Vadose zone lag time and potential 21st century climate change effects on spatially distributed groundwater recharge in the semi-arid Nebraska Sand Hills

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1. Introduction

Climate-related variables such as the spatial distribution and intensity of precipitation ($P$) and evapotranspiration ($ET$) control soil water content in the vadose zone, the region between the land surface and saturated zone through which groundwater recharge ($GR$) can occur (Green et al., 2011). Groundwater systems in semi-arid and arid environments are especially sensitive to climate change because of the strong dependence of $ET$ rates on temperature, and shifts in the precipitation regime affecting $GR$ (Toews and Allen, 2009). Long-term changes in climate and land use have substantially affected $GR$ rates in many regions of the world (Scanlon et al., 2006). While impacts to $GR$ caused by land use changes are generally well...
understood (e.g., Cook et al., 2003; Scanlon et al., 2007), those caused by future climate change remain less certain. Thus, interest in this topic has increased greatly over recent years (e.g., Crosbie et al., 2013; Ferguson and Maxwell, 2012; Green et al., 2011; Gurdak et al., 2007).

Among the various hydrologic cycle components, GR is the leading variable determining groundwater resources availability and sustainability in semi-arid and arid environments (Crosbie et al., 2013; Szilagyi et al., 2011b). Of practical importance to groundwater modeling and water resource management are the effects of projected changes in potential groundwater recharge (GR) rates (deep drainage beneath the root zone) on multi-decadal to century time scales, because regions with deep water tables and/or experiencing low GR rates with fine-textured soils can have vadose zone lag times that exceed a century (McMahon et al., 2006; Scanlon et al., 2010). Thus, climate changes occurring within the 21st century (the period for which climate change projections are commonly made) may not affect groundwater resources within the same time frame, and steady actual groundwater recharge (GR) rates (flux across the water table) will remain unchanged.

Even when estimates of GR rates have a sound foundation, these studies often do not account for the role that the vadose zone has in delaying the arrival of draining soil water before reaching the water table. This is especially the case for past applications of regional groundwater flow models in the western United States (Rossman and Zlotnik, 2013). Moreover, GR rates, when estimated as deep drainage (i.e., GR) are only accurate in time under steady-state climatic conditions, or when depth to groundwater is relatively small (less than ~5 m; Kollet and Maxwell, 2008). Otherwise, estimates of GR should not be regarded as GR. Therefore, in determining GR rates one must make a proper adjustment for the lag time of soil moisture traversing the vadose zone. This is in contrast to many previous studies focusing on water quality issues, and thus on solute movement in the vadose zone (e.g., McMahon et al., 2006; Schwartz, 2006; Sousa et al., 2013).

In order to determine the lag time of soil moisture (rather than solutes), some studies perform numerical simulations of vadose zone processes on regional or basin scales by solving the nonlinear 3D Richards equation and resorting to parallel supercomputing to reduce model execution times (e.g., Kollet and Maxwell, 2008; Kollet et al., 2010). Long model execution times may lead to complications during model calibration and sensitivity analysis (Brunner et al., 2012; Hill, 2006). A simplified treatment of flow dynamics in the vadose zone involves reducing the Richards equation to 1D format and neglecting soil moisture diffusivity, i.e., gravity-driven kinematic wave approach. Implementations include the MODFLOW Unsaturated-Zone Flow (UZF1) Package (Niswonger et al., 2006) and an option in MikeShe (Graham and Butts, 2005).

Recent multi-model assessments of climate change impacts call for increased accuracy of water resource predictions through improved hydrological model development (e.g., Allen et al., 2010; Schewe et al., 2013). However, complexity of the unsaturated flow models must be consistent with the ability to measure or estimate GR rates and vadose zone hydraulic parameters. The saturated hydraulic conductivity, the most important of the various hydraulic parameters (Stephens, 1995), can vary by orders of magnitude depending on geologic heterogeneity. Grismer (2013) states, "determination of GR rates and lag times to groundwater supplies at depth remains an iterative process that includes model and estimate refinement as additional information is developed." In fact, a very small number of regional-scale hydrological modeling studies that include the vadose zone have attempted to match soil pressure heads or water contents during calibration, and constraints from these measurements do not result in uniqueness of parameter values (Brunner et al., 2012). Additionally, in an evaluation of the source of uncertainties in future GR estimates in Australia, Crosbie et al. (2011) found that the choice of hydrological model is the source of the least uncertainty when compared against uncertainties due to choice of Global Climate Model (GCM) and downscaling method.

The simplified approach to modeling the vertical movement of moisture through the vadose zone has been investigated by Philip, 1957, Warrick et al., 1971, Wilson, 1974, Sisson et al., 1980, Wilson and Gelhar, 1981, Smith, 1983 and Rasmussen, 2001, and Cook et al. (2003), among others. In contrast to tracer-based advective velocity, these studies calculate lag times using the velocity of the capillary pressure wave response due to a small perturbation of hydrologic conditions in a uniformly wetted soil profile. Following this type of approach, we investigate the hydrological effects of changing 21st century climate (as the difference between P and ET) and vadose zone thickness on vadose zone velocity and lag time and the associated timing of changes to GR at the water table. In this way, we address the desired high resolution, large scale (>10^3 km^2) simulation of soil moisture movement without resorting to parallel supercomputing, commonly involved in variably-saturated 3D numerical modeling of basin hydrology. We utilize published, spatially distributed, high accuracy and high resolution (1.1-km) estimates of GR rates based on long-term (10 yr) MODerate resolution Imaging Spectroradiometer (MODIS) satellite measurements, rather than upscaled results of point-scale vadose zone modeling as done in previous studies (e.g., Allen et al., 2010; Crosbie et al., 2010; Crosbie et al., 2013).

In this article, we propose a simple approach for estimating spatially distributed vadose zone lag times associated with long-term averaged (decadal) climate conditions over large areas. We demonstrate an application of the approach where the aim is to answer the following four related research questions about vadose zone hydrology with regard to the Nebraska Sand Hills: (1) What is the effect of a heterogeneous vadose zone thickness on the spatial distribution of vadose zone lag times? (2) How does soil hydraulic parameter uncertainty affect vertical velocity and vadose zone lag time estimates? (3) How are 21st century climate change projections expected to impact GR rates and vadose zone lag times? and (4) What is the percentage of surface area expected to experience changes in GR rates over time scales of 10, 50 and 100 years, typical of water planning and future climate modeling time scales?

