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Precise Measurement of the Top Quark Mass in the Dilepton Channel at D0


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We measure the top quark mass ($m_t$) in $p\bar{p}$ collisions at a center of mass energy $\sqrt{s} = 1.96$ TeV using dilepton $t\bar{t} \rightarrow W^+bW^-\bar{b} \rightarrow \ell^+\nu_\ell b\ell^-\bar{\nu}_\ell\bar{b}$ events, where $\ell$ denotes an electron, a muon, or a tau that decays leptonically. The data correspond to an integrated luminosity of 5.4 fb$^{-1}$ collected with the D0 detector at the Fermilab Tevatron Collider. We obtain $m_t = 174.0 \pm 1.8$(stat) $\pm 2.4$(syst) GeV, which is in agreement with the current world average $m_t = 173.3 \pm 1.1$ GeV. This is currently the most precise measurement of $m_t$ in the dilepton channel.

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The measurement of the properties of the top quark has been a major goal of the Fermilab Tevatron Collider experiments since its discovery in 1995 [1,2]. As the heaviest known elementary particle, the top quark may play a special role in the mechanism of electroweak symmetry breaking. A precise measurement of its mass ($m_t$) is of particular importance, since, combined with the measurement of the W boson mass, it provides an indirect constraint on the mass of the Higgs boson in the standard model (SM) and can also constrain possible extensions of the SM.

We present a new measurement of the top quark mass in the dilepton channel ($ee$, $e\mu$, $\mu\mu$) in $t\bar{t} \rightarrow W^+bW^-\bar{b} \rightarrow \ell^+\nu_\ell b\ell^-\bar{\nu}_\ell\bar{b}$ events, where $\ell$ denotes an electron, a muon, or a tau decaying leptonically, using the matrix element method. The first measurement of $m_t$ based on this method was performed in the lepton + jets channel by the D0 experiment [3]. The CDF Collaboration has applied the matrix element approach to determine $m_t$ in the dilepton and all-hadronic final states [4,5], obtaining a mass precision of 4.0 GeV for dilepton events [4]. The measurement of $m_t$ in the dilepton channel has also been carried out by using other techniques [6–11], reaching a precision of 3.7 GeV. We report a measurement based on data collected by the D0 detector, corresponding to 5.4 fb$^{-1}$ of integrated luminosity from $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV.

The D0 detector has a central tracking system, consisting of a silicon microstrip tracker and a central fiber tracker, both located within a 1.9 T superconducting solenoidal magnet [12], with the design providing tracking and vertexing at pseudorapidities $|\eta| < 3$ [13]. The liquid-argon and uranium calorimeter has a central section covering pseudorapidities $|\eta|$ up to $\approx 1.1$ and two end calorimeters that extend coverage to $|\eta| \approx 4.2$, with all three housed in separate cryostats [14]. A muon system outside the calorimeters covers $|\eta| < 2$ and consists of a
layer of tracking detectors and scintillation trigger counters in front of 1.8 T toroids, followed by two similar layers after the toroids [15].

Despite the small branching fraction of this final state and the presence of two neutrinos in each event, the measurement of $m_t$ in the dilepton channel is interesting because the lower background and the smaller jet multiplicity relative to the lepton + jets channel result in a reduced sensitivity to the ambiguity from combining jets in the reconstruction of $m_t$. The dilepton measurement therefore complements the results from other final states. Moreover, significant differences in measured values of $m_t$ in different $\bar{t}t$ decay channels can be indicative of the presence of physics beyond the SM [16].

