Search for Signatures of Extra Dimensions in the Diphoton Mass Spectrum at the Large Hadron Collider

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Search for Signatures of Extra Dimensions in the Diphon Mass Spectrum at the Large Hadron Collider

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A search for signatures of extra spatial dimensions in the diphon invariant-mass spectrum has been performed with the CMS detector at the LHC. No excess of events above the standard model expectation is observed using a data sample collected in proton-proton collisions at $\sqrt{s} = 7$ TeV corresponding to an integrated luminosity of 2.2 fb$^{-1}$. In the context of the large-extra-dimensions model, lower limits are set on the effective Planck scale in the range of 2.3–3.8 TeV at the 95% confidence level. These limits are the most restrictive bounds on virtual-graviton exchange to date. The most restrictive lower limits to date are also set on the mass of the first graviton excitation in the Randall-Sundrum model in the range of 0.86–1.84 TeV, for values of the associated coupling parameter between 0.01 and 0.10.

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Over a decade ago, Arkani-Hamed, Dimopoulos, and Dvali (ADD) [1,2] proposed that extra spatial dimensions could potentially solve the standard model (SM) hierarchy problem [3], which consists of the observation of the unnatural difference of scales between the gravitational and electroweak theories. They proposed a scenario whereby the SM is constrained to the common $3 + 1$ space-time dimensions (brane), while gravity is free to propagate throughout a larger multidimensional space (bulk). The gravitational flux on the brane is therefore diluted by virtue of Gauss’s law in the bulk, which relates the fundamental Planck scale to the apparent reduced scale $M_D$ to the apparent reduced scale $M_{\text{Pl}} = 2 \times 10^{18}$ GeV according to the formula $M_D^{1/2} = M_{\text{Pl}}/(re)$, where $r$ and $n_{\text{ED}}$ are the size and number of the extra dimensions (ED), respectively. Postulating a fundamental Planck scale to be on the order of the electroweak symmetry breaking scale ($\sim 1$ TeV) results in ED with $r < 1$ mm for $n_{\text{ED}} \gtrsim 2$.

Another model of ED that solves the hierarchy problem was proposed by Randall and Sundrum (RS) [4]. In this model, the observed hierarchy is related instead to the warped anti–de Sitter (AdS) geometry of the ED. We specifically consider the RS1 model whereby only one finite ED exists separating two branes, one at each end of the ED. The geometry of the bulk is based on a slice of a five-dimensional AdS space with a length $\pi r_c$, where $r_c$ is the compactification radius. The full metric is given by $ds^2 = e^{-kr_c^2} \eta_{\mu\nu} dx^\mu dx^\nu - r_c^2 dy^2$, where Greek indices run over four-dimensional space-time, $\eta_{\mu\nu}$ is the Minkowski metric tensor, and $0 \leq y \leq \pi$ is the coordinate along the single ED of radius $r_c$. The value of $k$ specifies the curvature scale (or “warp factor”) and relates the fundamental Planck scale on one brane to the apparent scale on the other by $\Lambda_{\pi} = M_{\text{Pl}}e^{-kr_c^2}$. As a consequence, a value of $kr_c \sim 10$ would provide a natural solution to the hierarchy problem, yielding $\Lambda_{\pi} \sim 1$ TeV.

Phenomenologically, the excited gravitons in both models preferentially decay into two gauge bosons, such as photons, rather than into two leptons, because the graviton has spin 2, and so fermions cannot be produced in an s wave. In the RS scenario, gravitons appear as well-separated Kaluza-Klein (KK) excitations with masses and widths determined by the parameters of the RS1 model. One convenient choice of parametrization is the mass $M_1$ of the first excitation of the graviton and the dimensionless warp factor $k = k/M_{\text{Pl}}$, which defines the strength of associated coupling to the SM fields. Precision electroweak data constrain $k \gtrsim 0.01$, while perturbativity requirements limit $k \lesssim 0.10$ [5].

In the ADD model, the wave function of the KK gravitons must satisfy periodic boundary conditions, resulting in discrete energy levels with modal spacing of the order of the inverse ED size, from 1 to 100 meV, much smaller than the spacing in the RS1 model, which is expected to be of the order of 1 TeV. This effect produces an apparent continuum spectrum of diphotons, rather than distinct resonances, at high ($\sim 1$ TeV) diphoton invariant mass $M_{\gamma\gamma}$.