2. Study area

The Nebraska Sand Hills (NSH; Figure 1) is the largest dune region in the Western Hemisphere, with an area of ~50,000 km^2 (Loope and Swinehart, 2000). The region is characterized by a repeating pattern of native grass-stabilized sand dunes adjacent to lakes and wetlands in interdunal valleys, with a highly variable surface topography and vadose zone thickness (Bleed and Flowerday, 1998), causing lag effects to be extremely important in considerations of the spatio-temporal analysis of GR (Figure 2). Diffuse GR within dunes supplies the groundwater system with water that eventually discharges to rivers and more than 1500 perennial lakes (Rundquist, 1983) in hydraulic connection with the unconfined aquifer system (Chen et al., 2003). Most of the lakes are considered to be groundwater sinks because ET exceeds P and a net groundwater influx makes up for the difference (Chen and Chen, 2004; Zlotnik et al., 2010). Lake and wetland areal density is the highest in the western part of the NSH where significant natural drainage features or river valleys are absent (Figure 1 and Figure 3). This was caused by the mobilization of sand dunes causing paleovalleys to dam during several prolonged drought periods in the Holocene (Loope et al., 1995).
Dunes in the NSH are composed of eolian sand that is well-sorted, and fine-to-medium grained (Sweeney and Loope, 2001). Thus, soils in the region have sand content close to 100% in some locations (NRCS (Natural Resources Conservation Service), 2006 and Strassberg et al., 2009). Due to the high hydraulic conductivity of the sandy soils and limited precipitation in the semi-arid environment (450 mm/yr in the western-most part to 650 mm/yr in the eastern-most part), infiltration rates are high and overland flow is minimal (Bleed and Flowerday, 1998; Szilagyi et al., 2003). In the NSH, Holocene sand deposits overlie up to 300 m of Quaternary and/or Pliocene alluvial sand and silt (Wang et al., 2009) and coarse clastic sediments of the Miocene Ogallala Group, that all-together make up the thickest part of the High Plains aquifer (Loope et al., 1995). The High Plains aquifer is considered a vital source of water for irrigated agriculture in the central United States, leading the NSH to be regarded as one of its most important GR areas (Szilagyi et al., 2011b).

Groundwater recharge rates in the NSH can be large and have been estimated to be greater than 200 mm/yr in some locations (Szilagyi et al., 2011b). These high rates of GR, along with a large groundwater reservoir (High Plains aquifer), make the region economically as well as ecologically valuable, supplying water to major rivers, thousands of groundwater fed lakes and wetlands, and sub-irrigating meadows—responsible for a third of Nebraska’s beef cattle industry (Gosselin et al., 2000). The region is unique ecologically for its relatively natural state and biodiversity (Harvey et al., 2007), as most of the region is either undeveloped or used only for grazing livestock (Peterson et al., 2008). If GR were to be reduced because of extended and/or severe drought, as has happened in the geologic past (Loope et al., 1995; Mason et al., 2004; Schmieder et al., 2011), the water table would be lowered and discharge to lakes and rivers would be significantly decreased (Chen and Chen, 2004), threatening the existence of the region’s unique and valuable ecosystems and much of its economic value.

3. Methods

3.1. Vadose zone thickness

Calculating vadose zone lag time requires estimates of the thickness of the vadose zone, or depth to the water table ($D_{wt}$). The vadose zone thickness was estimated as a difference between land surface and water table elevations with consideration of surface water bodies.

A map of $D_{wt}$ was created using ArcGIS™ as the difference in elevations from a 30-m digital elevation model (DEM) of land surface topography (USGS, 1999) and a regional water table map generated in this study. The water table map was converted into a continuous field using a spline interpolation of vertices from 1995 digital water table contours (Summerside et al., 2001) and an appended point layer of lakes and rivers (USGS, 2010) with elevations extracted from the DEM of land surface topography. A conditional statement was used...
to make all negative values in the resulting dataset equal to zero (since negative vadose zone thickness cannot physically exist). Then the 30-m resolution dataset of $D_{\text{adv}}$ was aggregated to 120-m (using the ArcGIS™ spatial join by location tool with mean values) in order to reduce the total number of data points, making calculations possible during the next step in the analysis in which vadose zone thickness within each 1.1-km pixel of MODIS-derived (2000–2009) potential GR rates ($GR_{p,\text{MODIS}}$) is required, allowing for the estimation of spatially distributed vadose zone lag times (described in Sections 3.2 and 3.3). Mean $D_{\text{adv}}$ (120-m aggregated) within each $GR_{p,\text{MODIS}}$ pixel was utilized in calculations of vadose zone lag times. Descriptive statistics (mean, min., max., count (N), standard deviation ($\sigma$)) of the $D_{\text{adv}}$ variable within each $GR_{p,\text{MODIS}}$ pixel (81–100 $D_{\text{adv}}$ values each) were also calculated to quantify the variability of $D_{\text{adv}}$ estimates.

Depth to the water table within each 1.1-km pixel differs from the mean value due to the variability of the terrain and water table. In general, spatial variability of the water table is smaller than for the land surface elevations, and it is assessed on the order $\pm 1$ m since it was created using accurate land-based surveys and data interpolated and published by Summerside et al. (2001). However, the water table variability within a 1.1-km pixel may reach values similar to the variations in the land surface elevations near lakes in the western Sand Hills (Ong, 2010). We assessed the variability of $D_{\text{adv}}$ within $GR_{p,\text{MODIS}}$ pixels by calculating the spatial average standard deviation of $D_{\text{adv}}$ across the entire NSH (40,291 pixels), it is $\pm 8$ m. One should note that the measurement error (vertical error) for land surface topography for each 30-m DEM pixel can reach $\pm 5$ m Holmes et al. (2000). Considering the large height of dunes in the NSH (up to 152 m), the range of variability associated with averaged $D_{\text{adv}}$ over 1.1-km pixels for representation of the vadose zone thickness in this area is reasonable and of adequate accuracy for this study.

Values of $D_{\text{adv}}$ were assumed to remain the same over the entire period of study (2000–2099). This assumption has the potential to add relatively small errors to estimates of vadose zone lag time since a changing climate will likely lead to changes in the configuration and elevation of the water table. However, regional water table elevations have not changed significantly in the NSH for at least the past 60 years (the entire historic observational record), from 1950 to 2009 (McGuire, 2011), and any future changes are likely to compare in magnitude with the uncertainties in the datasets used to derive $D_{\text{adv}}$ and are likely to be much smaller than the average thickness of the vadose zone.