As the SM predicts top quarks to decay almost 100% of the time into a $W$ boson and a $b$ quark, $\bar{t}t$ events are classified according to the decays of the $W$ boson. In the dilepton channel, both $W$ bosons decay leptonically: $W^+ \rightarrow \ell^+ \nu_\ell t$ [17] with $\ell = e$, $\mu$, or $\tau$. We analyze the events characterized by two leptons $ee$, $e\mu$, or $\mu\mu$, with a large transverse momenta ($p_T$), large imbalance in transverse momentum from the undetected neutrinos ($p_T$), and two high-$p_T$ jets from the $b$ quarks. The $W^+ \rightarrow \tau^+ \nu_\tau \rightarrow \ell^+ \nu_\ell \bar{\nu}_\tau$ decays contribute through secondary $\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_e$ transitions. For the $ee$ and $\mu\mu$ analysis, we consider events selected by a set of single-lepton triggers. For the $e\mu$ channel, we use a mixture of single and multilepton triggers and $e+\mu$ lepton jets. Dilepton $\bar{t}t$ events are required to have at least two oppositely charged, isolated leptons with $p_T > 15$ GeV and either $|\eta| < 1$ or $1 < |\eta| < 2.5$ for electrons and $|\eta| < 2$ for muons. If more than one lepton-pair combination is found in an event, only the pair with the largest sum in scalar $p_T$ is used. Events must have at least two jets with $p_T > 20$ GeV and $|\eta| < 2.5$, well separated from the selected electrons. No explicit $b$-jet identification is required in this analysis. The main sources of background in the dilepton channel are Drell-Yan and $Z$ boson production ($Z/\gamma^* \rightarrow \ell^+ \ell^-$), diboson production ($WW, WZ, ZZ$), and instrumental background that originates from limited detector resolution and lepton misidentification. In the $ee$ channel, the discrimination between the $\bar{t}t$ signal and background improves by requiring a large significance of the measured $p_T$, which is defined through a likelihood discriminant constructed from the ratio of $\hat{p}_T$ to its uncertainty [18]. In the $\mu\mu$ channel, we require, in addition, $p_T > 40$ GeV. In the $e\mu$ channel, the requirement $H_T > 115$ GeV, where $H_T$ is the scalar sum of the transverse momenta of the leading lepton and the two leading jets, rejects most of the contribution from $\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_e$. The above selections minimize the expected statistical uncertainty on $m_t$. In total, we select 479 candidate events with 73, 266, and 140 events, respectively, in the $ee$, $e\mu$, and $\mu\mu$ channels, of which about 13 ± 5, 48 ± 15, and 56 ± 15 events, respectively, are expected to arise from the background.

The matrix element method is based on the probability for a given event to resemble a signal, which depends on the value of $m_t$, or a background, which is usually independent of $m_t$. Assuming that the different physics processes leading to the same final state do not interfere, the event probability can be written as the sum of probabilities from all possible contributions. In practice, because the matrix element method requires significant computing time, only the dominant background is taken into account, and the total event probability is given by

$$P_{\text{evt}} = f_{\bar{t}t}P_{\bar{t}t}(x; m_t) + (1 - f_{\bar{t}t})P_{Z+2\text{jets}}(x),$$

where $f_{\bar{t}t}$ is the fraction of $\bar{t}t$ events, $P_{\bar{t}t}$ and $P_{Z+2\text{jets}}$ are the signal and background probability densities, respectively, $m_t$ is the assumed top quark mass, and $x$ reflects the observed kinematic variables, i.e., the four-momenta of the measured jets and leptons. In the $ee$, $\mu\mu$, and $e\mu$ channels, $Z + 2$ jets events with $Z \rightarrow e^+ e^-$, $Z \rightarrow \mu^+ \mu^-$, and $Z \rightarrow \tau^+ \tau^- \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu$ are the dominant source of background. The second leading background, from misidentified leptons, is approximately a factor of 3 smaller. While neglecting the other background probabilities leads to some bias, the calibration procedure described below allows us to correct for these and other limitations of the model.

The leading-order (LO) matrix element for $q\bar{q} \rightarrow \bar{t}t \rightarrow W^+bW^-\bar{b} \rightarrow \ell^+ \nu_\ell \bar{\nu}_\tau \ell^+ \nu_\ell \bar{\nu}_\tau$ is used to compute the $\bar{t}t$ probability density. For each final state $y$ of the six produced partons, the signal probability is given by

$$P_{\bar{t}t}(x; m_t) = \frac{1}{\sigma_{\text{obs}}(m_t)} \sum_{j=1}^{8} \int dq_1 dq_2 f_{\text{PDF}}(q_1)f_{\text{PDF}}(q_2) \times \frac{(2\pi)^4|M(y; m_t)|^2}{q_1 q_2 s} d\Phi_6 W(x, y) W(p_T^2),$$

