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# Measurement of trilinear gauge boson couplings from $WW + WZ \to l\nu jj$ events in $pp$ collisions at $\sqrt{s}$= 1.96 TeV

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# Measurement of trilinear gauge boson couplings from $WW + WZ \to l\nu jj$ events in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV

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We present a direct measurement of trilinear gauge boson couplings at $\gamma WW$ and $ZWW$ vertices in $WW$ and $WZ$ events produced in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV. We consider events with one electron or muon, missing transverse energy, and at least two jets. The data were collected using the D0 detector and correspond to 1.1 fb$^{-1}$ of integrated luminosity. Considering two different relations between the couplings at the $\gamma WW$ and $ZWW$ vertices, we measure these couplings at 68% C.L. to be $\kappa_\gamma = 1.07^{+0.26}_{-0.29}$, $\lambda = 0.00^{+0.06}_{-0.06}$, and $g_1^Z = 1.04^{+0.09}_{-0.09}$ in a scenario respecting $SU(2)_L \otimes U(1)_Y$ gauge symmetry and $\kappa = 1.04^{+0.11}_{-0.11}$ and $\lambda = 0.00^{+0.06}_{-0.06}$ in an "equal couplings" scenario.

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## I. INTRODUCTION

A primary motivation for studying diboson physics is that the production of two weak bosons and their interactions provide tests of the electroweak sector of the standard model (SM) arising from the vertices involving trilinear gauge boson couplings (TGCs) [1]. Any deviation of TGCs from their predicted SM values would be an indication for

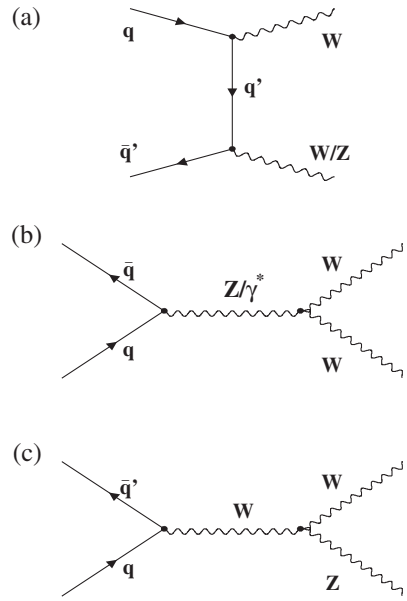


FIG. 1. Tree-level Feynman diagrams for the processes of $WW/WZ$ production at the Tevatron collider via (a) $t$-channel exchange and (b) and (c) $s$-channel.

new physics [2] and could provide information on a mechanism for electroweak symmetry breaking (EWSB).

The TGCs involving the $W$ boson have been previously probed in $WW$, $W\gamma$, and $WZ$ production at the Tevatron $p\bar{p}$ Collider [3–6] and $WW$ production at the CERN $e^+e^-$ collider (LEP) [7–10], at different center-of-mass energies and luminosities but no deviation from the SM predictions has been observed. The LEP experiments benefit from the full reconstruction of event kinematics in $e^+e^-$ collisions, high signal selection efficiencies, and small background contamination. At the Tevatron, despite larger backgrounds and limited ability to fully reconstruct event kinematics, larger collision energies are probed and $WZ$ production can be used to directly probe the $ZWW$ coupling. The study of $WW$ and $WZ$ production at hadron colliders has focused primarily on the purely leptonic final states [3,4,11]. In this paper we present a measurement of the $\gamma WW/ZWW$ couplings based on the same data set used to obtain the recent evidence for semileptonic decays of $WW/WZ$ boson pairs in hadron collisions [12].

As shown in the tree-level diagrams of Fig. 1, TGCs contribute to $WW/WZ$ production via $s$-channel diagrams. Production of $WW$ via the $s$-channel process contains both trilinear $\gamma WW$ and $ZWW$ gauge boson vertices. On the other hand, $WZ$ production is sensitive exclusively to the $ZWW$ vertex.

## II. PHENOMENOLOGY

Unraveling the origins of EWSB and the mass generation mechanism are currently the highest priorities in particle physics. The SM introduces an effective Higgs potential with an upper limit on the Higgs boson mass of $\simeq 1$ TeV to prevent tree-level unitarity violation [13].

In a Higgs-less scenario or for heavier Higgs boson masses this unitarity limit on the Higgs boson mass indicates the mass scale at which the SM must be superseded by new physics in order to restore unitarity at TeV energies. In this case, the SM is considered to be a low-energy approximation of a general theory. Conversely, if a light Higgs boson exists, the SM may nevertheless be incomplete and new physics could appear at higher energies.

The effects of this general theory can be described by an effective Lagrangian, $\mathcal{L}_{\rm eff}$, describing low-energy interactions of the new physics at higher energies in a model-independent manner. Expanding in powers of $(1/\Lambda_{\rm NP})$ [14],

$$\mathcal{L}_{\rm eff} = \mathcal{L}_{\rm eff}^{\rm SM} + \sum_{n\geq 1}\sum_i \frac{f_i}{\Lambda_{\rm NP}^n}\mathcal{O}_i^{(n+4)}, \tag{1}$$

where $\mathcal{L}_{\rm eff}^{\rm SM}$ is the $SU(2)_L \times U(1)_Y$ gauge-invariant SM Lagrangian, $\Lambda_{\rm NP}$ is the energy scale of the new physics, and $i$ sums over all operators $\mathcal{O}_i$ of the given energy dimension $(n+4)$. The coefficients $f_i$ parametrize all possible interactions at low energies. Effects of the new physics may not be directly observable because the scale of the new physics is above the energies currently experimentally accessible. However, there could be indirect consequences with measurable effects; for example, on gauge boson interactions.

For the study of gauge boson interactions, the relevant terms in Eq. (1) are those that produce vertices with three or four gauge bosons. The effective Lagrangian, $\mathcal{L}_{\rm eff}$, that parametrizes the most general Lorentz invariant $VWW$ vertices ($V = Z, \gamma$) involving two $W$ bosons can be defined as [15]

$$\begin{aligned}\frac{\mathcal{L}_{\rm eff}^{VWW}}{g_{VWW}} &= ig_1^V(W_{\mu\nu}^\dagger W^\mu V^\nu - W_\mu^\dagger V_\nu W^{\mu\nu}) \\ &\quad + i\kappa_V W_\mu^\dagger W_\nu V^{\mu\nu} + i\frac{\lambda_V}{M_W^2}W_{\lambda\mu}^\dagger W_\nu^\mu V^{\nu\lambda} \\ &\quad - g_4^V W_\mu^\dagger W_\nu(\partial^\mu V^\nu + \partial^\nu V^\mu) \\ &\quad + g_5^V \epsilon^{\mu\nu\lambda\rho}(W_\mu^*\partial_\lambda W_\nu - \partial_\lambda W_\mu^\dagger W_\nu)V_\rho \\ &\quad + i\tilde{\kappa}_V W_\mu^\dagger W_\nu \tilde{V}^{\mu\nu} + i\frac{\tilde{\lambda}_V}{M_W^2}W_{\lambda\mu}^\dagger W_\nu^\mu \tilde{V}^{\nu\lambda},\end{aligned} \tag{2}$$

where $\epsilon_{\mu\nu\lambda\rho}$ is the fully antisymmetric $\epsilon$ tensor, $W$ denotes the $W$ boson field, $V$ denotes the photon or $Z$ boson field, $V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu$, $W_{\mu\nu} = \partial_\mu W_\nu - \partial_\nu W_\mu$, $\tilde{V}_{\mu\nu} = 1/2(\epsilon_{\mu\nu\lambda\rho}V^{\lambda\rho})$, $g_{\gamma WW} = -e$, and $g_{ZWW} = -e\cot\theta_W$, where $e$ is the electron electric charge, $\theta_W$ is the weak mixing angle, and $M_W$ is the $W$ boson mass. The 14 coupling parameters of $VWW$ vertices are grouped according to the symmetry properties of their corresponding operators: $C$ (charge conjugation) and $P$ (parity) conserv-