3.2. Estimating potential groundwater recharge rates

3.2.1. Modern period

Here we use previously published (Szilagyi and Jozsa, 2013) remote sensing-based, spatially distributed and high resolution (1.1-km) estimates of $GR_p$ rates for the modern period (2000–2009). These potential $GR_p$ rates ($GR_{p,\text{MODIS}}$) are estimated as the difference between mean $P$ (PRISM Climate Group, 2012) and MODIS-based $ET$ (Figure 4), by taking advantage of the fact that overland flow is minimal in the NSH. A water balance approach is used, which states $P-ET$ is equal to the change in water storage at the zero-flux plane (Healy, 2010), consistent with the approach applied by Munch et al. (2013). In this approach, monthly $GR_{p,\text{MODIS}}$ fluxes are averaged over a suitably long 10-yr period, making total subsurface storage changes negligible (i.e., steady-state). The technique uses basic climate data, including $P$, air temperature, humidity, global radiation, and MODIS-based monthly aggregated 8-day average daytime surface temperature values. The temperature values are subjected to a linear transformation into $ET$ values based on the application of the Priestley and Taylor (1972) equation in combination with the complementary relationship (Bouchet, 1965) of evaporation, as formulated by the Morton et al. (1985) WREVAP program. This is one of the most widely tested areal $ET$ estimation tools available (see Szilagyi and Jozsa, 2013 and Szilagyi et al., 2003 and references therein, Szilagyi et al., 2011a and Szilagyi et al., 2011b). The $GR_{p,\text{MODIS}}$ rates derived from this technique are considered as net $GR$ estimates, and it is possible to obtain negative values where $ET$ is consistently larger than $P$. When averaged over 10 years, these areas are generally considered to be groundwater discharge zones (see Figure 2 and Figure 4). Since groundwater discharge zones correspond to areas with a shallow water table of less than ~5 m, known as the critical depth or extinction depth (see Chen and Chen, 2004; Kollet and Maxwell, 2008; Szilagyi et al., 2013), and relatively short vadose zone lag times, the lag times presented in this study are only for positive net $GR$ zones (i.e., dune areas with $GR_{p,\text{MODIS}} > 0$).

The MODIS-based technique provides $GR_{p,\text{MODIS}}$ estimates with an expected error range of 15% (based on 5% error in $P$, and 10% error in $ET$ rates), not unusual for field-based $GR$ estimates, and is considered to be acceptable for many applications including regional groundwater modeling (Szilagyi et al., 2011b). However, mean decadal $ET$ values from Szilagyi and Jozsa (2013) have been slightly corrected to account for about 8% overestimation based on a multi-year/multi-site energy balance Bowen ratio. While the use of the $P-ET$ approach
assumes any changes in soil moisture are negligible, it is very accurate with regard to the water balance partly because it captures the effects of the plant root zone with a monthly temporal resolution. Thus, the long-term estimates of deep drainage \(GR_p^{\text{MODIS}}\) are influenced by the effects of root zone soil moisture changes during wet and dry parts of the year. The resulting \(GR_p^{\text{MODIS}}\) rates for the NSH have been verified by comparison with \(GR_p\) estimates using groundwater chloride mass balance and basin runoff analyses, and they have an unprecedented spatial resolution for distributed \(GR_p\) estimates in the region (Szilagyi et al., 2011b). All \(P - ET\) rates are within 36 mm/yr (7% of mean \(P\)) for basin runoff analyses in three NSH watersheds, and within 1 mm/yr for the chloride mass balance estimates (Szilagyi et al., 2011b).

3.2.2. Future period

Changes in future period (2010–2099) \(GR_p\) rates were developed from two sets of bias-corrected spatially downscaled hydroclimate projections from the World Climate Research Program (WCRP) Coupled Model Intercomparison Project Phase 3 (CMIP3). Data are from the U.S. Bureau of Reclamation (USBR, 2011) with hydrology variables produced using the Variable Infiltration Capacity (VIC) macroscale hydrology model (Liang et al., 1994). These hydroclimate scenarios are referred to herein as CMIP3/VIC scenarios. These data were downloaded from the U.S. Bureau of Reclamation website (http://gdo-dcp.ucirnl.org/downscaled_cmip_projections), containing monthly archives of both climate and hydrology variables from a large number of GCM results. CMIP3, rather than CMIP5, model data were used to enable comparisons to previous work and because hydrology projections were not yet available for CMIP5 at the time of writing of this article. In fact, CMIP5 climate projections change little from CMIP3 projections for the central Great Plains region of the U.S., and thus for the NSH (Brekke et al., 2013).

From the U.S. Bureau of Reclamation archive, we used the GCM produced climate variable \(P\) and the VIC produced hydrology variable \(ET\) in order to calculate (as an intermediate step) mean \(GR_p\) rates for each decade in the future period (2010–2019, 2020–2029, ..., 2090–2099). Specifically, we used two GCM scenarios, including SRES-B1-NCAR-CCSM3-3-04 (from the National Center for Atmospheric Research), and SRES-A1B-GFDL-CM2.1 (from the U.S. Department of Commerce/NOAA/Geophysical Fluid Dynamics Laboratory). These two GCMs perform relatively well in terms of their skill in reproducing observations of temperature and \(P\) (Knutti et al., 2013). However, visual inspection of plotted mean decadal CMIP3/VIC scenario \(GR_p\) rates in the NSH for the modern period (2000–2009) from all 36 available GCMs forced by the SRES A2 greenhouse gas emissions path (the highest global warming scenario; see IPCC, 2000), revealed a weak overall correlation with and spatial bias as compared against the \(GR_p^{\text{MODIS}}\) dataset. Especially concerning is the fact that none of the CMIP3/VIC scenarios show negative \(GR_p\) rates within the NSH, even though they occur in 8.5% of pixels from Szilagyi and Jozsa’s (2013) MODIS-based product, and the magnitude of the negative \(GR_p^{\text{MODIS}}\) rates exceeds 300 mm/yr in some of the pixels (see Figure 4). The poor relationship between \(GR_p\) rates from these different products (\(GR_p^{\text{CMIP3/VIC}}\) vs. \(GR_p^{\text{MODIS}}\)) is due primarily to two reasons, including limited observational data in the NSH in which the statistical downsampling of the GCM results is based upon, affecting the accuracy of the climate model variable \(P\), and the use of the VIC macroscale hydrology model to simulate \(ET\). The VIC model does not adequately treat groundwater interactions with surface water because of its model structure and relatively large cell size (~12-km), leading to a very poor calibration to streamflows in and surrounding the NSH (USBR, 2011).

Because of the large discrepancy between these two \(GR_p\) datasets, we opted to use a modified “Delta” method implemented by the U.S. Bureau of Reclamation (USBR, 2010), and follow the approach similar to Crosbie et al. (2013) in presenting future climate change results as changes in \(GR_p\). With this method, adjustments are made to the modern period (2000–2009) \(GR_p^{\text{MODIS}}\) rates based on relative changes projected by the CMIP3/VIC scenarios as recharge scaling factors (RSFs). The assumption is that by calculating climate change signals from the CMIP3/VIC model simulations and applying these changes to the observed climate, the effect of bias in the future projections is minimized. In this way, the method preserves...
nearly the same spatial pattern and the exact same resolution of \(G_{\theta,\text{MODIS}}\) estimates. To do this, we utilized the ratio of future period (2010–2099) to modern period (2000–2009) \(G_{\theta}\) from the CMIP3/VIC scenarios. Thus, for the future decades \((t)\), RSFs were calculated as \(RSF(t) = G_{\theta}(t)/G_{\theta}(2000–2009)\). Then, the dataset of \(G_{\theta,\text{MODIS}}\) values were multiplied by \(RSF(t)\) to obtain future annual potential \(G_{\theta}\) averaged over time \(t\) \((G_{\theta}(t))\). This was done for each \(G_{\theta,\text{MODIS}}\) pixel and each future decade (from 2010 to 2099) for both a wet and dry future GCM scenario.