Summing over all KK modes in the ADD scenario results in a divergence in the cross section, so an ultraviolet (UV) cutoff scale $M_S$ is imposed. This effective Planck scale is related to—but potentially different from—the fundamental Planck scale $M_D$. The precise relationship depends on the UV completion of the effective theory. The effects of virtual-graviton production on the differential diphoton cross section are parametrized by the single

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variable $\eta_{\gamma} = F/M_{\gamma}^4$, where $F$ is an order-unity dimensionless parameter, for which several conventions exist [6]. In this Letter, we set lower limits on $M_{\gamma}$ in three different conventions: GRW [7], Hewett [8], and HLZ [9].

Searches for ED via virtual-graviton effects in the ADD model have been conducted at HERA, LEP, the Tevatron, and the LHC [10,11]. The most stringent previously published limits on $M_{\gamma}$ for $n_{\text{ED}} = 2$ come from the previous measurement in the diphoton channel at the Compact Muon Solenoid (CMS) experiment [6]. For $n_{\text{ED}} = 2$, measurements by the D0 experiment in the dijet [12] and diphoton + dielectron [13] channels are more restrictive. The most sensitive previous search for RS gravitons was conducted by the ATLAS experiment [14]. They used a search in the dilepton final state to exclude $M_{\gamma} < 1.63$ TeV for $\kappa = 0.10$.

In this Letter, we present a search for both nonresonant and resonant diphoton production, in the ADD and RS1 models, respectively. We use data corresponding to an integrated luminosity of 2.2 fb$^{-1}$, collected in $pp$ collisions at $\sqrt{s} = 7$ TeV at the LHC with the CMS detector between March and August 2011.

The CMS detector [15] is designed to study collisions at the LHC. An all-silicon tracker, an electromagnetic calorimeter (ECAL), and a hadronic sampling calorimeter are all contained within a large-bore 3.8 T superconducting solenoid. In the central region, the tracker consists of three radial layers of silicon pixel detectors followed radially by silicon strip detectors. The finely segmented ECAL has a radial layers of silicon pixel detectors followed radially by silicon strip detectors. The finely segmented ECAL has a radial layers of silicon pixel detectors followed radially by silicon strip detectors. The finely segmented ECAL has a radial layers of silicon pixel detectors followed radially by silicon strip detectors. The finely segmented ECAL has a radial layers of silicon pixel detectors followed radially by silicon strip detectors. The finely segmented ECAL has a radial layers of silicon pixel detectors followed radially by silicon strip detectors.

Events for the analysis were collected through a diphoton trigger, where each photon was required to have a transverse energy $E_T > 60$ GeV, depending on the instantaneous luminosity. We require that an event be consistent with a $pp$ collision and have at least one well-reconstructed primary vertex [17]. We then reconstruct photons with $E_T > 70$ GeV in the ECAL barrel by clustering electromagnetic energy deposits. Electrons that do not originate from photon conversions are suppressed by using information from the pixel detector to associate tracks and ECAL clusters compatible with an electron hypothesis. The probability of misidentification of an electron as a photon is approximately 3%, resulting in a negligibly small contribution to the diphoton spectrum in the signal region.

Hadronic jets can be misidentified as photons when their leading hadron is an energetic $p^0$ or $\eta$ meson. We reduce the misidentification rate from this source by placing the same restrictions on the isolation as in the previous analysis for this channel [6]. These restrictions limit the total transverse energy because of tracks and calorimeter depositions near the photon cluster. Restrictions on the shower-shape variable $\sigma_{\eta\gamma}$, which is a modified second moment of the electromagnetic energy cluster about its mean $\eta$ position [18], also suppress hadronic misidentification. Topological and timing criteria suppress anomalous signals present in the ECAL [19]. Diphoton events are selected in which $M_{\gamma\gamma} > 140$ GeV.