ing ($g_1^V$, $\kappa_V$, and $\lambda_V$), $C$ and $P$ violating but $CP$ conserving ($g_5^V$), and $CP$ violating ($g_4^V$, $\tilde{\kappa}_V$, and $\tilde{\lambda}_V$). In the SM all couplings vanish ($g_5^V = g_4^V = \tilde{\kappa}_V = \tilde{\lambda}_V = \lambda_V = 0$) except $g_1^V = \kappa_V = 1$. The value of $g_1^\gamma$ is fixed by electromagnetic gauge invariance ($g_1^\gamma = 1$) while the value of $g_1^Z$ may differ from its SM value. Considering the $C$ and $P$ conserving couplings only, five couplings remain, and their deviations from the SM values are denoted as the anomalous TGCs $\Delta g_1^Z = (g_1^Z - 1)$, $\Delta\kappa_\gamma = (\kappa_\gamma - 1)$, $\Delta\kappa_Z = (\kappa_Z - 1)$, $\lambda_\gamma$ and $\lambda_Z$.

If nonzero anomalous TGCs are introduced in Eq. (2), an unphysical increase in the $WW$ and $WZ$ production cross sections will result as the center-of-mass energy, $\sqrt{\hat{s}}$, of the partonic constituents approaches $\Lambda_{\rm NP}$. Such divergences would violate unitarity, but can be controlled by introducing a form factor for which the anomalous coupling vanishes as $\hat{s} \to \infty$:

$$\Delta a(\hat{s}) = \frac{\Delta a_0}{(1 + \hat{s}/\Lambda_{\rm NP}^2)^n}, \tag{3}$$

where $n = 2$ for $\gamma WW$ and $ZWW$ couplings, and $a_0$ is a low-energy approximation of the coupling $a(\hat{s})$. Thus, the previously described anomalous TGCs scale as $\Delta a_0$ in Eq. (3). The values of $\Delta a_0$ (and $a_0$) are constrained by requiring the $S$-matrix unitarity condition that bounds the $J = 1$ partial-wave amplitude of inelastic vector boson scattering by a constant. These constants were derived by Baur and Zeppenfeld [16] for each coupling that contributes to reduced helicity amplitudes in $WZ$, $\gamma W$, or $WW$ production via $s$ channel. Calculated with $M_W = 80$ GeV, $M_Z = 91.1$ GeV, and with the dipole form factor as given by Eq. (3), the unitarity bounds for $\Delta\kappa_\gamma$, $\Delta\kappa_Z$, $\Delta g_1^Z$, and $\lambda$ TGCs are

$$\begin{aligned}
|\Delta\kappa_\gamma^0| &\le \frac{n^n}{(n-1)^{n-1}} \frac{1.81\ \text{TeV}^2}{\Lambda_{\rm NP}^2}, \\
|\Delta\lambda_\gamma^0| &\le \frac{n^n}{(n-1)^{n-1}} \frac{0.96\ \text{TeV}^2}{\Lambda_{\rm NP}^2} \\
|\Delta\kappa_Z^0| &\le \frac{n^n}{(n-1)^{n-1}} \frac{0.83\ \text{TeV}^2}{\Lambda_{\rm NP}^2}, \\
|\Delta\lambda_Z^0| &\le \frac{n^n}{(n-1)^{n-1}} \frac{0.52\ \text{TeV}^2}{\Lambda_{\rm NP}^2} \\
|\Delta g_1^{Z0}| &\le \frac{n^n}{(n-1)^{n-1}} \frac{0.84\ \text{TeV}^2}{\Lambda_{\rm NP}^2}.
\end{aligned} \tag{4}$$

For $n = 2$ and $\Lambda_{\rm NP} = 2$ TeV, the unitarity condition sets constraints on the TGCs of $|\Delta\kappa_\gamma^0| \le 1.81$, $|\Delta\lambda_\gamma^0| \le 0.96$, $|\Delta\kappa_Z^0| \le 0.83$, $|\Delta\lambda_Z^0| \le 0.52$, and $|\Delta g_1^{Z0}| \le 0.84$. The scale of new physics, $\Lambda_{\rm NP}$, was chosen such that the unitarity limits are close to, but no tighter than, the coupling limits set by data. Clearly, as $\Lambda_{\rm NP}$ increases the effects on anomalous TGCs decrease and their observation requires either more precise measurements or higher $\hat{s}$.

## III. RELATIONS BETWEEN COUPLINGS

The interpretation of the effective Lagrangian [Eq. (1)] depends on the specified symmetry and the particle content of the underlying low-energy theory. In general, $\mathcal{L}_{\rm eff}$ can be expressed using either the linear or nonlinear realization of the $SU(2)_L \times U(1)_Y$ symmetry [17] to prevent unitarity violation, depending on its particle content. Thus, $\mathcal{L}_{\rm eff}$ can be rewritten in a form that includes the operators that describe interactions involving additional gauge bosons, and/or Goldstone bosons, and/or the Higgs field and operators of interest for any new physics effects. The number of operators can be reduced by considering their detectable contribution to the measured coupling.

Assuming the existence of a light Higgs boson, the low-energy spectrum is augmented by the Higgs doublet field $\phi$, and $SU(2)_L$ and $U(1)_Y$ gauge fields. Because experimental evidence is consistent with the existence of an $SU(2)_L \times U(1)_Y$ gauge symmetry, it is reasonable to require $\mathcal{L}_{\rm eff}$ to be invariant with respect to this symmetry. Thus, the second term in Eq. (1) consisting of operators up to energy dimension six, is also required to have local $SU(2)_L \times U(1)_Y$ gauge symmetry and the underlying physics is described using a linear realization [18] of the $SU(2)_L \times U(1)_Y$ symmetry. By considering operators that give rise to nonstandard $\gamma WW$ and $ZWW$ couplings at the tree level, $\mathcal{L}_{\rm eff}$ can be parametrized in terms of the $\alpha_i$ parameters [19]. Those parameters relate to the $f_i$ parameters of the Lagrangian given in Eq. (1) and to the TGCs in the Lagrangian of Eq. (2) as follows [20]:

$$\begin{aligned}
\Delta\kappa_\gamma &= (f_{W\phi} + f_{B\phi})\frac{M_W^2}{2\Lambda_{\rm NP}^2} = \alpha_{W\phi} + \alpha_{B\phi} \\
\Delta g_1^Z &= f_{W\phi}\frac{M_Z^2}{2\Lambda_{\rm NP}^2} = \Delta\kappa_Z + \frac{s_W^2}{c_W^2}\Delta\kappa_\gamma = \frac{\alpha_{W\phi}}{c_W^2} \\
\lambda &= \lambda_\gamma = \lambda_Z = 3g^2\frac{M_W^2}{2\Lambda_{\rm NP}^2} f_{WWW} = \alpha_W,
\end{aligned} \tag{5}$$

where $g$ is the $SU(2)_L$ gauge coupling constant ($g = e/\sin\theta_W$), $c_W = \cos\theta_W$, $s_W = \sin\theta_W$, and indices $W\phi$ ($B\phi$) and $W$ refer to operators that describe the interactions between the $W$ ($B$) gauge boson field and the Higgs field $\phi$, and the gauge boson field interactions, respectively. The relations in Eq. (5) give the expected order of magnitude for TGCs to be $\mathcal{O}(M_W^2/\Lambda_{\rm NP}^2)$. Thus, for $\Lambda_{\rm NP} \approx 2$ TeV, the expected order of magnitude for $\Delta\kappa_\gamma$, $\Delta g_1^Z$, and $\lambda$ is $\mathcal{O}(10^{-3})$. This gauge-invariant parametrization, also used at LEP, gives the following relations between the $\Delta\kappa_\gamma$, $\Delta g_1^Z$, and $\lambda$ couplings:

$$\Delta\kappa_Z = \Delta g_1^Z - \Delta\kappa_\gamma \cdot \tan^2\theta_W \quad \text{and} \quad \lambda \equiv \lambda_Z = \lambda_\gamma. \tag{6}$$

Hereafter we will refer to this relationship as the "LEP parametrization" [or $SU(2) \times U(1)$ respecting scenario] with three different parameters: $\Delta\kappa_\gamma$, $\lambda$, and $\Delta g_1^Z$. The

coupling $\Delta\kappa_Z$ can be expressed via the relation given by Eq. (6).

