene for which only 14 normal modes are IR ($4t_{1u}$) or Raman ($2a_g + 8h_g$) active,\textsuperscript{11} the number of IR or Raman active modes of the borospherene $B_{40}$ is significantly larger. Indeed, as shown in Fig. 1c and d, the computed IR and Raman spectra of $B_{40}$ display numerous active absorption peaks. Detailed IR and Raman peak positions, intensities and assignments are given in ESI,\textsuperscript{†} Table S2. The $D_{2d}$-$B_{40}$ encompasses 43 IR ($15b_2 + 28e$) and 73 Raman ($16a_1 + 14b_1 + 15b_2 + 28e$) active modes. However, intensities of most IR and Raman active modes are very weak. Especially for the IR spectrum, only modes $v_{22}$ (382 cm$^{-1}$), $v_{104}$ (1259 cm$^{-1}$), $v_{107}$ (1271 cm$^{-1}$) and $v_{108}$ (1281 cm$^{-1}$) exhibit strong vibration. Note that $v_{22}$, $v_{104}$ and $v_{108}$ are two-fold degenerate normal modes with $e$ symmetry, both being the main IR active modes according to our computation. Likewise, the modes with $a_1$ symmetry contribute mainly to the Raman spectrum. Also note that in the study of carbon nanotubes, the so-called “radial breathing mode” (RBM) is used to identify the hollow structures.\textsuperscript{12} Here we report that the RMB frequency of $B_{40}$ with a hollow structure is about 171 cm$^{-1}$ (at PBE0/6-311G* level).

Next, we present the electronic spectra of borospherene $B_{40}$. The FC approximation is most satisfactory for the description of vibronic transition with large oscillator strength, giving rise to the so-called FC spectrum. For weak and forbidden transitions, the HT effect is important to give full and rich vibrational structures.\textsuperscript{10} Thus, using the method published previously,\textsuperscript{9,10} we obtain highly resolved electronic absorption and emission spectra of $B_{40}$ including the HT effect. We have assigned most of the involved vibrational normal modes (the results are displayed in Fig. 2, ESI,\textsuperscript{†} Fig. S2 and Table S3). Note that the band origin is set at 15 808 cm$^{-1}$ (1.96 eV), which is the computed adiabatic energy gap between $S_0$ and $S_1$ (Table 1). The assignment is expected to offer a guideline for future $B_{40}$ isomeric structure identification. The simulated spectra which include both FC and HT contributions are denoted as FCHT. To investigate the HT effect separately, the spectra involving only the HT contribution are also plotted (see ESI,\textsuperscript{†} Fig. S2b and e).

The harmonic approximation is used to simulate the FC spectrum because the difference between vibrational frequencies

Table 1 Computed vertical transition energy ($\Delta E$), adiabatic energy ($E^{(0)}$) and oscillator strengths ($f$) of the first five excited states of borospherene $B_{40}$ [at the PBE0/6-311+G* level]

<table>
<thead>
<tr>
<th>State</th>
<th>Configuration</th>
<th>$\Delta E$ a</th>
<th>$E^{(0)}$ a</th>
<th>$f$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1^{1}B_2$</td>
<td>HOMO $\rightarrow$ LUMO (70%)</td>
<td>2.32</td>
<td>0.006</td>
<td>1.96 b</td>
</tr>
<tr>
<td>$1^{1}B_1$</td>
<td>HOMO $- 1 \rightarrow$ LUMO (70%)</td>
<td>2.34</td>
<td>0.000</td>
<td></td>
</tr>
<tr>
<td>$1^{1}E$</td>
<td>HOMO $- 3 \rightarrow$ LUMO (69%)</td>
<td>2.40</td>
<td>0.001</td>
<td></td>
</tr>
<tr>
<td>HOMO $\rightarrow$ LUMO $+ 1$ (13%)</td>
<td>2.40</td>
<td>0.001</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$2^{1}E$</td>
<td>HOMO $- 2 \rightarrow$ LUMO (69%)</td>
<td>2.40</td>
<td>0.002</td>
<td></td>
</tr>
<tr>
<td>HOMO $- 1 \rightarrow$ LUMO $+ 2$ (13%)</td>
<td>2.51</td>
<td>0.000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$1^{1}A_2$</td>
<td>HOMO $- 4 \rightarrow$ LUMO (69%)</td>
<td>2.51</td>
<td>0.000</td>
<td></td>
</tr>
</tbody>
</table>

a Unit is in eV. b The PBE0/6-311G* level is used.