The photon reconstruction and identification efficiency is determined in Monte Carlo (MC) simulation and corrected using a data-to-MC scale factor of $1.005 \pm 0.034$ derived from studying $Z \rightarrow e^+ e^-$ events. The measured efficiency for a single $E_T > 70$ GeV photon with $|\eta| < 1.44$ is ($87.4 \pm 5.4$)% and depends only weakly on the $E_T$ and $\eta$ of the photon, and the number of extra collisions present in the event. The systematic uncertainty bounds the variation as a function of these variables, the most significant of which is the number of extra collisions. We reweight the simulation to give the same reconstructed primary-vertex distribution (on average 6–8 vertices) as observed in the data. We determine the corresponding diphoton reconstruction and identification efficiency ($76.4 \pm 9.6$)% by squaring the single-photon efficiency.

The simulation of ED in the ADD model is performed using version 1.3.0 of the SHERPA [20] MC generator. The simulation includes both SM diphoton production and signal diphoton production via virtual-graviton exchange in order to account for the interference effects between the SM and ADD processes. The leading-order (LO) SHERPA cross sections are multiplied by a constant next-to-leading-order (NLO) $K$ factor of $1.6 \pm 0.1$, a value that represents an updated calculation for $\sqrt{s} = 7$ TeV by the authors of Refs. [21,22]. The systematic uncertainty on the signal $K$ factor reflects the approximate variation of the $K$ factor over a large region of the model parameters; it is not intended to account for the theoretical uncertainty. The cross sections in the simulation are conservatively set to zero for $\sqrt{s} > M_{\gamma}$ because the theory becomes nonperturbative for larger values of $\sqrt{s}$. Introducing this sharp truncation reduces the upper limits on $M_{\gamma}$ by a few percent.

The simulation of RS-graviton production is performed using version 6.424 of the PYTHIA [23] MC program. The signal cross section is scaled by a mass-dependent NLO $K$ factor [21,22], which ranges from 1.6 to 1.8 as a function of $M_{\gamma\gamma}$ and for different values of $\kappa$. The CTEQ6L1 [24] parton distribution functions (PDF) are used in the simulation of both the ADD and RS models, and a 1.5% relative uncertainty on the signal acceptance is included by measuring its dependence on the choice of PDF and its uncertainties.
Optimization of the event selection is done separately for both ADD and RS scenarios. The signal in both cases is predominantly at central values of $\eta$, while the high-$M_{\gamma\gamma}$ SM background dominates the signal in the forward region; therefore, we restrict ourselves to photons located in the ECAL barrel only. In the ADD scenario, we find that the optimal region for the search, based on the expected signal significance, is $M_{\gamma\gamma} > 900$ GeV. This choice of selection depends weakly on the model parameters.

In the search for RS gravitons, a fixed window is selected about the $M_1$ mass point of interest. Because the signal shapes deviate from Gaussian distributions, we define an effective measure of the signal width $\sigma_{\text{eff}}$ as the half-width of the narrowest mass interval containing 68% of the signal from simulation. The value of $\sigma_{\text{eff}}$ ranges from 6 to 21 GeV for RS gravitons with $M_1$ between 500 and 2000 GeV and $\bar{k} = 0.01$. The dependence on $M_1$ is linear and also increases with $\bar{k}$ ($\sigma_{\text{eff}} = 42$ GeV for $M_1 = 2$ TeV and $\bar{k} = 0.10$). A window is then formed about the resonance mean of size $\pm 5\sigma_{\text{eff}}$ in the data. This window contains 96%–97% of the signal acceptance for all mass points considered in this analysis, and the detector resolution is negligible with respect to the window size. This choice of the window maximizes the signal acceptance and analysis sensitivity in the case of small backgrounds.

Backgrounds from the misidentification of a hadronic jet as a photon are small in the signal region but contribute to the low-$M_{\gamma\gamma}$ region. Two such sources of backgrounds from isolated-photon misidentification are considered: multijet production and prompt single-photon ($\gamma + \text{jet}$) production. In particular, we measure on a background-dominated sample a misidentification rate, defined as the ratio of the number of isolated photon candidates to non-isolated photonlike objects. These photonlike objects are reconstructed as photons but fail one of the isolation or shower-shape criteria; therefore, the samples corresponding to numerator and denominator are mutually exclusive, and prompt photons have a negligibly small contribution to the denominator. The misidentification rate is measured in a photon-triggered sample in bins of photon(like) candidate $E_T$, but the objects used in the measurement are required to be well separated from the triggered object to avoid a trigger-induced bias.