A second interpretive scenario, referred to as the equal couplings (or $ZWW = \gamma WW$) scenario [1], specifies the $\gamma WW$ and $ZWW$ couplings to be equal. This is also relevant for studying interference effects between the photon and $Z$-exchange diagrams in $WW$ production (see Fig. 1). In this case, electromagnetic gauge invariance forbids any deviation of $g_1^\gamma$ from its SM value ($\Delta g_1^Z = \Delta g_1^\gamma = 0$) and the relations between the couplings become

$$\Delta\kappa \equiv \Delta\kappa_Z = \Delta\kappa_\gamma \quad \text{and} \quad \lambda \equiv \lambda_Z = \lambda_\gamma. \tag{7}$$

As already stated, for $WW$ and $WZ$ production the anomalous couplings contribute to the total cross section via the $s$-channel diagram. Anomalous couplings enter the differential production cross sections through different helicity amplitudes that depend on $\hat{s}$. The coupling $\lambda$ primarily affects transversely polarized gauge bosons, which is the main contribution to the total cross section. Consequently, for a given $\hat{s}$, the sensitivity to the coupling $\lambda$ is higher than to $\kappa$ because $\lambda$ is multiplied by $\hat{s}$ in dominating amplitudes for $WW$ and $WZ$ production. Different sensitivity to the $\kappa$ couplings is expected due to the choice of scenario: the sensitivity to the $\kappa$ coupling in the equal couplings scenario is higher than in the LEP parametrization scenario simply because of the different relations between Eq. (6) and Eq. (7).

## IV. D0 DETECTOR

The analyzed data were produced in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV by the Tevatron collider at Fermilab and collected by the D0 detector [21] during 2002–2006. They correspond to $1.07 \pm 0.07$ fb$^{-1}$ of integrated luminosity for each of the two lepton channels ($e\nu q\bar{q}$ and $\mu\nu q\bar{q}$).

The D0 detector is a general purpose collider detector consisting of a central tracking system, a calorimeter system, and an outer muon system. The central tracking system consists of a silicon microstrip tracker and a central fiber tracker, both located within a 2 T superconducting solenoidal magnet, with designs optimized for tracking and vertexing at pseudorapidities [22] $|\eta| < 3$ and $|\eta| < 2.5$, respectively. A liquid-argon and uranium calorimeter has a central section covering pseudorapidities $|\eta|$ up to $\approx 1.1$, and two end calorimeters that extend coverage to $|\eta| \approx 4.2$, with all three housed in separate cryostats [23]. An outer muon system, covering $|\eta| < 2$, consists of a layer of tracking detectors and scintillation trigger counters in front of 1.8 T iron toroids, followed by two similar layers after the toroids [24].

Jets at D0 are reconstructed using the Run II cone algorithm [25] with cone radius $R = \sqrt{(\Delta y)^2 + (\Delta\phi)^2} = 0.5$; where $y$ is the rapidity. Jet energies are corrected to the particle level. The jet energy resolution for data, defined as $\sigma_{p_T}/p_T$, ranges from ~15%–25% for jets with $p_T =$ 20 GeV to ~7%–12% for jets with $p_T = 300$ GeV, depending on the rapidity of the jet.

The D0 detector uses a three-level trigger system for quickly filtering events from a rate of 1.7 MHz down to around 100 Hz that are stored for analysis. Events analyzed in the electron channel had to pass a trigger based on a single electron or electron + jet(s) requirement, resulting in an efficiency of $98^{+2}_{-3}$%. The triggers based on specific single muon and muon + jet(s) requirements are about 70% efficient. Thus, all available triggers were used for the muon channel to achieve higher efficiency. We select all events that satisfy our kinematic selection requirements with no specific trigger requirement. The efficiency in this kinematic region is very nearly 100%. To estimate and account for possible biases on the shape of kinematic distributions, we compare data selected with the inclusive triggers to data selected with triggers based on a single muon. In the kinematic region of interest, the inclusive trigger is estimated to have a shape uncertainty of less than 5% and a normalization uncertainty of 2%.

## V. EVENT SELECTION AND CROSS SECTION MEASUREMENT

The analysis presented here builds upon a previous publication in which we reported the first evidence of $WW/WZ$ production with semileptonic final states at a hadron collider [12]. Such events have two energetic jets from the hadronic decay of either a $W$ or $Z$ boson as well as an energetic charged lepton and significant missing transverse energy (indicating a neutrino) from the leptonic decay of the associated $W$ boson. Therefore, at the analysis level, we selected events with a reconstructed electron or muon with transverse momentum $p_T \geq 20$ GeV and pseudorapidity $|\eta| \leq 1.1(2.0)$ for electrons (muons), a missing transverse energy of $\not{E}_T \geq 20$ GeV, and at least two jets with $p_T \geq 20$ GeV and $|\eta| \leq 2.5$. The jet of highest $p_T$ was required to satisfy $p_T \geq 30$ GeV. To reduce background from processes that do not contain $W \to \ell\nu$, we required the transverse mass [26] from the lepton and $\not{E}_T$ to be $M_T^{\ell\nu} \geq 35$ GeV. The multijet background, for which a jet is misidentified as a lepton, was estimated using independent data samples.

Signal ($WW$ and $WZ$) and background ($W$ + jets, $Z$ + jets, $t\bar{t}$ and single top quark) processes were modeled using Monte Carlo (MC) simulation. All MC samples were normalized using next-to-leading order (NLO) or next-to-next-to-leading-order predictions for SM cross sections, except the dominant background $W$ + jets, which was scaled to match the data as described below.

In the previously published cross section measurement analysis [12], the signal and backgrounds were further separated using a multivariate classifier to combine information from several kinematic variables. The multivariate classifier chosen was a random forest (RF) classifier [27,28]. Thirteen well-modeled kinematic variables that

TABLE I. Measured number of events for signal and each background after the combined fit (with total uncertainties determined from the fit) and the number observed in data.

| | $e\nu q\bar{q}$ channel | $\mu\nu q\bar{q}$ channel |
|---|---|---|
| Diboson signal | 436 ± 36 | 527 ± 43 |
| $W$ + jets | 10 100 ± 500 | 11 910 ± 590 |
| $Z$ + jets | 387 ± 61 | 1180 ± 180 |
| $t\bar{t}$ + single top | 436 ± 57 | 426 ± 54 |
| Multijet | 1100 ± 200 | 328 ± 83 |
| Total predicted | 12 460 ± 550 | 14 370 ± 620 |
| Data | 12 473 | 14 392 |

demonstrated a difference in probability density between signal and at least one of the backgrounds were used as inputs to the RF. The effects of systematic uncertainties on the normalization and on the shape of the RF distributions were evaluated for signal and backgrounds.