Fig. 2 Simulated well-resolved absorption (a) and emission (b) spectra of borospherene $B_{40}$ within a range of 2000 cm$^{-1}$ (the 0–0 line is set to zero).
of \( S_0 \) and \( S_1 \) states is small for every totally symmetric \( (a_1 \) under \( D_{2d} \) point group) normal mode (the largest difference is about 20 cm\(^{-1}\)) in the present situation, see ESI,† Table S4). The vertical transition results show that the \( S_1 \) \( \leftarrow S_0 \) absorption spectrum of \( B_{40} \) is very weak in the visible region with an oscillator strength of 0.006 (Table 1). ESI,† Fig. S2a shows that the FC spectral profile is dominated by the 0–0 transition. This suggests that only small displacement of the position of the minimum on the potential energy surface between ground- and excited-states is generated,9 which is confirmed by the small Huang–Rhys factors of totally symmetric normal modes (see ESI,† Table S5). Our computation also suggests that the FC spectral profile of borospherene \( B_{40} \) is primarily described by the FC progression in terms of nine totally symmetric normal modes and their combination. The computed frequencies of these nine modes \( (\nu_2, \nu_{22}, \nu_{33}, \nu_{37}, \nu_{45}, \nu_{49}, \nu_{63}, \nu_{102} \) and \( \nu_{114} \) ) are 172, 339, 432, 443, 455, 518, 660, 1181 and 1316 cm\(^{-1}\), respectively (note that in the simulated absorption spectrum, frequencies of the \( S_0 \) state are used, while in the emission spectrum frequencies of \( S_0 \) are adopted).

Among the FC active modes, \( \nu_2, \nu_{22}, \nu_{37}, \nu_{45}, \nu_{49} \) and \( \nu_{102} \) are the longest progression-forming modes, and modes \( \nu_{49}, \nu_{63} \) and \( \nu_{114} \) have little contribution to the FC absorption spectrum. The relative intensities of some combined peaks, such as \( 49^{1}22^{1} \), \( 102^{1}22^{1} \) and \( 63^{1}49^{1} \), are significant and cannot be ignored. It is interesting to note that in the FC absorption spectrum, the most intense vibrational band is from mode \( \nu_{49} \), and its relative intensity \((25.62)\) is about one-fourth of the 0–0 transition (see ESI,† Table S3). This will be compared with the FCHT absorption spectrum.

Fig. 2a displays the simulated FCHT spectral profile of \( B_{40} \), where the tentative assignments of major vibrational transitions are presented (detailed assignments are given in ESI,† Fig. S3). The strong impact of HT contribution to the spectrum could be easily seen by comparing the profiles of the FC and FCHT spectra (see ESI,† Fig. S2a–c). Compared with the FC absorption spectrum, a large number of vibrational lines with strong intensity appear in the FCHT spectrum, labeled in red. Within the region of 0–1500 cm\(^{-1}\) (the origin of 0–0 line is set as 0), one dominant congestion is shaped along twelve fundamental modes \( 2^{1}, 12^{2} (261 \text{ cm}^{-1}), 22^{1}, 27^{1} (393 \text{ cm}^{-1}), 31^{1} (398 \text{ cm}^{-1}), 38^{1}, 49^{1}, 60^{1} (656 \text{ cm}^{-1}), 99^{1} (1148 \text{ cm}^{-1}), 102^{1}, 111^{1} (1283 \text{ cm}^{-1}) \) and \( 114^{1} \) (their relative intensities are listed in ESI,† Table S3). Among these modes, six non-totally symmetric normal modes, \( \nu_{12}, \nu_{27}, \nu_{31}, \nu_{60}, \nu_{99} \) and \( \nu_{111} \), make great contribution to the FCHT spectrum (see ESI,† Fig. S2b).

Especially, modes \( \nu_{27} \) and \( \nu_{60} \) become the most intense peaks in the FCHT spectrum, which is completely different from the FC spectrum. In addition, the HT active modes also significantly change the spectral profile in the high frequency region by the combined bands, such as \( 114^{1}12^{2} \) \((\nu_{114} + \nu_{12} = 1577 \text{ cm}^{-1})\), \( 102^{1}60^{1} \) \((\nu_{102} + \nu_{60} = 1837 \text{ cm}^{-1}) \), etc.