where $q_1$ and $q_2$ denote the momentum fractions of the incident quarks in the proton and antiproton, respectively, $f_{\text{PDF}}$ are the parton distribution functions (PDF) for finding a parton of a given flavor and longitudinal momentum fraction in the proton or antiproton (in this analysis we use the CTEQ6L1 PDF [19]), $s$ is the square of the energy in the $q\bar{q}$ rest frame, $M(y)$ is the leading-order matrix element [20], and $d\Phi_6$ is an element of the 6-body phase space. Detector resolution is taken into account through a transfer function $W(x, y)$ that describes the probability of the partonic final state $y$ to be measured as $x$. The finite transverse momentum of the $\bar{t}t$ system is accounted for through an integration over its probability distribution, which is derived from parton-level simulated events using ALPGEN [21], employing PYTHIA [22] for parton showers and hadronization. As the angular resolution of the jets and leptons, as well as the electron energy resolution, are sufficiently well determined, there is no need to introduce resolution functions. By taking into account energy and momentum conservation, Eq. (2) can be reduced to an
integration over the energies associated with the $b$ quarks, the lepton-neutrino invariant masses, the differences between neutrino transverse momenta, the transverse momentum of the $t\bar{t}$ system, and the radii of curvature ($p_T$) of muons. The sum runs over both possible jet-parton assignments and over up to two real solutions for each neutrino energy [23]. The normalization factor $\sigma_{\text{obs}}$ is the product of the LO cross section and the mean efficiency of the final selections. A transfer function $W(x, y)$ is used for each jet and each muon in the final state. The jet energy resolution is parametrized as the sum of two Gaussian functions, with parameters depending linearly on parton energies, while the resolution in muon $p_T$ is described by a single Gaussian function. All parameters in $W(x, y)$ are determined from Monte Carlo (MC) $t\bar{t}$ events, tuned to match the resolutions observed in the data.

To take account of all background processes and to provide a correct statistical sampling of possible spin, flavor, and color configurations, the background probability $P_{Z+2\text{jets}}$ is calculated by using Vecbos [24]. Since $Z \rightarrow \tau^+ \tau^-$ decay is not modeled in Vecbos, an additional transfer function in the $e\mu$ channel is used to describe the energy of the final state lepton relative to the initial $\tau$ lepton, derived from parton-level information [23]. The direction of the final state lepton is assumed to be close to that of the $\tau$ lepton, since in only such cases is the lepton from the $\tau$ decay sufficiently energetic to pass the $p_T$ selection. For the $(Z \rightarrow \tau^+ \tau^- \rightarrow e^+\mu^-\bar{\nu}_{e}\bar{\nu}_{\mu})+2\text{jets}$ probability, the energy fractions for final state leptons are sampled according to this $\tau$ transfer function. The jet and charged-lepton directions are assumed to be well-measured, and each kinematic solution is weighted according to the $p_T$ of the $Z+2\text{jets}$ system. The integration of the probability for $Z+2\text{jets}$ is performed over the energies of the two partons that lead to the jets. Both possible assignments of jets to quarks are considered.

To calculate the signal and background probability densities, a MC-based integration of Eq. (2) is performed, and $m_t$ is changed in steps of 2.5 GeV over a range of 30 GeV. For each mass hypothesis, a likelihood function $L_{\text{evt}}(m_t, f_{ij})$ is defined by the product of individual event probabilities $P_{\text{evt}}$, and the signal fraction $f_{ij}$ is determined by minimizing $-\ln L_{\text{evt}}$. Finally, the most likely value of $m_t$ and its uncertainty are extracted from a fit of $L_{\text{evt}}(m_t)$ to a Gaussian form near its maximum by using the value of $f_{ij}$ found in the previous step.