The signal cross section was determined from a fit of signal and background RF output distributions to the data by minimizing a Poisson $\chi^2$ function (i.e., a negative log likelihood) with respect to variations of the systematic uncertainties [29], assuming SM $\gamma WW$ and $ZWW$ couplings. The fit simultaneously varied the $WW/WZ$ and $W$ + jets contributions, thereby also determining the normalization factor for the $W$ + jets MC sample. The measured yields for signal and each background are given in Table I and the dijet mass peak extracted from data compared to the $WW/WZ$ MC prediction is shown in Fig. 2. The combined fit of both channels to the RF output resulted in a measured cross section of $20.2 \pm 2.5(\text{stat}) \pm 3.6(\text{syst}) \pm 1.2(\text{lumi})$ pb, which is consistent with the NLO SM predicted cross section of $\sigma(WW + WZ) = 16.1 \pm 0.9$ pb [30].

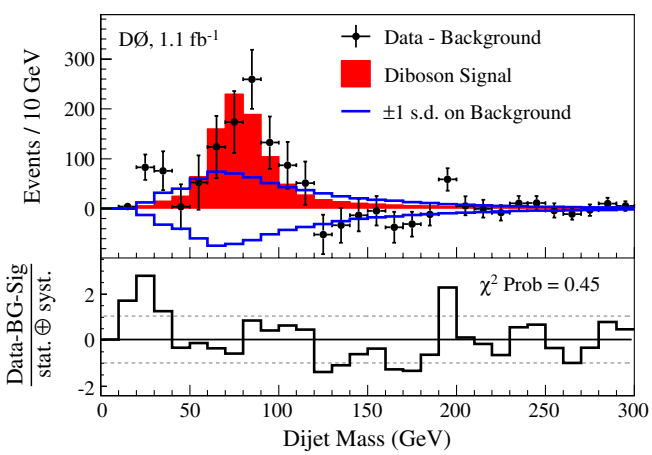


FIG. 2 (color online). A comparison of the extracted signal (filled histogram) to background-subtracted data (points), along with the ±1 standard deviation (s.d.) systematic uncertainty on the background. The residual distance between the data points and the extracted signal, divided by the total uncertainty, is given at the bottom.

## VI. SENSITIVITY TO ANOMALOUS COUPLINGS

For TGCs analysis we use the same selection and set limits on anomalous TGCs using a kinematic variable that is highly sensitive to the effects of deviations of $\Delta\kappa$, $\lambda$, and $\Delta g_1^Z$. Because TGCs introduce terms in the Lagrangian that are proportional to the momentum of the weak boson, the differential and the total cross sections will deviate from the SM prediction in the presence of anomalous couplings. This behavior is also expected at large production angles of a weak boson. Thus, the weak boson transverse momentum spectrum, $p_T$, is sensitive to anomalous couplings and can show a significant enhancement at high values of $p_T$.

The predicted $WW$ and $WZ$ production cross sections in the presence of anomalous TGCs are generated with the leading order (LO) MC generator of Hagiwara, Zeppenfeld, and Woodside (HZW) [1] with CTEQ5L [31] parton distribution functions (PDFs). For example,

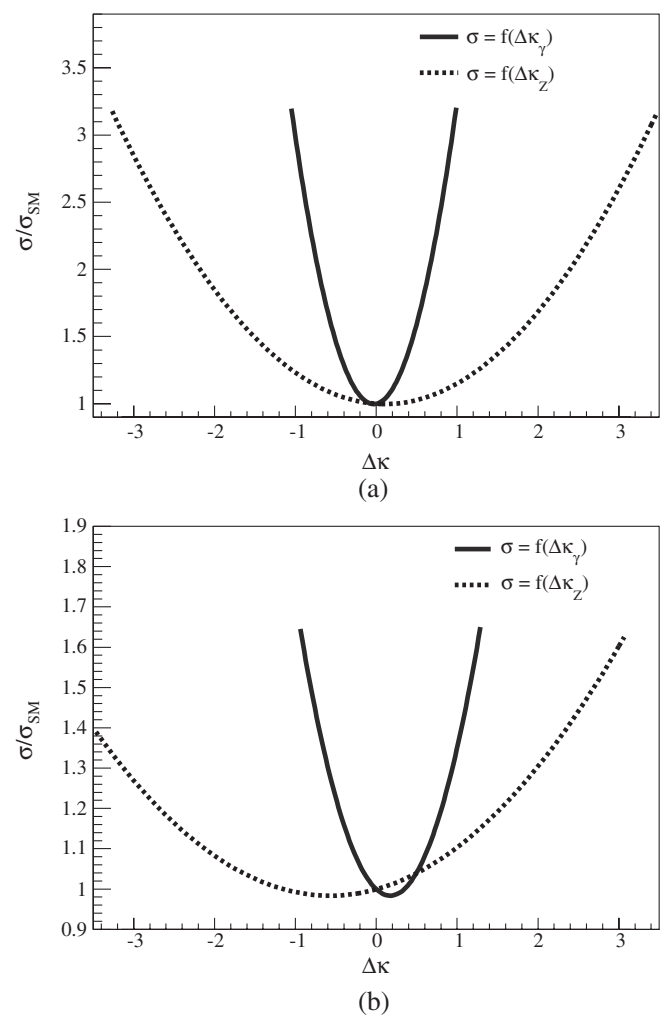


FIG. 3. Semileptonic production cross sections for (a) $WW$ and (b) $WZ$ normalized to the SM prediction as a function of anomalous coupling $\Delta\kappa$ ($\lambda = \Delta g_1^Z = 0$) in the LEP parametrization scenario. The new physics scale $\Lambda_{\text{NP}}$ is set to 2 TeV.

the predicted "anomalous" cross sections relative to the SM value given by the HZW generator are shown in Fig. 3 as a function of anomalous couplings. For this figure we vary only the $\Delta\kappa$ coupling with the constraint between $\Delta\kappa_\gamma$ and $\Delta\kappa_Z$ as given by Eq. (6). The couplings $\lambda$ and $\Delta g_1^Z$ are fixed to their SM values (i.e., $\lambda = \Delta g_1^Z = 0$). The effects of anomalous couplings on two $WW$ kinematic distributions ($p_T$ and rapidity of the $q\bar{q}$ system) for the LEP parametrization are shown in Fig. 4. Here again, we vary only one coupling at a time ($\Delta\kappa$, $\lambda$, or $\Delta g_1^Z$) according to Eq. (6) and leave the others fixed to their SM values. Finally, we choose the $p_T^{q\bar{q}}$ (i.e., reconstructed dijet $p_T$) distribution to be our kinematic variable to probe anomalous couplings in data. Results are interpreted in two different scenarios: LEP parametrization and equal couplings, both with $\Lambda_{\rm NP} = 2$ TeV.