While only two CMIP3/VIC scenarios are utilized in this study (wet and dry), their method of selection allows for the representation of the uncertainty range in projections of changes in \(G_{\theta}\) rates for a 2090–2099 climate relative to a 2000–2009 climate, due to different magnitudes of global warming by the end of the 21st century and differences among GCMs and greenhouse gas emission paths. This was accomplished by first calculating the sample standard deviations of the spatially averaged RSFs (mean for 2090–2099) from all 112 available CMIP3/VIC hydroclimate model runs (including 16 GCMs and 3 emission paths) in the NSH. Then, the two hydroclimate scenarios with RSFs nearest to \(\pm 1\) from the mean were selected. We found the scenario nearest to \(+1\) (SRES-B1-NCAR-CCSM-3-0.4) and the scenario nearest to \(-1\) (SRES-A1B-GFDL-CM2.1) from the mean of the 112 spatially averaged RSFs. These were defined as wet and dry scenarios, respectively.

A more rigorous evaluation quantifying uncertainty due to these scenarios would explicitly include all 112 available hydroclimate projections in the calculation of vadose zone lag times, and would examine other sources of uncertainty, such as caused by statistical downscaling and the use of the VIC hydrology model. This would require an unnecessarily large amount of time, and the resulting RSFs obtained from this approach are similar in magnitude to those presented by Crosbie et al. (2013) for the Northern High Plains (which encompasses the NSH region).

### 3.3. Vertical velocity and lag time of soil moisture

There are three major velocity characteristics of soil moisture in the vadose zone with a unit hydraulic gradient initial profile; one is Darcy’s velocity. If we assume that the movement of moisture through the vadose zone is vertical (where the vertical coordinate \(z\) increases downward), gravity-driven, and steady, such that a unit hydraulic gradient exists \((dH/dz = -1)\), as is conventionally specified (e.g., Rasmussen, 2001; Sisson et al., 1980; Warrick et al., 1971), we obtain the following expression:

\[
q - G_{\theta} = K(\theta)
\]  

which states that Darcy’s velocity \((q)\) equals the potential GR rate \((G_{\theta})\) and the water-dependent hydraulic conductivity \([K(\theta)]\), where \(\theta\) is the volumetric soil water content, and \(H\) is the total hydraulic head.

Small perturbations of hydrologic conditions at the land surface result in similarly small changes of soil moisture contents and pressure (or pressure gradients) traveling downward with the vertical velocity \((c)\) as follows:

\[
q = \frac{dq}{d\theta} = \frac{dK(\theta)}{d\theta} c
\]  

This velocity is used if one is interested in the timing of arrival of capillary pressure changes at the water table resulting from the changes in pressure and pressure gradients at the land surface (Philip, 1957; Warrick et al., 1971; Wilson, 1974), referred to as the kinematic wave approximation (Sisson et al., 1980) or kinematic velocity (Rasmussen, 2001). The pressure-based velocity is the most relevant when calculating lag times associated with GR. The relationship \(K(\theta) = G_{\theta}\) from Eq. (1) can also be used to infer spatially distributed, but vertically averaged \(\theta\) values in pixels where \(G_{\theta}\) and soil hydraulic parameters are specified.

Finally, a conservative tracer-based velocity \((v)\) in the vadose zone is calculated as the advective tracer velocity using:

\[
v = \frac{q}{\theta} = \frac{K(\theta)}{\theta}
\]  

which is the equation of interest for aquifer vulnerability studies (e.g., Healy, 2010).

Studies of Warrick et al., 1971, Wilson, 1974 and Wilson and Gelhar, 1981, and Rasmussen (2001) showed that the pressure-based (kinematic) velocity exceeds the tracer-based (advective) velocity by a factor in excess of two to four, depending on moisture content, choice of conductivity–water content relation and solute transport parameters. The tracer-based velocity is greater than Darcy’s velocity as follows from Eq. (3).

Considering the relative homogeneity of soil texture within sand dunes, and a previous study of numerous High Plains sites with thick vadose zones (15–50 m), in which McMahon et al. (2006) found that hydraulic gradients are near unity, ranging from 0.83 to 0.97, the assumptions used in obtaining Eq. (2) are thought to be valid for application in the NSH. The unit hydraulic gradient assumption is also valid when considering the relatively small changes in \(G_{\theta}\) associated with the decadal time step used. However, selection of this large time step does have the potential to inflate estimates of the lag times of the draining water’s center of mass, since wet periods (with duration of days to weeks) could significantly increase \(G_{\theta}\) rates and vertical velocities (see Grismer, 2013). Thus, we consider the lag time estimates achieved with this approach as conservative (large), and recommend that it be used as a first-order approximation with a decadal (or longer) time step. The van Genuchten–Mualem equation (Mualem, 1976; van Genuchten, 1980) is used to calculate \(K(\theta)\) and \(c\), with baseline soil hydraulic parameters taken for sand from Carsel and Parrish (1988) and NRCS (2006). This equation for hydraulic conductivity is expressed as

\[
K(S_v) = K_v S_v^{1/2} \left[1 - (1 - S_v^{1/m})^m\right]^2
\]  

and the relative saturation \((S_v)\) as

\[
S_v = \left(\frac{\theta - \theta_r}{\theta_f - \theta_r}\right)
\]  

where \(K_v\) is the saturated hydraulic conductivity; \(\theta_r\) is the residual soil water content; \(\theta_f\) is the saturated soil water content; and \(m\) is a pore size distribution coefficient. The equation for soil moisture vertical velocity \((c)\) is obtained by differentiating Eq. (4) with respect to \(\theta\), expressed as

\[
c = \frac{dK(\theta)}{d\theta} = \frac{K(1 - S_v^m)^2}{2(\theta_f - \theta_r) S_v^{1/m}} \left[1 + \frac{4S_v^{1/m} S_v^{m-1}}{1 - S_v^m}\right]
\]  

where

\[
S_v = 1 - S_v^{1/m}
\]  

The reference to “baseline” soil hydraulic parameters is used here as they are estimates, which are known to vary at least somewhat across the NSH. Nevertheless, they are considered as current best estimates, given that field studies of soil hydraulic parameters are limited in the NSH (especially for depths below the root zone). Sensitivity analyses of the effects of soil hydraulic parameter uncertainty on the spatial mean and range of vertical velocity and lag time estimates were also conducted by systematically varying the two most sensitive and uncertain parameters, \(K_v\) and \(\theta_f\).
Once vertical velocity ($c$) had been determined using Eqs. (6) and (7), vadose zone lag time ($\tau$) was computed using the following expression:

$$\tau = D_{at}/c$$  \hspace{1cm} (8)

where $D_{at}$ is the mean depth to the water table (or vadose zone thickness) described in Section 3.1. The spatial pattern of $\tau$ was mapped in ArcGIS™ by appending values of it to a point shapefile of $GR_{p,MODIS}$ values, and then converting them into a raster dataset aligning with $GR_{p,MODIS}$ pixels. Values of $c$ and $\tau$ were calculated only for positive $GR_{p,MODIS}$ pixels (36,663 pixels, $\sim 44,600 \text{ km}^2$), representative of upland net GR zones (see Figure 2), because lag times should be small and can be neglected for zones with net groundwater discharge ($GR_{p,MODIS}$ < 0).

