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Evaluating the complementary relationship of evapotranspiration in the alpine steppe of the Tibetan Plateau

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Abstract The complementary relationship (CR) of evapotranspiration allows the estimation of the actual evapotranspiration rate (ETa) of the land surface using only routine meteorological data, which is of great importance in the Tibetan Plateau (TP) due to its sparse observation network. With the highest in situ automatic climate observation system in a typical semiarid alpine steppe region of the TP, the wind function of Penman was replaced by one based on the Monin-Obukhov Similarity theory for calculating the potential evapotranspiration rate (ETp); the Priestley-Taylor coefficient, α, was estimated using observations in wet days; and the slope of the saturation vapor pressure curve was evaluated at an estimate of the wet surface temperature, provided the latter was smaller than the actual air temperature. A symmetric CR was obtained between the observed daily actual and potential evapotranspiration. Local calibration of the parameter value (in this order) is key to obtaining a symmetric CR: x, wet environment air temperature (Twet), and wind function. Also, present symmetric CR contradicts previous research that used default parameter values for claiming an asymmetric CR in arid and semiarid regions of the TP. The effectiveness of estimating the daily ETa via symmetric CR was greatly improved when local calibrations were implemented. At the same time, an asymmetric CR was found between the observed daily ETa and pan evaporation rates (Ep), both for D20 aboveground and E601B sunken pans. The daily ETa could also be estimated by coupling the Ep, of D20 aboveground and/or E601B sunken pan through CR. The former provided good descriptors for observed ETa, while the latter still tended to overestimate it to some extent.

1. Introduction

Quantifying terrestrial evapotranspiration rates (ETa) is not only critical for understanding how the water cycle interacts between the land and the atmosphere, but is also crucial for sustainable water resource management, and thus ecological and environmental conservation in semiarid and arid regions where the water crisis is most severe [Wang and Dickinson, 2012]. The Tibetan Plateau (TP), the world’s highest plateau, with an average altitude exceeding 4000 m above sea level (asl), is vitally important to the Northern Hemisphere’s climate due to its thermodynamic influence on atmospheric circulation patterns [Wu et al., 2012; Ye and Wu, 1998]. ETa in the TP therefore plays a key role in hemispheric energy and water cycle at various temporal and spatial scales through the release of latent heat. Consequently, research on ETa using in situ observations [Biermann et al., 2014; Gu et al., 2008], remote sensing techniques [Chen et al., 2013; Ma et al., 2014], and land surface models [Yang et al., 2011; Yin et al., 2013] at different spatial and temporal scales has intensified in the TP over the past few years. Owing to a harsh environment, only a sparse observation network exists, hindering a reliable estimation of the spatial variation of ETa within the TP. Specifically, existing meteorological stations managed by the Chinese Meteorological Administration (CMA) [see Yin et al., 2013, Figure 1], and the in situ observatories for land-atmosphere interactions [see Ma et al., 2008, Figure 1], still form an extremely sparse and unevenly distributed network: most stations are located in the eastern and southern TP, with only a few in the western regions. In addition, most stations are in valleys at a relatively low elevation and currently no station is located higher than 4800 m asl [Qin et al., 2009]. Undoubtedly, deriving regionally representative ETa rates with such scarce data is an obvious challenge, albeit urgent. For instance, the predominant cover of alpine steppe in the central and western TP has experienced significant degradation in the past decade due to changes in precipitation and the melting of frozen soil...
Nevertheless, whether the CR could be applied to estimate \( \text{ET}_a \) and \( \text{ET}_a \) rates over longer periods, the complementary relationship (CR) of Bouchet [1963], based on a proposed complementary feedback mechanism between \( \text{ET}_a \) and its potential maximum rate, \( \text{ET}_m \), under the same environmental conditions, is of value. The CR makes it possible to estimate \( \text{ET}_a \) from routinely measured meteorological variables, without requiring any major instrumentation. It also dispenses with measuring vegetation and soil conditions, arduous tasks in remote areas. Application of the CR at the catchment/basin scale is very convenient since it bypasses the collection of multiyear precipitation and runoff data to calculate \( \text{ET}_a \) with the help of a water balance approach. As a result, the CR theory has been applied to quantify \( \text{ET}_a \) on a wide range of spatial scales from a few kilometers [Huntington et al., 2011; Liu et al., 2012; Kahler and Brutsaert, 2006; Mallick et al., 2013] to basin-size [Liu et al., 2006; Matin and Bourque, 2013; Wang et al., 2011], as well as temporal scales from annual [Hobbins et al., 2004; Ramirez et al., 2005], to monthly [Szilagyi and Jozsa, 2008, 2009a; Szilagyi et al., 2009; Hobbins et al., 2001b; Xu and Singh, 2005], daily [Han et al., 2013; Jaksa et al., 2013; Ozdogan and Salvucci, 2004], or subdaily [Crango and Crowley, 2005; Han et al., 2014; Parlange and Katul, 1992].