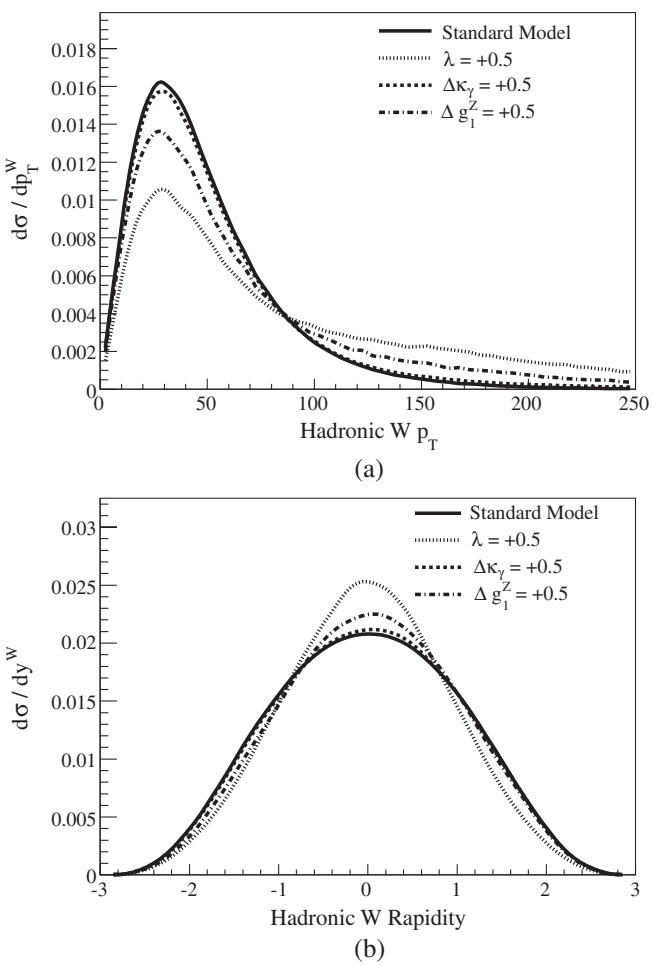


FIG. 4. Normalized distributions of the hadronic $W$ boson (a) $p_T$ and (b) rapidity at the parton level in $WW$ production including anomalous couplings under the LEP parametrization scenario: $\Delta\kappa_\gamma = +0.5$ ($\lambda = \Delta g_1^Z = 0$, $\Delta\kappa_Z = -0.15$), $\lambda = +0.5$ ($\Delta\kappa_\gamma = \Delta\kappa_Z = \Delta g_1^Z = 0$), and $\Delta g_1^Z = +0.5$ ($\Delta\kappa_\gamma = \lambda = 0$, $\Delta\kappa_Z = 1.5$) compared to the SM distribution for $WW$ production with unity normalization. The new physics scale $\Lambda_{\rm NP}$ is set to 2 TeV.

## VII. REWEIGHTING METHOD

The PYTHIA [32] LO MC generator with CTEQ6L1 PDFs was used to simulate a sample of $WW$ and $WZ$ events at LO. We use the MC@NLO MC generator [33] with CTEQ6M PDFs to correct the event kinematics for higher order QCD effects by reweighting the differential distributions of $p_T(WV)$ and $\Delta R(W, V)$ produced by PYTHIA to match those produced via MC@NLO. We simulate the LO effects of anomalous couplings on the $p_T$ distribution by reweighting the SM predictions for $WW$ and $WZ$ production from PYTHIA to include the contribution from the presence of anomalous couplings. The anomalous coupling contribution to the normalization and to the shape of $p_T^{q\bar{q}}$ distribution relative to the SM is predicted by the HZW LO MC generator.

The reweighting method uses the matrix element values given by the generator to predict an event rate in the presence of anomalous couplings. More precisely, an event rate ($R$) is assigned representing the ratio of the differential cross section with anomalous couplings to the SM differential cross section. Because the HZW generator does not recalculate matrix element values, we use high statistics samples to estimate the weight as a function of different anomalous couplings. Thus, we consider our approach to be a close approximation of an exact reweighting method.

The basis of the reweighting method is that, in general, the equation of the differential cross section, which has a quadratic dependence on the anomalous couplings, can be written as

$$\begin{aligned} d\sigma &= \text{const} \cdot |\mathcal{M}|^2 dX = \text{const} \cdot |\mathcal{M}|^2_{\rm SM} \frac{|\mathcal{M}|^2}{|\mathcal{M}|^2_{\rm SM}} dX \\ &= \text{const} \cdot |\mathcal{M}|^2_{\rm SM}[1 + A(X)\Delta\kappa + B(X)\Delta\kappa^2 + C(X)\lambda \\ &\quad + D(X)\lambda^2 + E(X)\Delta\kappa\lambda + \ldots]dX \\ &= d\sigma_{\rm SM} \cdot R(X; \Delta\kappa, \lambda, \ldots), \end{aligned} \tag{8}$$

where $d\sigma$ is the differential cross section that includes the contribution from the anomalous couplings, $d\sigma_{\rm SM}$ is the SM differential cross section, $X$ is a kinematic distribution sensitive to the anomalous couplings, and $A(X)$, $B(X)$, $C(X)$, $D(X)$, and $E(X)$ are reweighting coefficients dependent on $X$.

In the LEP parametrization, Eq. (8) is parametrized with the three couplings $\Delta\kappa_\gamma$, $\lambda$, and $\Delta g_1^Z$ and nine reweighting coefficients, $A(X) - I(X)$. Thus, the weight $R$ in the LEP parametrization scenario is defined as

$$\begin{aligned} R(X; \Delta\kappa, \lambda, \Delta g_1) &= 1 + A(X)\Delta\kappa + B(X)(\Delta\kappa)^2 + C(X)\lambda \\ &\quad + D(X)\lambda^2 + E(X)\Delta g_1 + F(X)(\Delta g_1)^2 \\ &\quad + G(X)\Delta\kappa\lambda + H(X)\Delta\kappa\Delta g_1 \\ &\quad + I(X)\lambda\Delta g_1 \end{aligned} \tag{9}$$

with $\Delta\kappa = \Delta\kappa_\gamma$, $\lambda = \lambda_\gamma = \lambda_Z$, and $\Delta g_1 = \Delta g_1^Z$.

TABLE II. The values of $\Delta\kappa_\gamma$, $\lambda$, and $\Delta g_1^Z$ used to calculate the reweighting coefficients $A(X) - I(X)$ in the LEP parametrization scenario.

| | $F_1$ | $F_2$ | $F_3$ | $F_4$ | $F_5$ | $F_6$ | $F_7$ | $F_8$ | $F_9$ |
|---|---|---|---|---|---|---|---|---|---|
| $\Delta\kappa_\gamma$ | 0 | 0 | +0.5 | −0.5 | 0 | 0 | +0.5 | +0.5 | 0 |
| $\lambda$ | +0.5 | −0.5 | 0 | 0 | 0 | 0 | +0.5 | 0 | +0.5 |
| $\Delta g_1^Z$ | 0 | 0 | 0 | 0 | +0.5 | −0.5 | 0 | +0.5 | +0.5 |

In the equal couplings scenario, Eq. (8) is parametrized with the two couplings $\Delta\kappa$ and $\lambda$ and five reweighting coefficients, $A(X) - E(X)$. In this case the weight is defined as

$$R(X; \Delta\kappa, \lambda) = 1 + A(X)\Delta\kappa + B(X)\Delta\kappa^2 + C(X)\lambda + D(X)\lambda^2 + E(X)\Delta\kappa\lambda \tag{10}$$

with $\Delta\kappa = \Delta\kappa_\gamma = \Delta\kappa_Z$ and $\lambda = \lambda_\gamma = \lambda_Z$.

The kinematic variable $X$ is chosen to be the $p_T$ of the $q\bar{q}$ system, which is highly sensitive to anomalous couplings, as demonstrated in Fig. 4. Depending on the number of reweighting coefficients, a system of the same number of equations allows us to calculate their values for each event. Applied on the SM distribution of $X$ for any combination of anomalous couplings, the distribution of $X$ weighted by $R$ corresponds to the kinematic distribution in the presence of the given non-SM TGC.

To calculate reweighting coefficients in the LEP parametrization scenario, we generate nine different functions, $F_i$ $(i = 1 - 9)$, fitting the shape of the $p_T^{q\bar{q}}$ distributions in the presence of anomalous couplings. The values of anomalous TGCs are chosen to deviate $\pm 0.5$ relative to the SM as shown in Table II. We calculate nine weights $R_i$ normalizing the functions $F_i$ with the cross sections given by the HZW generator.