The methods used here to estimate $D_{at}$ may lead to an overestimation of lag times because the effects of capillary rise near the water table and thickness of the root zone are not taken into account (i.e., $D_{at}$ is considered to be the difference between the land surface and the water table elevations). However, in general, these factors will likely lead to only small errors in lag time estimates, and potential errors arising from these factors would be largest where the water table is relatively shallow and smallest where the water table is relatively deep.

4. Results and discussion

4.1. Vadose zone thickness in the NSH

The tremendous spatial variability of topography in the NSH (Figure 3) causes considerable changes in vadose zone thickness ($D_{at}$) on local and regional scales (Figure 5), affecting the interaction between the climate and the aquifer through ET and GR. Figure 5 illustrates the extreme variation of $D_{at}$ in the NSH, which ranges from 0 to 152 m, with a mean of 21.9 m ($\sigma = 15.6$ m). Approximately 80.3% of the region ($\sim 39,000 \text{ km}^2$) has $D_{at}$ that is greater than the approximate extinction depth of 4 m (Chen and Chen, 2004 and Szilagyi et al., 2013), where groundwater ET is no longer influenced by vegetation (Soilu et al., 2010). Additionally, a substantial portion of the region (35.7%, $\sim 17,500 \text{ km}^2$) has $\rho_{at} > 25$ m. These areas generally occur in the central and western parts of the NWH, with exceptionally large $D_{at}$ where there are large sand dunes, and in some areas surrounding highly incised river valleys, including two large areas near the headwaters of the Dismal and Middle Loup Rivers in the central part of the NSH (Figure 1, and warm colors in Figure 5). The extensive occurrence of a thick vadose zone indicates the importance of lag times for future water resources planning and climate change studies (e.g., at 10, 50 and 100 yr time scales). The spatial distribution and overall magnitude of vadose zone thickness presented here is consistent with that found within a large portion of the central NSH (10,000 km²) by Chen and Chen (2004), who used similar regional datasets of the land surface and water table topography.

4.2. Vadose zone lag times with modern period potential groundwater recharge

Estimates of vadose zone lag times using Eq. (8) were made for 36,663 independent $GR_{p,MODIS}$ pixels in the NSH ($\sim 44,600 \text{ km}^2$). The large $GR_{p,MODIS}$ rates (Figure 4), with a mean of 78 mm/yr for positive $GR_{p,MODIS}$ areas, along with the highly permeable sand deposits that characterize the NSH’s geology, promote relatively quick drainage of vadose zone water. However, extreme variations exist in the spatial distribution of lag time estimates (Figure 6). Comparison of Figure 4, Figure 5 and Figure 6 allows examination of the effect of a heterogeneous vadose zone thickness on the spatial distribution of vadose zone lag times (as influenced by modern period GR conditions). The longest vadose zone lag time estimates in the NSH (warm colors in Figure 6) occur in areas with a deep water table (warm colors in Figure 5) and low GR rates (cool colors in Figure 4), and vice versa for the shortest lag times. Many pixels with relatively long lag time estimates in the north-central and western parts of the NSH (sand dune areas) are found directly adjacent to those with minimal lag times (areas with lakes and wetlands; see Figure 3). Also, other areas with a thick vadose zone (besides dunes; described in Section 4.1) have relatively long (greater than the mean) lag time estimates, whereas vast areas in eastern parts of the NSH have relatively short lag time estimates due to a shallow water table and large GR rates.

Estimated vadose zone lag times with average modern period $GR_{p,MODIS}$ rates range from 0 to 359 yrs, with a spatial mean of 5.28 yrs (assuming baseline soil hydraulic parameters; see Table 1). These lag time estimates are consistent with the range of tracer-based lag times reported by McMahon et al. (2006) of about 50–375 yrs for irrigated sites in the High Plains (with 15–50 m thick vadose zones) when one considers the relationship between pressure-based and tracer-based velocities, since solutes move by a factor of roughly two to four times slower than pressure changes in the vadose zone (Rasmussen, 2001; Wilson, 1974). Vertical velocities estimated here (mean of 5.68 m/yr, ranging from 0.24 to 14.9 m/yr), assuming baseline soil hydraulic parameters, are also consistent with those reported by McMahon et al. (2003) of at least 2–3 m/yr for an irrigated site in the Central High Plains composed of sandy and loamy soils (with an estimated deep drainage rate of 53–54 mm/yr). Furthermore, Istanbulluoglu et al. (2012) applied a linear reservoir model fitted to the North Loup watershed’s (see Figure 1) empirically determined runoff response to climate, and found a basin drainage time scale of 9.5 years, effectively representing the combined lag effects of both the vadose zone and High Plains aquifer. Their single estimate of lag time is several years longer than the mean found here for the NSH, as expected, since lag times associated with the aquifer are excluded here. Thus, our relatively simple technique yields estimates that are consistent with those from previous field and more detailed modeling studies.

4.3. Sensitivity of vertical velocity and lag time estimates to soil hydraulic parameter uncertainty

Here we focus on the sensitivity of the two most important and uncertain hydraulic parameters, saturated hydraulic conductivity ($K_s$) and residual soil moisture content ($\theta_r$). The highest $GR_{p,MODIS}$ rate for any pixel in the NSH is 276 mm/yr, constraining the inferred depth-averaged soil moisture content within any given $GR_{p,MODIS}$ pixel to be no greater than 0.151 m³/m³ (based on assumptions in using Eq. (1)). Thus, the influence of varying $\theta_r$ is expected to be much larger than for $K_s$ (assumed to be 0.43 m³/m²; see Table 1). Parameter $m$ in the van Genuchten–Mualem equation is unlikely to vary much for eolian sand, and its sensitivity with regard to changes in vertical velocity and lag time are also assumed to be small relative to those caused by variations in $K_s$ and $\theta_r$.