Because the background-dominated sample in which we measure the misidentification rate may contain some genuine, isolated photons that “contaminate” the numerator of the misidentification rate, we correct for this on a bin-by-bin basis. The $\sigma_{\gamma\eta}$ requirement is released and the numerator sample is fit for the fraction of prompt photons using one-dimensional probability density histograms (“templates”) in $\sigma_{\gamma\eta}$. The signal template is constructed from MC simulation, and the background template is constructed from reconstructed photons that fail one or more of the isolation criteria. The measured misidentification rate falls from 7% at $E_T = 70$ GeV and $|\eta| < 1.44$. The shaded band around the background estimation corresponds to the average systematic uncertainty over the spectrum. The precise per-bin uncertainty is not provided for the sake of clarity. The last bin includes the sum of all contributions for $M_{\gamma\gamma} > 2.0$ TeV. The simulated distributions for two, nonexcluded signal hypotheses are shown for comparison as dotted (ADD) and dashed (RS) lines.

<table>
<thead>
<tr>
<th>Process</th>
<th>Diph. invariant-mass range [TeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>[0.14, 0.2]</td>
</tr>
<tr>
<td>Multijet</td>
<td>15 ± 6</td>
</tr>
<tr>
<td>$\gamma + \text{jet}$</td>
<td>102 ± 15</td>
</tr>
<tr>
<td>Diphoton</td>
<td>372 ± 70</td>
</tr>
<tr>
<td>Backgrounds</td>
<td>489 ± 73</td>
</tr>
<tr>
<td>Observed</td>
<td>484</td>
</tr>
</tbody>
</table>

FIG. 1 (color online). Observed event yields (points with error bars) and background expectations (filled solid histograms) as a function of the diphoton invariant mass. Photons are required to be isolated, with $E_T > 70$ GeV and $|\eta| < 1.44$. The shaded band around the background estimation corresponds to the average systematic uncertainty over the spectrum. The precise per-bin uncertainty is not provided for the sake of clarity. The last bin includes the sum of all contributions for $M_{\gamma\gamma} > 2.0$ TeV. The simulated distributions for two, nonexcluded signal hypotheses are shown for comparison as dotted (ADD) and dashed (RS) lines.
The multijet and $\gamma+$ jet backgrounds to the reconstructed diphoton spectrum are estimated by using the misidentification rate to extrapolate from two background-dominated reference regions, both selected with the same diphoton trigger as the primary signal sample. One region includes events with only one isolated photon, but one or more nonisolated photons. The other region includes events with no isolated photons, but two or more nonisolated photons. The diphoton trigger is sufficiently inclusive that the regions are unaffected by the trigger selection. By applying the prompt-photon misidentification rate to these two reference regions, we predict the $\gamma+\text{jet}$ and multijet backgrounds in the signal region.

The SM diphoton background dominates the signal region. The expected number of background events due to this process is computed by rescaling the prediction from PYTHIA with a NLO $K$ factor that varies with $M_{\gamma\gamma}$. The NLO prediction is calculated with the DIPHOX+GAMMA2MC [25,26] generators, which take into account the fragmentation processes in which the photons can come from the collinear fragmentations of hard partons. A separate analysis by CMS has also demonstrated good agreement with the NLO prediction at low $M_{\gamma\gamma} \leq 300$ GeV [27]. The subleading-order gluon-fusion box diagram is included as a part of the PYTHIA calculation because of its large contribution at the LHC energy, although its effects are small at high $M_{\gamma\gamma}$. The $K$ factor varies between 1.7 and 1.1 from low to high $M_{\gamma\gamma}$. A systematic uncertainty of 15% on the value of the $K$ factor is determined by examining the PDF uncertainties and variation of the renormalization and factorization scales.

Figure 1 shows the invariant-mass distribution of the selected events, together with the estimated distributions for each of the backgrounds. Table I presents the observed number of events in the data and the predicted number of events, neither resonant nor nonresonant.

To set limits on virtual-graviton exchange in the ADD scenario, we compare the number of observed and expected events in the signal region ($M_{\gamma\gamma} > 0.9$ TeV) and set 95% confidence level (C.L.) upper limits on the quantity $S = (\sigma_{\text{total}} - \sigma_{\text{SM}}) \times B \times A$, where $\sigma_{\text{total}}$ represents the total diphoton production cross section (including signal, SM, and interference effects), and $\sigma_{\text{SM}}$ represents the SM diphoton background.