To verify the derived reweighting parameters, we calculated the weight $R$ for different $\Delta\kappa$, $\lambda$, and/or $\Delta g_1^Z$ values, applied the reweighting coefficients and compared reweighted $p_T^{q\bar{q}}$ shapes to those predicted by the generator. Discrepancies in the $p_T^{q\bar{q}}$ shape of less than 5% and in normalization of less than 0.1% from those predicted by the generator represent reasonable agreement.

When measuring TGCs in the LEP parametrization, we vary two of the three couplings at a time, leaving the third coupling fixed to its SM value. This gives the three two-parameter combinations $(\Delta\kappa, \lambda)$, $(\Delta\kappa, \Delta g_1^Z)$, and $(\lambda, \Delta g_1^Z)$. For the equal couplings scenario there is only the $(\Delta\kappa, \lambda)$ combination. In each case, the two couplings being evaluated are each varied between $-1$ and $+1$ in steps of 0.01. For a given pair of anomalous coupling values, each event in a reconstructed dijet $p_T$ bin is weighted by the appropriate weight $R$ and all the weights are summed in that bin. The observed limits are determined from a fit of background and reweighted signal MC distributions for differ-

TABLE III. Systematic uncertainties in percent for Monte Carlo simulations and multijet estimates. Uncertainties are identical for both lepton channels except where otherwise indicated. The nature of the uncertainty, i.e., whether it refers to a normalization uncertainty (type I) or a shape dependence (type II), is also provided. The values for uncertainties with a shape dependence correspond to the maximum amplitude of shape fluctuations in the dijet $p_T$ distribution (0 GeV $\leq p_T \leq$ 300 GeV) after $\pm 1$ s.d. parameter changes. However, the full shape dependence is included in the calculations.

| Source of systematic uncertainty | Diboson signal [%] | $W$ + jets [%] | $Z$ + jets [%] | Top [%] | Multijet [%] | Type |
|---|---|---|---|---|---|---|
| Trigger efficiency, electron channel[a] | $+2/-3$ | $+2/-3$ | $+2/-3$ | $+2/-3$ | | I |
| Trigger efficiency, muon channel | $+0/-5$ | $+0/-5$ | $+0/-5$ | $+0/-5$ | | II |
| Lepton identification[a] | $\pm 4$ | $\pm 4$ | $\pm 4$ | $\pm 4$ | | I |
| Jet identification | $\pm 1$ | $\pm 1$ | $\pm 1$ | $\pm < 1$ | | II |
| Jet energy scale | $\pm 4$ | $\pm 7$ | $\pm 5$ | $\pm 5$ | | II |
| Jet energy resolution | $\pm 3$ | $\pm 4$ | $\pm 4$ | $\pm 4$ | | I |
| Luminosity | $\pm 6.1$ | $\pm 6.1$ | $\pm 6.1$ | $\pm 6.1$ | | I |
| Cross section (including PDF uncertainties) | | $\pm 20$ | $\pm 6$ | $\pm 10$ | | I |
| Multijet normalization, electron channel | | | | | $\pm 20$ | I |
| Multijet normalization, muon channel | | | | | $\pm 30$ | I |
| Multijet shape, electron channel | | | | | $\pm 7$ | II |
| Multijet shape, muon channel | | | | | $\pm 10$ | II |
| Diboson signal NLO/LO shape | $\pm 10$ | | | | | II |
| Diboson signal reweighting shape | $\pm 5$ | | | | | II |
| Parton distribution function (acceptance only) | $\pm 1$ | $\pm 3$ | $\pm 2$ | $\pm 2$ | | II |
| ALPGEN $\eta$ and $\Delta R$ corrections | | $\pm 1$ | $\pm 1$ | | | II |
| Renormalization and factorization scale | | $\pm 1$ | $\pm 1$ | | | II |
| ALPGEN parton-jet matching parameters | | $\pm 1$ | $\pm 1$ | | | II |

[a]Lepton efficiencies depend on kinematics; however, their fractional uncertainties are much less kinematically dependent and have a negligible effect on the shape of the dijet $p_T$ distribution.

ent anomalous couplings contributions to the observed data using the dijet $p_T$ distribution of candidate events.

## VIII. SYSTEMATIC UNCERTAINTIES

We consider two general types of systematic uncertainties. Uncertainties of the first class (type I) are related to the overall normalization and efficiencies of the various contributing physical processes. The largest contributing type I uncertainties are those related to the accuracy of the theoretical cross section used to normalize the background processes. These uncertainties are considered to arise from Gaussian parent distributions. The second class (type II) consists of uncertainties that, when propagated through the analysis selection, impact the shape of the dijet $p_T$ distribution. The dependence of the dijet $p_T$ distribution on these uncertainties is determined by varying each parameter by its associated uncertainty ( $\pm$ 1 s.d.) and reevaluating the shape of the dijet $p_T$ distribution. The resulting shape dependence is considered to arise from a Gaussian parent distribution. Although type II uncertainties may also impact efficiencies or normalization, any uncertainty shown to impact the shape of the dijet $p_T$ distribution is treated as type II. Both types of systematic uncertainty are assumed to be 100% correlated amongst backgrounds and signals. All sources of systematic uncertainty are assumed to be mutually independent, and no intercorrelation is propagated. A list of the systematic uncertainties used in this analysis can be found in Table III.

## IX. ANOMALOUS COUPLING LIMITS

The fit utilizes the MINUIT [34] software package to minimize a Poisson $\chi^2$ with respect to variations to the systematic uncertainties [29]. The $\chi^2$ function used is

$$\chi^2 = -2\ln\left(\prod_{i=1}^{N_b}\frac{\mathcal{L}^P(d_i; m_i(\vec{R}))}{\mathcal{L}^P(d_i; d_i)}\prod_{k=1}^{N_s}\frac{\mathcal{L}^G(R_k\sigma_k; 0, \sigma_k)}{\mathcal{L}^G(0; 0, \sigma_k)}\right)$$
$$= 2\sum_{i=1}^{N_b} m_i(\vec{R}) - d_i - d_i\ln\left(\frac{m_i(\vec{R})}{d_i}\right) + \sum_{k=1}^{N_s} R_k^2,$$

in which the indices $i$ and $k$ run over the number of histogram bins ($N_b$) and the number of systematic uncertainties ($N_s$), respectively. In this function $\mathcal{L}^P(\alpha; \beta)$ is the Poisson probability for $\alpha$ events with a mean of $\beta$ events; $\mathcal{L}^G(x; \mu, \sigma)$ is the Gaussian probability for $x$ events in a distribution with a mean value of $\mu$ and a variance $\sigma^2$; $R_k$ is a dimensionless parameter describing departures in nuisance parameters in units of the associated systematic uncertainty $\sigma_k$; $d_i$ is the number of data events in bin $i$; and $m_i(\vec{R})$ is the number of predicted events in bin $i$ [29].

Systematics are treated as Gaussian-distributed uncertainties on the expected numbers of signal and background events. The individual background contributions are fitted to the data by minimizing this $\chi^2$ function over the individual systematic uncertainties [29]. The fit computes the optimal central values for the systematic uncertainties, while accounting for departures from the nominal predictions by including a term in the $\chi^2$ function that sums the squared deviation of each systematic in units normalized by its $\pm 1$ s.d. uncertainties.