Baseline and adjusted soil hydraulic parameters used in the sensitivity analyses and their impact on the spatial mean and range of the vertical velocity ($c$) and vadose zone lag time ($\tau$) estimates within the NSH (assuming mean decadal $GR_{p,MODIS}$ rates) are presented in Table 1. Runs 2–5 test changes in adjustments to $K_s$ (varied between 0.316 and 10.54 m/d), and runs 6–9 test changes in adjustments to $\theta_r$ (varied between 0.0135 and 0.0900). Baseline parameters are taken for sand from Carsel and Parrish (1988), and NRCS (2006) for $K_s$, in the absence of detailed field characterization of deep soils/vadose zone geology in the NSH. The range in adjusted $K_s$ values
investigated here is representative of the expected range of variation based on field work in the western part of the NSH presented by Zlotnik et al. (2007), who used direct push methods to obtain $K_s$ measurements from three depths (exceeding several meters) at 11 sites. The range in adjusted $\theta_r$ values represents variations for sand consistent with those presented by Carsel and Parrish (1988). Testing the influence of these expected variations allows for assessment of the level of potential error arising from the uncertainty involved in soil hydraulic parameter estimates.

The largest changes in vertical velocity and lag time estimates are due to the most sensitive and uncertain soil hydraulic parameter, $K_s$ (Table 1). Furthermore, the longest vadose zone lag time estimate of 496 yrs (mean of 7.28 years) is associated with the smallest $K_s$ value tested (0.316 m/d); and the shortest lag time estimates (mean of 2.85 yrs, and max. of 194 yrs) is associated with the largest $K_s$ value tested (10.54 m/d). The effects of varying $K_s$ and $\theta_r$ independently for all nine runs (including the baseline) are shown graphically in Figure 7, illustrating their effect on the nonlinear relationship between

Figure 5. Thickness of the vadose zone (m) in the Sand Hills within eight color-coded classes, estimated as the difference in 30-m digital elevation model data after USGS (1999) and spring 1995 water table digital data after Summerside et al. (2001). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

Figure 6. Vadose zone lag time (yrs) of soil moisture in the NSH with baseline soil hydraulic parameters, estimated using vadose zone thickness and modern period averaged (2000–2009) mean $GR_{MODİS}$ rates. Note the logarithmic scaling of color-coded classes. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).
vertical velocity of the pressure pulse and soil moisture content, based on the proposed 1D pressure-based approach. Figure 7 also shows the expected range in soil moisture content in positive net GR zones (where $GR_{p,MODIS} > 0$), which varies from 0.030 to 0.151 m$^3$/m$^3$ (the range on the x-axis), and that the estimated vertical velocities do not exceed 27.4 m/yr (the max. value on the y-axis). Although, for individual combinations of $K_s$ and $\theta_r$, the predicted range in $\theta$ and $c$ is smaller than that shown in Fig 7. While the possible range of vertical velocities is shown to vary substantially in Figure 7, the impacts of the uncertainty due to $K_s$ and $\theta_r$ does not lead to the same relative changes in estimated mean lag times as they do for mean vertical velocities (see Table 1). In fact, the degree of sensitivity to $K_s$, decreases with increasing $K_s$ values for the mean $\tau$ relative to the sensitivity of the mean $c$. This is caused by the mediating factor of $D_{sr}$ used in calculating lag times, and the fact that the degree of sensitivity of vertical velocity to $K_s$ is a function of $\theta_r$ and that sensitivity decreases with decreasing $\theta_r$, whereas the degree of sensitivity to $\theta_r$ does not vary with $\theta$ (Figure 7). Although, the sensitivity of $\theta_r$ also appears to vary in direction depending on the predicted variable ($c$ or $\tau$).

4.4. Vadose zone lag times with future period potential groundwater recharge

The effects of the two future climate change scenarios investigated (wet and dry CMIP3/VIC scenarios), on spatially averaged 10-yr $GR_p$ rates in the NSH, differ by both magnitude and direction of changes relative to the modern period (Figure 8). Also, $GR_p$ rates in the future period (2010–2099) exhibit moderate (dry scenario) to high (wet scenario) interdecadal variations (Figure 8). The wet hydroclimate scenario produces a spatially averaged future period (2010–2099) mean $GR_p$ rate of 1.49, which translates into a mean $GR_p$ rate of 118 mm/yr over the NSH. By the end of the century (2090–2099), the decadal $GR_p$ rate under a wet future climate is projected to be 128 mm/yr ($RSF = 1.63$), an increase of 50 mm/yr relative to the modern period (2000–2009). Additionally, the largest variation for a single decade in the wet scenario produces the highest projected spatially averaged $GR_p$ rate of 212 mm/yr ($RSF = 2.68$), occurring in the decade of 2060–2069. In contrast, the dry hydroclimate scenario produces a spatially averaged future period mean $RSF$ of 0.82, translating into a mean $GR_p$ rate of 65 mm/yr. By the end of the century (2090–2099), the spatially averaged 10-yr mean $GR_p$ under a dry future climate is projected to be 61 mm/yr ($RSF = 0.76$), a decrease of 17 mm/yr relative to the modern period. In addition, the lowest projected mean $GR_p$ rate, occurring in the decade of 2030–2039, is 47 mm/yr ($RSF = 0.60$). Thus, there is considerable uncertainty in the magnitude and direction of projected groundwater recharge changes for the NSH, since the two future scenarios are representative of ±1σ from the mean $RSF$ of 1.21 ($N = 112$).

The NSH mean $GR_{p,MODIS}$ rate, and wet and dry scenario RSFs for 2000–2009 are: 78 mm/yr, 1.63, and 0.76, respectively (for pixels where $GR_{p,MODIS} > 0$). These values are comparable to those found by Crosbie et al. (2013) for the Northern

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**Table 1.** Results of sensitivity analyses of the mean and range of vertical velocity and lag time estimates within the NSH using baseline (run 1) and adjusted soil hydraulic parameters (runs 2–9).

<table>
<thead>
<tr>
<th>Run</th>
<th>$K_s$ (m/d)</th>
<th>$\theta_r$ (m$^3$/m$^3$)</th>
<th>$c$</th>
<th>Mean (m/yr)</th>
<th>Range (m/yr)</th>
<th>$\tau$</th>
<th>Mean (yrs)</th>
<th>Range (yrs)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.054</td>
<td>0.0450</td>
<td>5.68</td>
<td>0.24–14.9</td>
<td>5.28</td>
<td>0–359</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>0.632 (−40)</td>
<td>0.0450</td>
<td>4.96</td>
<td>0.21–13.0</td>
<td>6.05 (±15)</td>
<td>0–412</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>0.316 (−70)</td>
<td>0.0450</td>
<td>4.13</td>
<td>0.17–10.9</td>
<td>7.28 (±38)</td>
<td>0–496</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>2.108 (+100)</td>
<td>0.0450</td>
<td>6.83</td>
<td>0.29–17.8</td>
<td>4.39 (−17)</td>
<td>0–298</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>10.54 (+900)</td>
<td>0.0450</td>
<td>10.5</td>
<td>0.45–27.4</td>
<td>2.85 (−46)</td>
<td>0–194</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>1.054</td>
<td>0.0270 (−40)</td>
<td>5.43</td>
<td>0.23–14.2</td>
<td>5.53 (±5)</td>
<td>0–376</td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>1.054</td>
<td>0.0135 (−70)</td>
<td>5.25</td>
<td>0.22–13.7</td>
<td>5.71 (±8)</td>
<td>0–387</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>1.054</td>
<td>0.0675 (+50)</td>
<td>6.03</td>
<td>0.26–15.8</td>
<td>4.97 (−6)</td>
<td>0–339</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>1.054</td>
<td>0.0900 (+100)</td>
<td>6.43</td>
<td>0.28–16.8</td>
<td>4.66 (−12)</td>
<td>0–315</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