### Table II

The 95% C.L. lower limits on $M_5$ (in TeV) in the GRW, Hewett, and HLZ conventions for two values of the ADD signal $K$ factor, 1.0 and $1.6 \pm 0.1$. All limits are computed with a signal cross section truncated to zero for $\sqrt{s} > M_5$, where $\sqrt{s}$ is the center-of-mass of the partonic collision. The limits are presented for both positive and negative interference in the Hewett convention and for $n_{\text{ED}} = 2$–7 in the HLZ convention. The median expected lower limits are given in parentheses.

<table>
<thead>
<tr>
<th>$K$</th>
<th>GRW Positive</th>
<th>GRW Negative</th>
<th>Hewett $n_{\text{ED}} = 2$</th>
<th>Hewett $n_{\text{ED}} = 3$</th>
<th>Hewett $n_{\text{ED}} = 4$</th>
<th>Hewett $n_{\text{ED}} = 5$</th>
<th>Hewett $n_{\text{ED}} = 6$</th>
<th>Hewett $n_{\text{ED}} = 7$</th>
<th>HLZ $n_{\text{ED}} = 2$</th>
<th>HLZ $n_{\text{ED}} = 3$</th>
<th>HLZ $n_{\text{ED}} = 4$</th>
<th>HLZ $n_{\text{ED}} = 5$</th>
<th>HLZ $n_{\text{ED}} = 6$</th>
<th>HLZ $n_{\text{ED}} = 7$</th>
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<tbody>
<tr>
<td>1.0</td>
<td>2.94</td>
<td>2.63</td>
<td>2.28</td>
<td>3.29</td>
<td>3.50</td>
<td>2.94</td>
<td>2.66</td>
<td>2.47</td>
<td>2.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(2.99)</td>
<td>(2.67)</td>
<td>(2.31)</td>
<td>(3.37)</td>
<td>(3.56)</td>
<td>(2.99)</td>
<td>(2.71)</td>
<td>(2.52)</td>
<td>(2.38)</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>1.6 ± 0.1</td>
<td>3.18</td>
<td>2.84</td>
<td>2.41</td>
<td>3.68</td>
<td>3.79</td>
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<td></td>
<td>(3.24)</td>
<td>(2.90)</td>
<td>(2.44)</td>
<td>(3.77)</td>
<td>(3.85)</td>
<td>(3.24)</td>
<td>(2.93)</td>
<td>(2.73)</td>
<td>(2.58)</td>
<td></td>
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</table>
the SM diphoton production cross section. The signal branching fraction to diphotons is indicated by $\mathcal{B}$ and the signal acceptance by $A$. We use the CL$_{S}$ technique [28,29] to compute the limits with a likelihood constructed from the Poisson probability to observe $N$ events, given $S$, the signal efficiency ($76.4 \pm 9.6\%$), the expected number of background events ($1.5 \pm 0.3$), and the integrated luminosity $L = (2.2 \pm 0.1) \text{ fb}^{-1}$ [16]. The variation of the $K$ factor is included in the statistical analysis as an uncertainty on the signal yield.

The observed (median expected) 95% C.L. upper limit on $S$ is 3.0 fb (2.7 fb). For the HLZ $n_{BD} = 2$ case, we parametrize $S$ directly as a smooth function of $1/M_{S}^{2}$. For all other conventions, $S$ is parametrized as a function of the parameter $\eta_{G}$, as in Ref. [6]. The observed 95% C.L. limit, together with the signal parametrization, is shown in Fig. 2. The intersection of the cross-section limit with the parametrized curve determines the 95% C.L. upper limit on the parameter $\eta_{G}$. As seen from the plot, these upper limits on $S$ correspond to upper limits of $\eta_{G} \leq 0.0097$ TeV$^{-4}$ and $1/M_{S}^{4} \leq 0.0055$ TeV$^{-4}$. The upper limits on $\eta_{G}$ are equated to lower limits on $M_{S}$ and are shown in Table II.

For the RS scenario, the same limit-setting calculation is performed, but in a bounded window in $M_{\gamma\gamma}$. Figure 3 shows the excluded regions in the $M_{1}$-$\tilde{k}$ plane. Also shown are bounds due to electroweak constraints and naturalness ($\Lambda_{\chi} > 10$ TeV). Perturbativity requirements bound $\tilde{k} \leq 0.10$.