Figure 5 shows the dijet $p_T$ distributions in the combined electron and muon channels after the fit. The value of $\chi^2$ is measured between data and MC dijet $p_T$ distributions as the signal MC is varied in the presence of anomalous couplings. The $\Delta\chi^2$ values of 1 and 3.84 from the minimum $\chi^2$ in the parameter space, for which all other anomalous couplings are zero, represent the 68% confidence level (C.L.) and 95% C.L. limits, respectively. For the LEP

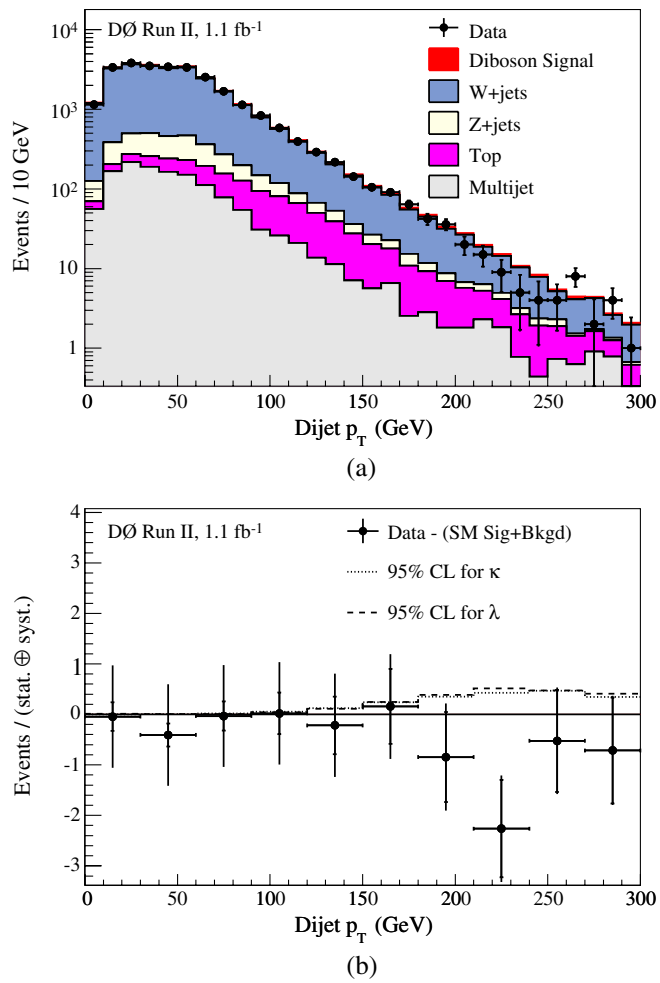


FIG. 5 (color online). (a) The dijet $p_T$ distribution of combined (electron + muon) channels for data and SM predictions following the fit of MC to data. (b) The difference between data and simulation divided by the uncertainty (statistical and systematic) for the dijet $p_T$ distribution. Also shown are the MC signals for anomalous couplings corresponding to the 95% C.L. limits for $\Delta\kappa$ and $\lambda$ in the LEP parametrization scenario. The full error bars on the data points reflect the total (statistical and systematic) uncertainty, with the ticks indicating the contribution due only to the statistical uncertainty.

TABLE IV. The most probable values with total uncertainties (statistical and systematic) at 68% C.L. for $\kappa_\gamma$, $\lambda$, and $g_1^Z$ along with observed 95% C.L. one-parameter limits on $\Delta\kappa_\gamma$, $\lambda$, and $\Delta g_1^Z$ measured in 1.1 fb$^{-1}$ of $WW/WZ \to \ell\nu jj$ events with $\Lambda_{\rm NP} = 2$ TeV.

| 68% C.L. | $\kappa_\gamma$ | $\lambda = \lambda_\gamma = \lambda_Z$ | $g_1^Z$ |
|---|---|---|---|
| LEP parametrization | $\kappa_\gamma = 1.07^{+0.26}_{-0.29}$ | $\lambda = 0.00^{+0.06}_{-0.06}$ | $g_1^Z = 1.04^{+0.09}_{-0.09}$ |
| Equal couplings | $\kappa_\gamma = \kappa_Z = 1.04^{+0.11}_{-0.11}$ | $\lambda = 0.00^{+0.06}_{-0.06}$ | |
| 95% C.L. | $\Delta\kappa_\gamma$ | $\lambda = \lambda_\gamma = \lambda_Z$ | $\Delta g_1^Z$ |
| LEP parametrization | $-0.44 < \Delta\kappa_\gamma < 0.55$ | $-0.10 < \lambda < 0.11$ | $-0.12 < \Delta g_1^Z < 0.20$ |
| Equal couplings | $-0.16 < \Delta\kappa < 0.23$ | $-0.11 < \lambda < 0.11$ | |

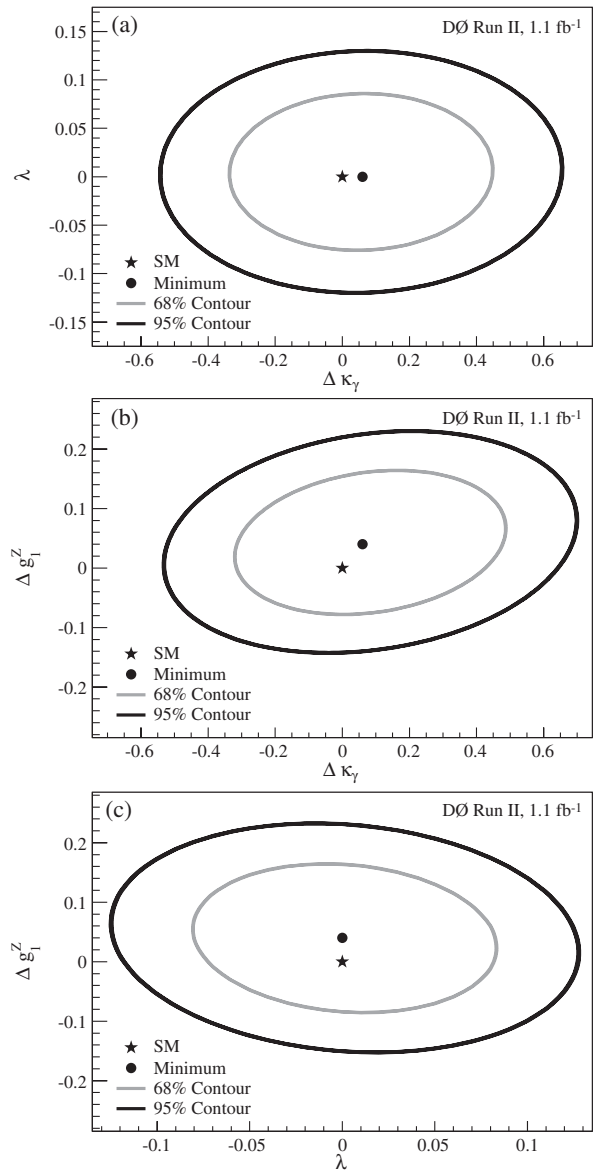


FIG. 6. The 68% C.L. and 95% C.L. two-parameter limits on the $\gamma WW/ZWW$ coupling parameters $\Delta\kappa_\gamma$, $\lambda$, and $\Delta g_1^Z$, in the LEP parametrization scenario and $\Lambda_{\rm NP} = 2$ TeV. The dots indicate the most probable values of anomalous couplings from the two-parameter combined (electron + muon) fit and the star markers denote the SM prediction.

parametrization, the most probable coupling values as measured in data with associated uncertainties at 68% C.L. are $\kappa_\gamma = 1.07^{+0.26}_{-0.29}$, $\lambda = 0.00^{+0.06}_{-0.06}$, and $g_1^Z = 1.04^{+0.09}_{-0.09}$. For the equal couplings scenario the most probable coupling values as measured in data with associated uncertainties at 68% C.L. are $\kappa = 1.04^{+0.11}_{-0.11}$ and $\lambda = 0.00^{+0.06}_{-0.06}$. The observed 95% C.L. limits estimated from the single parameter fit are $-0.44 < \Delta\kappa_\gamma < 0.55$, $-0.10 < \lambda < 0.11$, and $-0.12 < \Delta g_1^Z < 0.20$ for the LEP parametrization or $-0.16 < \Delta\kappa < 0.23$ and $-0.11 < \lambda < 0.11$ for the equal couplings scenario (Table IV).