a. Percent relative changes from the baseline are shown in parentheses. Modern period (2000–2009) mean $GR_{p,MODIS}$ rates are used. Soil hydraulic parameters are for sand from Carsel and Parrish (1988), with $K_s$ from NRCS (2006). $\theta_r$ (0.430 m$^3$/m$^3$) and $m$ (0.0627) are unchanged for all runs.
High Plains region (which encompasses the NSH), despite the differences in methodology used to estimate GRp and future RSFs. They modeled a spatially averaged mean GRp rate of 78 mm/yr for the historical period (1982–2011), and future (2050) RSFs of 1.32 and 0.76 with GCM climate variables used as input to the Soil-Vegetation-Atmosphere-Transfer model, WAVES, and upscaling of results with the aid of regional soil texture and vegetation datasets. The fact that the RSFs calculated by Crosbie et al. (2013) were for year 2050 might explain some of the difference between their wet scenario RSF and that found here of 0.31 (ΔRSF = 1.63–1.32), as the wet scenario analyzed in this study has a mean RSF of 1.30 for the 2040–2060 period. However, the 2040–2060 mean RSF for the dry scenario is 0.95 here, a value of 0.19 larger than that reported by Crosbie et al. (2013) for 2050. For future GRp scenarios in the NSH, we thus conclude that interdecadal variations in RSFs between GCM scenarios are large, adding to some of the observed deviations in RSFs throughout the 21st century. This is evident because Crosbie et al. (2013) used average results of 16 GCMs, while only one GCM scenario was used here for each of the two hydroclimate scenarios. Yet, the historical mean and overall trends in future spatially averaged mean GRp rates found here are comparable to those found by Crosbie et al. (2013). However, an important distinction is that the spatial distribution of future RSFs from this study are substantially different than those found by Crosbie et al. (2013). This is explained by the utilization of the “Delta” method here, rather than aggregated estimates of GRp from point-scale modeling. That is why the spatial distribution of future GRp rates found in this study still greatly reflects that from the MODIS-based estimates of Szilagyi and Jozsa (2013), which is most likely a more accurate representation of the spatial distribution of GRp.

Figure 9 and Figure 10 illustrate the spatial distribution of vadose zone lag time with mean end-of-century (2090–2099) GRp rates (wet and dry scenarios, respectively). The wet and dry future GRp scenario spatially averaged end-of-century (2090–2099) mean (max.) vadose zone lag time estimates are 3.78 yrs (583 yrs) and 6.55 yrs (253 yrs), respectively (assuming baseline soil hydraulic parameters; see Table 1). This represents a change in the mean (max.) vadose zone lag times by −29% (~42%) and +24% (+30%) for the wet and dry scenarios, respectively. However, the large RSF for the wet scenario, with a spatial mean over the NSH of 1.63 (representing a 63% increase in GRp for 2090–2099 relative to 2000–2009), does not translate into the same magnitude of changes in estimated lag times. This is partially attributed to the spatial bias in the future wet CMIP3/VIC hydroclimate scenario GRp rates, because they systematically predict greater increases in GRp for the northern and western parts of the NSH. These areas have low GRp,MODIS rates and make up a large proportion of the pixels with long lag times.

A particularly interesting finding is that the entire histogram of vadose zone lag time estimates for the 2090–2099 period is shifted relative to those with 2000–2009 GRp,MODIS rates (Figure 11). The wet scenario shifts the histogram toward shorter lag times, while the dry scenario shifts the histogram toward longer lag times. Additionally, analysis of cumulative frequency curves of vadose lag time estimates within the NSH (Figure 11) provides estimates of the percentage of NSH area expected to experience changes in GRp rates over any time scale (equal to the vadose zone lag time of interest). With modern period mean GRp,MODIS rates, most of the NSH groundwater system surface area (89.9%) is expected to reflect changes in GRp from changing climatic conditions within 10 years (by 2019), and nearly all of it within 50 years (99.6% by 2059), and 100 years (99.9% by 2099).

For comparison, with future GRp rates (2090–2099), 99.8% (wet scenario) and 99.4% (dry scenario) of the NSH groundwater system surface area is estimated to be affected by changes in the GRp rate within 50 years (by 2059). This translates into a change in the area affected by only ±85 km² (relative to 2000–2009). Compared to the large changes in the mean estimated vadose zone lag time in response to changes in GRp rates under future hydroclimate scenarios (~29% and +24%), the expected changes at the tail end of the distribution are relatively small (notice the convergence of cumulative frequency curves for large lag times in Figure 11).

Since only a small portion of the NSH has estimated vadose zone lag times exceeding 10 years, changes in GRp that differ from GRp rates, for the same decade, are not predicted to
be drastic throughout the entire 21st century. The longest estimated future mean vadose zone lag times in the NSH (assuming baseline soil hydraulic parameters) occur when the \( GR_p \) in the dry scenario drops to a low of 47.2 mm/yr in the decade of 2030–2039 (from 78 mm/yr for 2000–2009), with a corresponding mean lag time of 7.7 years. During that decade, ~75% of the NSH is expected to have lag times shorter than 10 years. Also, interdecadal variability in \( GR_p \) rates for the dry scenario future climate are considered moderate—mean annual \( GR_p \) rates range from 47.2 mm/yr to 88.0 mm/yr, while the mean for the entire future period (2010–2099) is 65.4 mm/yr (Figure 8).

These findings provide evidence that for groundwater modeling applications in the NSH, changes in \( GR_p \) can be used as input without explicitly accounting for vadose zone lag times only if the interest lies in utilizing stress periods with a temporal resolution of approximately a decade, or longer. However, lag times will not be the same in other regions, and for many applications shorter stress periods in models will be needed. Therefore, the proposed pressure-pulse, or kinematic wave-based approach, combined with satellite-derived estimates of \( ET \) (to provide \( GR_p \)) will be useful in groundwater modeling applications for testing whether or not inclusion of the lag effect caused by the vadose zone is warranted or not.