To check for any bias caused by approximations of the method, such as the use of the LO matrix element for $P_{ij}$ or from neglecting backgrounds other than $Z+2\text{jets}$, the measurement is calibrated by using MC events generated with ALPGEN-PYTHIA. All events are processed through a full GEANT3 [25] detector simulation, followed by the same reconstruction and analysis chain as used for the data. Effects from additional $p\bar{p}$ interactions are simulated by overlaying the data from random $p\bar{p}$ crossings over the MC events. Five $t\bar{t}$ MC samples are generated with input top quark masses of $m_t = 165, 170, 172.5, 175,$ and $180$ GeV. Probabilities for the $t\bar{t}$ signal and for $Z/\gamma^* \rightarrow \ell^+\ell^-$, diboson, and instrumental backgrounds are used to form randomly drawn pseudoexperiments. The total number of events in each pseudoexperiment is fixed to the number of events in the data for the combined dilepton channels. The signal and background fractions are fluctuated according to multinomial statistics around the fractions determined from the measured $t\bar{t}$ cross section in the separate channels [26]. The mean values of $m_t$, measured in 1000 pseudoexperiments as a function of the input $m_t$, are shown in Fig. 1(a). The deviation from the ideal response, where the extracted mass is equal to the input mass, is caused both by the presence of backgrounds without a corresponding matrix element in the event probability and by approximations in the calculation of the $Z+2\text{jets}$ probabilities. For the case of background-free pseudoexperiments, no difference is observed. The width of the distribution of the pulls (“pull width”), defined as the mean deviation of $m_t$ in single pseudoexperiments from the mean for all 1000 values at a given input $m_t$, in units of the measured uncertainty per pseudoexperiment, is shown in Fig. 1(b). The statistical uncertainty measured in the data is corrected for the deviation of the pull width from unity. The calibrated value of $m_t$ from the fit to the data is shown in Fig. 2(a). Figure 2(b) compares the measured uncertainty for $m_t$ with the distribution of expected uncertainties in pseudoexperiments at $m_t = 175$ GeV. The difference between the observed and median expected uncertainty is not statistically significant. We also note that, when we change the signal to background ratio within uncertainties, the expected uncertainty generally increases and agrees well with the observation.

Systematic uncertainties on the measurement of $m_t$ can be divided into three categories. The first involves uncertainties from modeling of the detector, such as the uncertainty on the energy scale of light-quark jets and the
uncertainty in the relative calorimeter response to $b$ and light-quark jets, as well as in the energy resolution for jets, muons, and electrons. The second category is related to the modeling of $t\bar{t}$ production. This includes possible differences in the amount of initial and final state radiation, effects from next-to-leading-order contributions and different hadronization models, color reconnection, and modeling of $b$-quark fragmentation as well as uncertainties from the choice of PDF. The third category comprises effects from calibration, such as the uncertainties in the calibration function shown in Fig. 1(a), and from variations in signal and background contributions in the pseudoexperiments. Contributions to the total systematic uncertainty in the measurement of $m_t$ are summarized in Table I.

The dominant systematic uncertainty arises from the different detector response of light and $b$-quark jets. It accounts for the different calorimeter response of single pions in the data and MC simulations and the different fractions of single pions in light and $b$-quark jets. The relative uncertainty of the response has been evaluated to be 1.8% leading to a shift of 1.6 GeV in $m_t$. The next important uncertainty comes from uncertainties in the jet energy scale (JES) of light quarks. This JES is calibrated by using $\gamma +$ jets events [27]. More than 80% of the JES uncertainty is due to the understanding of the detector response and the showering of jets. The total uncertainty typically adds up to about 1.5% per jet, which translates into an uncertainty on $m_t$ of 1.5 GeV. The main uncertainty from modeling $t\bar{t}$ production is from higher-order effects and hadronization. It is evaluated by using $t\bar{t}$ events generated with \textsc{MC@NLO} [28] and evolved in \textsc{HERWIG} [29]. The next leading uncertainty on modeling $t\bar{t}$ arises from the description of $b$-quark fragmentation. It is derived by comparing the extracted $m_t$ for the default measurement with the result using a reweighting of the default MC samples to a Bowler scheme tuned to LEP or SLD data [30]. The largest difference is quoted as the uncertainty.

In summary, we have presented a measurement of the top quark mass in the $t\bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow \ell^+ \nu_\ell b \bar{b} c \bar{c}$ channel using the matrix element method. Based on an integrated luminosity of 5.4 fb$^{-1}$ collected by the D0 Collaboration, the top quark mass is found to be

$$m_t = 174.0 \pm 1.8(\text{stat}) \pm 2.4(\text{syst}) \text{ GeV}. \quad (3)$$

This measurement is in good agreement with the current world average $m_t = 173.3 \pm 1.1 \text{ GeV} [31]$. Its total uncertainty of 3.1 GeV corresponds to a 1.8% accuracy and represents the most precise measurement of $m_t$ from dilepton $t\bar{t}$ final states.

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[13] The pseudorapidity $\eta$ is defined relative to the center of the detector as $\eta = -\ln[\tan(\theta/2)]$, where $\theta$ is the polar angle with respect to the proton beam direction.
[17] Throughout this Letter, charge conjugated processes are included implicitly.