The observed 68% C.L. and 95% C.L. limits in two-parameter space are shown in Figs. 6 and 7 as a function of anomalous couplings along with the most probable values of $\Delta\kappa$, $\lambda$, and $\Delta g_1^Z$.

As shown in Table V, the 95% C.L. limits on anomalous couplings $\Delta\kappa_\gamma$, $\Delta\lambda$, and $\Delta g_1^Z$ set using the dijet $p_T$ distribution of $WW/WZ \to \ell\nu jj$ events are comparable with the 95% C.L. limits set by the D0 Collaboration from $WW$ [3], $WZ$ [4], and $W\gamma$ [5] production in fully leptonic channels using $\approx 1$ fb$^{-1}$ of data. The most recent 95% C.L. one-parameter limits from the CDF

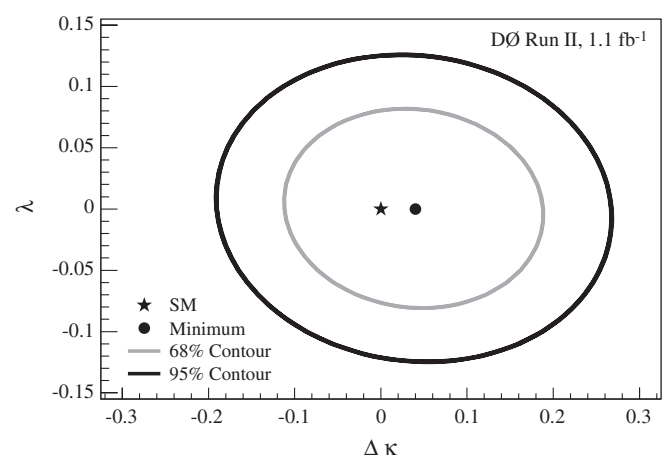


FIG. 7. The 68% C.L. and 95% C.L. two-parameter limits on the $\gamma WW/ZWW$ coupling parameters $\Delta\kappa$ and $\lambda$, in the equal couplings scenario and $\Lambda_{\rm NP} = 2$ TeV. The dot indicates the most probable values of anomalous couplings from the two-parameter combined (electron + muon) fit and the star marker denotes the SM prediction.

TABLE V. Comparison of 95% C.L. one-parameter TGC limits between the different channels studied at D0 with $\approx 1$ fb$^{-1}$ of data: $WW \to \ell\nu\ell\nu$, $W\gamma \to \ell\nu\gamma$, $WZ \to \ell\ell\ell\nu$, and $WW + WZ \to \ell\nu jj$ ($l = \mu, e$) at $\Lambda_{\rm NP} = 2$ TeV.

| LEP parametrization | $\Delta\kappa_\gamma$ | $\lambda = \lambda_\gamma = \lambda_Z$ | $\Delta g_1^Z$ |
|---|---|---|---|
| $WZ \to \ell\nu\ell\ell$ (1 fb$^{-1}$) | | $-0.17 < \lambda < 0.21$ | $-0.14 < \Delta g_1^Z < 0.34$ |
| $W\gamma \to \ell\nu\gamma$ (0.7 fb$^{-1}$) | $-0.51 < \Delta\kappa_\gamma < 0.51$ | $-0.12 < \lambda < 0.13$ | |
| $WW \to \ell\nu\ell\nu$ (1 fb$^{-1}$) | $-0.54 < \Delta\kappa_\gamma < 0.83$ | $-0.14 < \lambda < 0.18$ | $-0.14 < \Delta g_1^Z < 0.30$ |
| $WW + WZ \to \ell\nu jj$ (1.1 fb$^{-1}$) | $-0.44 < \Delta\kappa_\gamma < 0.55$ | $-0.10 < \lambda < 0.11$ | $-0.12 < \Delta g_1^Z < 0.20$ |
| Equal couplings | $\Delta\kappa_\gamma$ | $\lambda = \lambda_\gamma = \lambda_Z$ | $\Delta g_1^Z$ |
| $WZ \to \ell\nu\ell\ell$ (1 fb$^{-1}$) | | $-0.17 < \lambda < 0.21$ | |
| $W\gamma \to \ell\nu\gamma$ (0.7 fb$^{-1}$) | | $-0.12 < \lambda < 0.13$ | |
| $WW \to \ell\nu\ell\nu$ (1 fb$^{-1}$) | $-0.12 < \Delta\kappa < 0.35$ | $-0.14 < \lambda < 0.18$ | |
| $WW + WZ \to \ell\nu jj$ (1.1 fb$^{-1}$) | $-0.16 < \Delta\kappa < 0.23$ | $-0.11 < \lambda < 0.11$ | |

TABLE VI. Measured values of $\kappa_\gamma$, $\lambda$, and $g_1^Z$ couplings and their associated uncertainties at 68% C.L. obtained from the one-parameter fits combining data from different topologies and energies at LEP2 experiments. The last column shows the D0 result obtained from the $\ell\nu jj$ final states only selected from 1 fb$^{-1}$ of data. The uncertainties include both statistical and systematic sources.

| 68% C.L. | ALEPH | OPAL | L3 | D0 ($\ell\nu jj$) |
|---|---|---|---|---|
| $\kappa_\gamma$ | $0.971 \pm 0.063$ | $0.88^{+0.09}_{-0.08}$ | $1.013 \pm 0.071$ | $1.07^{+0.26}_{-0.29}$ |
| $\lambda$ | $-0.012 \pm 0.029$ | $-0.060^{+0.034}_{-0.033}$ | $-0.021 \pm 0.039$ | $0.00^{+0.06}_{-0.06}$ |
| $g_1^Z$ | $1.001 \pm 0.030$ | $0.987^{+0.034}_{-0.033}$ | $0.966 \pm 0.036$ | $1.04^{+0.09}_{-0.09}$ |

Collaboration under the equal couplings scenario at $\Lambda_{\rm NP} = 1.5$ TeV are $-0.46 < \Delta\kappa < 0.39$ and $-0.18 < \lambda < 0.17$ using 350 pb$^{-1}$ of data, combining the $\ell\nu jj$ and $\ell\nu\gamma$ ($l = e, \mu$) final states [6]. These results are limited by statistics, but a factor of nearly 10 times more data is expected to be available for analysis by D0 by the end of Run II of the Fermilab Tevatron. With additional data the potential to reach the individual LEP2 anomalous TGC limits [7–9] shown in Table VI is significant. The combined LEP2 results still represent the world's tightest limits on charged anomalous couplings [10] and give the most probable values of $\kappa_\gamma$, $\lambda$, and $g_1^Z$ as $\kappa_\gamma = 0.973^{+0.044}_{-0.045}$, $\lambda = -0.028^{+0.020}_{-0.021}$, and $g_1^Z = 0.984^{+0.022}_{-0.019}$ at 68% C.L.

In summary, we have presented a measurement of $\gamma WW/ZWW$ couplings using a sample of semileptonic decays of $WW/WZ$ boson pairs corresponding to 1.1 fb$^{-1}$ of $p\bar{p}$ collisions collected with the D0 detector at the Fermilab Tevatron Collider. The measurement is in agreement with the SM. On the other hand, this analysis yields the most stringent limits on $\gamma WW/ZWW$ anomalous couplings from the Tevatron to date, complementing similar measurements performed in fully leptonic decay modes from $W\gamma$, $WW$, and $WZ$ production.

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