It should be noted that the pixel size (1.1-km) may have a certain bearing on the results. With a smaller pixel size, one should expect only some changes of the shape and position of the modern and future period histogram of vadose zone lag times, shown in Figure 11. However, the variability of \( D_{wt} \) within such pixels is smaller than the range of the vadose zone thickness (Figure 5) as discussed in Section 3.1, which would result in nearly the same quantitative and qualitative conclusions.

5. Summary and conclusions

This study evaluates water movement through the vadose zone in areas within a large portion of the NSH (~44,600 km²) where average \( P \) exceeds \( ET \) (over the 10-yr measurement period), leading to significant \( GR \). Spatially distributed and high resolution (1.1-km) MODIS-based decade averaged \( GR_{p,MODIS} \) rates for the modern period (2000–2009) provides the basis for calculating the pressure-based (or kinematic wave-based) velocities, which are then used to estimate vadose zone lag times. The analysis also relies on inputs of vadose zone thickness (depth to the water table), estimates of future period (2010–2099) \( GR_p \) rates from WCRP CMIP3 hydroclimate model projections, and estimates of hydraulic conductivity using the van Genuchten–Mualem equation. The proposed approach does not rely on parallel supercomputing, commonly involved in variably-saturated 3D numerical modeling of basin hydrology. Yet, it provides the desired high resolution, large scale (>10⁶ km²) simulation of soil moisture movement through the vadose zone under long-term average climate conditions.
This study answers four research questions with regard to the NSH: (1) What is the effect of a heterogeneous vadose zone thickness on the spatial distribution of vadose zone lag times? (2) How does soil hydraulic parameter uncertainty affect vertical velocity and vadose zone lag time estimates? (3) How are 21st century climate change projections expected to impact GRp rates and vadose zone lag times? and (4) What is the percentage of surface area expected to experience changes in GRp rates over time scales of 10, 50 and 100 years, typical of water planning and future climate modeling time scales? These questions are relevant for many other regions in the world and are needed for groundwater modeling applications, analysis of climate change impacts on groundwater, and the effective management and sustainability of future water resources.

In the NSH, the high spatial variability of vadose zone thickness and spatio-temporal variability of climatic conditions both influence the distribution and magnitude of the time lag between changes in deep drainage and actual GR at the water table. The mean vadose zone thickness is 21.9 m (σ = 15.6 m), while the mean GRp rate and vadose zone lag time (τ) for the decade of 2000–2009 are 78 mm/yr and 5.28 yrs, respectively (for positive GRp MODIS pixels assuming baseline soil hydraulic parameters). Variability of RSFs was incorporated into the analysis of potential climate change effects through the selection of wet and dry hydroclimate scenarios from 112 GCM scenarios as nearest to ±10% from the mean RSF (1.21) for 2050–2099 in the NSH. Thus, the spatial mean GRp rates for the future period are highly uncertain for the region and are projected to vary between a high of 212 mm/yr (RSF = 2.68) and a low of 47 mm/yr (RSF = 0.60), with end-of-century (2090–2099) RSFs of 1.63 and 0.76 for the wet and dry hydroclimate scenarios evaluated. The percentage of the NSH surface area expected to experience changes in GRp rates (lag times calculated using GRp MODIS rates and baseline soil hydraulic parameters) is 89.9% in 10 yrs (2019), 99.6% in 50 yrs (2059), and 99.9% in 100 yrs (2099). The longest estimated future spatially averaged vadose zone lag time estimate in the NSH occurs when the GRp rates from the dry scenario drops to a low of 47.2 mm/yr in the decade of 2030–2039, with a corresponding mean vadose zone lag time of 7.7 yrs. During that decade, ~75% of the NSH is expected to have lag times shorter than 10 yrs.

Hydraulic conductivity and vertical velocity (and thus, lag time) estimates in the NSH have uncertainties due to potential heterogeneity in geologic materials and limited data from field measurements. Sensitivity analyses reveal that saturated hydraulic conductivity is the most important hydraulic parameter, as expected, but that its sensitivity varies with moisture content and GRp. Variations in vertical velocity and vadose zone lag time estimates due to uncertainty in Ks can be substantial. In fact, the expected range of possible Ks values leads to a greater change in estimated vadose zone lag times than do projected changes in end-of-century GRp rates (2090–2099 relative to 2000–2009). The spatially averaged vadose zone lag time estimates range from 2.85 to 7.28 yrs for all Ks variations, and from 3.78 to 6.55 yrs for expected future climate variations (2090–2099). Therefore, it is quite clear that more detailed field characterization of hydrogeologic properties is desirable, especially when using hydrological models to make decisions about the future management of water resources impacted by climate change. These findings suggest that for the NSH, vadose zone model development efforts should be focused on assessment of model parameters, and they indicate that uncertainty caused by future GCM scenarios and downscaling methods are less important than those due to the hydrologic model, and not because a relatively simple model was used here.

While uncertainty in lag time estimates due to future climate projections and uncertainty in soil hydraulic parameters were explicitly evaluated, errors in lag time estimates associated with estimating Dsv and GRp MODIS rates, as well as assuming that long-term (10-yr) average GRp rates can be used to accurately estimate long-term vertical velocities and lag times of soil moisture, can also be significant. As a caution, it should be stated that pressure heads and wetting fronts are not explicitly tracked with the simple gravity-driven kinematic velocity-based approach proposed here. That is why the approach should be used to estimate velocities and lag times under steady-state (~10-yr) climate conditions. Uncertainties arising from all of these factors combined preclude highly accurate prediction of lag time estimation even for regions with relatively homogeneous soil properties such as the NSH. Therefore, the proposed approach can only be used currently to obtain first-order estimates of the spatial distribution of lag times. At preliminary stages of work, these lag times indicate when the groundwater system will respond to changes in climate (as changes in diffuse GRp). It is encouraging, however, that lag time estimates obtained here are consistent with those from previous field and more detailed modeling studies.

The proposed approach will be especially helpful in regions with longer vadose zone time lags than those of the NSH and more arid environments, where the water table is deeper and/or soil texture is finer. Additionally, many applications require shorter stress periods than analyzed here (decadal). So, this approach will be useful for testing whether or not inclusion of the lag effect caused by the vadose zone is warranted in groundwater modeling, with consideration of the desired temporal resolution. Overall, the proposed simple analytical approach to calculate gravity-driven vertical velocity provides a rapid quantitative screening tool that can be used to study lag times between changes in GRp (deep drainage) and GRp (at the water table) affected by spatially variable vadose zone thickness and climate change. The approach also provides estimates expected to have the same degree of uncertainty as those obtained from the use of advanced analytical and numerical solvers, such as the MODFLOW UZF1 Package, ParFlow, MikeShe, or HYDRUS, since their use also requires estimates of GRp (or parameters to estimate actual ET) and soil hydraulic parameters. In summary, the proposed 1D vadose zone moisture modeling and GIS approach is applicable for use in semi-arid and arid regions with deep water tables and where long-term P and ET data for current and future conditions are available.

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