The simulated \( S_1 \) \( \rightarrow \) \( S_0 \) emission spectra of borospherene \( B_{40} \) and the assignment are displayed in Fig. 2b (for convenience, the FC and HT spectra are given in ESI,‡ Fig. S2). Similar to the FC absorption, the 0–0 transition of the FC emission spectrum is also found to carry most of the FC intensity. Four active FC totally symmetric normal modes, \( \nu_1 \) \((171 \text{ cm}^{-1})\), \( \nu_{17} \) \((354 \text{ cm}^{-1})\), \( \nu_{49} \) \((524 \text{ cm}^{-1}) \) and \( \nu_{99} \) \((1200 \text{ cm}^{-1}) \), have the largest Huang–Rhys factors (see ESI,‡ Table S5), indicating that they are the primary progression forming modes. From ESI,‡ Fig. S2c, one can see that the HT contribution also has a large effect on the emission spectral profile. In the FCHT emission spectrum, a primary difference is seen in the range of 1250–1300 cm\(^{-1}\) where the superposition of three non-totally symmetric normal modes, \( \nu_{104}, \nu_{107} \) and \( \nu_{109} \) leads to a strong transition with relative intensity comparable to that of mode \( \nu_{49} \). Briefly, the basic feature of the FCHT emission spectrum of \( B_{40} \) is described by the bands at 171, 354, 382, 429, 437, 524, 654, 1200, 1271 and 1281 cm\(^{-1}\), which are tentatively assigned as modes \( \nu_1, \nu_{17}, \nu_{22}, \nu_{31}, \nu_{35}, \nu_{49}, \nu_{60}, \nu_{99}, \nu_{107} \) and \( \nu_{109} \). Moreover, one can find that the mirror symmetry between the FC absorption and emission spectra is almost retained, whereas mirror symmetry breakdown (MSB) can be observed between the FCHT absorption and emission spectra. Based on the above analyses, we therefore attribute the MSB to the HT effect.

In summary, we have investigated electronic and spectral properties of the hollow-cage structure \( B_{40} \). The computed vertical absorption spectrum suggests that the \( S_0(1A_1) \) \( \rightarrow S_1(1B_2) \) is a weakly allowed absorption with the \( \pi\pi^* \) feature. The computed IR and Raman spectra suggest that there are 43 IR \((15b_2 + 28e)\) and 73 Raman \((16a_1 + 14b_1 + 15b_2 + 28e)\) active modes, but only a few of them have strong absorption. More importantly, the well-resolved \( S_0(1A_1) \) \( \leftrightarrow S_1(1B_2) \) absorption and emission spectra of \( B_{40} \) are simulated, where the vibrational assignments are made tentatively. The HT effect has great influence on the simulated electronic spectra, which produces a richer vibrational structure and leads to the mirror symmetry breakdown between the absorption and emission spectra. The present results can be used, when compared with future spectroscopy measurements, to distinguish the hollow-cage structure of \( D_{2d}B_{40} \) from other quasi-planar structures (as shown in ESI,† Table S6 and Fig. S4), one can see that the IR and Raman spectra of the plate-like isomer \( B_{40} \) are markedly different from those of the hollow-cage \( B_{40} \) isomer.\(^{40,5,13}\) The obtained optical spectra will be helpful not only for identifying the borospherene \( B_{40} \) among its quasi-planar isomers, but also for analyzing the electronic transitions in the weakly allowed \( S_1(1A_1) \) \( \leftrightarrow S_2(1B_2) \) absorption and fluorescence spectra. Knowledge on the spectral properties should be useful for understanding the borospherene and the transition from open-ended quasi-planar structures to the hollow-cage structure at \( B_{38} \) and \( B_{40} \).\(^{5,14}\)

RXH acknowledges the financial support from the Natural Science Foundation of China (21173169), the Chongqing Municipal Natural Science Foundation (cstc2013jcyjA90015) and the Fundamental Research Funds for the Central Universities (No. XDJK2013A008). XCZ is supported by NSF through the Nebraska Materials Research Science and Engineering Center (MRSEC) (Grant no. DMR-1420645), and UNL Holland Computing Centre, and a grant from USTC for (1000 Talent Plan) summer research.

Notes and references