In summary, we have performed a search for extra spatial dimensions leading to enhanced resonant or nonresonant diphoton production in proton-proton collisions at a center-of-mass energy of 7 TeV at the LHC. Using a data sample corresponding to an integrated luminosity of 2.2 fb$^{-1}$ recorded by the CMS experiment, we observe no excess in diphoton production above the rate predicted from SM background sources. Values of the effective Planck scale $M_{S}$ less than 2.3–3.8 TeV are excluded at 95% C.L. for ADD models. We also exclude at 95% C.L. resonant graviton production in the RS1 model with values of $M_{1}$ less than 0.86–1.84 TeV depending on the normalized coupling strength $\tilde{k}$. We present limits on both the ADD and RS1 models of extra dimensions in the diphoton final state that extend those observed at the D0 experiment [13], as well as those set previously by the CMS [6] and ATLAS [14] experiments.

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Table III. The 95% C.L. lower limits on $M_{1}$ for given values of the coupling parameter $\tilde{k}$. For $\tilde{k} < 0.03$, masses above the presented limits are excluded by electroweak and naturalness constraints. The median expected lower limits are numerically the same for the presented precision except for the $\tilde{k} = 0.01$ case, for which the expected lower limit on $M_{1}$ is 0.84 TeV.

<table>
<thead>
<tr>
<th>$\tilde{k}$</th>
<th>0.01</th>
<th>0.02</th>
<th>0.03</th>
<th>0.04</th>
<th>0.05</th>
<th>0.06</th>
<th>0.07</th>
<th>0.08</th>
<th>0.09</th>
<th>0.10</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M_{1}$ [TeV]</td>
<td>0.86</td>
<td>1.13</td>
<td>1.27</td>
<td>1.39</td>
<td>1.50</td>
<td>1.59</td>
<td>1.67</td>
<td>1.74</td>
<td>1.80</td>
<td>1.84</td>
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Also at University of Visva-Bharati, Santiniketan, India.
1Also at Sharif University of Technology, Tehran, Iran.
2Also at Isfahan University of Technology, Isfahan, Iran.
3Also at Shiraz University, Shiraz, Iran.
4Also at Plasma Physics Research Center, Science and Research Branch, Islamic Azad University, Teheran, Iran.
5Also at Facoltà Ingegneria Università di Roma, Roma, Italy.
6Also at Università della Basilicata, Potenza, Italy.
7Also at Laboratori Nazionali di Legnaro dell’ INFN, Legnaro, Italy.
8Also at Università degli studi di Siena, Siena, Italy.
9Also at Faculty of Physics of University of Belgrade, Belgrade, Serbia.
10Also at University of California, Los Angeles, Los Angeles, California, USA.
11Also at University of Florida, Gainesville, Florida, USA.
12Also at Scuola Normale e Sezione dell’ INFN, Pisa, Italy.
13Also at INFN Sezione di Roma, Università di Roma “La Sapienza,” Roma, Italy.
14Also at University of Athens, Athens, Greece.
15Also at Rutherford Appleton Laboratory, Didcot, United Kingdom.
16Also at The University of Kansas, Lawrence, Kansas, USA.
17Also at University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia.
18Also at Paul Scherrer Institut, Villigen, Switzerland.
19Also at Institute for Theoretical and Experimental Physics, Moscow, Russia.
20Also at Gaziosmanpasa University, Tokat, Turkey.
21Also at Adiyaman University, Adiyaman, Turkey.
22Also at The University of Iowa, Iowa City, Iowa, USA.
23Also at Mersin University, Mersin, Turkey.
24Also at Kafkas University, Kars, Turkey.
25Also at Suleyman Demirel University, Isparta, Turkey.
26Also at Ege University, Izmir, Turkey.
27Also at School of Physics and Astronomy, University of Southampton, Southampton, United Kingdom.
28Also at INFN Sezione di Perugia, Università di Perugia, Perugia, Italy.
29Also at Utah Valley University, Orem, Utah, USA.
30Also at Institute for Nuclear Research, Moscow, Russia.
31Also at Los Alamos National Laboratory, Los Alamos, New Mexico, USA.
32Also at Erzincan University, Erzincan, Turkey.
33Also at Kyungpook National University, Daegu, Korea.