Nevertheless, whether the CR could be applied to estimate \( \text{ET}_a \) in the TP is a matter of debate. On the one hand, it is well established that \( \text{ET}_a \) and \( \text{ET}_m \) exhibit an inverse relationship in water-limited areas [e.g., Golubev et al., 2001; Hobbins et al., 2001a, 2004; Jaksa et al., 2013; Ramirez et al., 2005]. Previous research in arid, semiarid, and other regions have demonstrated that the CR-estimated \( \text{ET}_a \) rates are realistic when compared with water-balance-based [e.g., Hobbins et al., 2001b; Liu et al., 2006; Ozdogan and Salvucci, 2004; Wang et al., 2011] and eddy-covariance-based [e.g., Han et al., 2013, 2014; Liu et al., 2012; Mallick et al., 2013, 2014] approaches. Recently, Brutsaert [2013] also confirmed the existence of an inverse trend between pan evaporation and \( \text{ET}_a \) in the TP using the CR. On the other hand, several researchers have argued that the CR deviated from Bouchet’s [1963] theory to a considerable extent in the arid and semiarid regions of the TP [Wang et al., 2013; Yang et al., 2011; Zhang et al., 2007]. Yu et al. [2009] ascribed this deviation to the limited vapor transfer potential at high altitudes because low air temperatures lead to low vapor pressure deficits. However, these studies did not apply locally calibrated parameter values. Applying the original parameter values most frequently encountered in the CR studies for the TP, where solar radiation and the wind are stronger but temperatures are lower, can lead to substantial errors, as was pointed out by Brutsaert [2013]. In fact, calibration of the CR parameter values at a regional basis may be important not only in the TP, but also in other regions. For instance, Xu and Singh [2005] and Hobbins et al. [2001b] concluded that the original parameter values of the CR would lead to evidently biased \( \text{ET}_a \) estimates in comparison with water-balance-derived \( \text{ET}_a \) values in the semiarid region of Cyprus and in the 139, only minimally altered, basins of the U.S., respectively.

With regard to vegetation cover, the CR approach has been tested in shrublands [Huntington et al., 2011; Jaksa et al., 2013], prairie [Crango and Crowley, 2005; Kahler and Brutsaert, 2006; Szilagyi, 2007], and cropland [Liu et al., 2012; Mallick et al., 2013; Ozdogan and Salvucci, 2004] over the past decade. These works have advanced our understanding of the CR theory involving different vegetation types, but not in conditions that exist in high altitudes. Consequently, with the help of the highest in situ automatic climate observation system in the alpine steppe region of the TP, the objectives of the present study are as follows. (1) Testing the existence of the CR in a high-altitude semiarid alpine steppe ecosystem. (2) Determination of the local parameter values of the CR to estimate daily evapotranspiration rates for the semiarid region of the TP. (3) Exploration of the specific relationship between observed daily \( \text{ET}_a \) and its maximum potential rate, the latter estimated with the help of evaporation pans as well as with the Penman equation [Penman, 1948]. (4) Evaluation of the CR-estimated daily actual evapotranspiration values.
2. Background of the Complementary Relationship

The complementary relationship of evapotranspiration was initially advanced by Bouchet [1963], emphasizing the feedback mechanism between $ET_a$ and $ET_p$ over a homogeneous area with minimum advection. Given a homogeneous surface with ample moisture, $ET_a = ET_p = ET_w$ where $ET_w$ is the wet environment evapotranspiration. Differentiation between $ET_p$ and $ET_w$ stems from the horizontal extent of the relevant wet area over which they are defined. For $ET_w$, it is large enough to modify its environment significantly. With limited water availability, $ET_a$ decreases. The energy that would have been consumed by $ET_a$ thus becomes sensible heat, thereby increasing $ET_p$, i.e.,

$$ET_p - ET_w = \varepsilon (ET_w - ET_a) \tag{1}$$

where $\varepsilon$ is a coefficient that depicts the proportion of the sensible heat that increases $ET_p$. When $\varepsilon$ equals unity, the unit decrease of $ET_a$ yields a corresponding unit increase of $ET_p$, signifying a symmetric CR (Figure 1a). This is the case for the widely applied advection-aridity (AA) model proposed by Brutsaert and Stricker [1979]. However, if the actual wet surface is too small (or too large) and/or some additional heat transfer exists (e.g., through the side and bottom of an evaporation pan), thereby altering the energy flux rate available for the wet surface, the rate of decrease in $ET_a$ would differ from the rate of increase in $ET_p$. In this case, $\varepsilon$ would deviate from unity, creating an asymmetric CR (Figure 1b). It should be noted that a strictly symmetric CR may be difficult to achieve due to the numerous limits imposed by actual conditions. Sugita et al. [2001] demonstrated that $\varepsilon$ can be expected to equal unity only when soil moisture is ample enough and the evaporation surface is largely smooth. Pettijohn and Salvucci [2006] suggested that surface conductance would affect the symmetry of the CR especially when transpiration accounts for a large part of $ET_a$.

3. Normalized CR and Practical Applications of $ET_p$ and $ET_w$

Following Brutsaert [2005], one can normalize the $ET_a$ and $ET_p$ values by dividing (1) with $ET_w$ to obtain dimensionless expressions, i.e.,

$$\frac{ET_a}{ET_w} = \frac{1 + \varepsilon}{1 + \frac{ET_a}{ET_p}} \tag{2}$$

$$\frac{ET_p}{ET_w} = \frac{1 + \varepsilon}{1 + \frac{ET_p}{ET_w}} \tag{3}$$

Under water-limited conditions, the $(ET_a/ET_p)$ term of (2) and (3) is mainly dependent upon the soil moisture and vegetation cover and could therefore be regarded as a land surface humidity index.
namely \( ET_w = ET_s/ET_p \) [Brutsaert, 2005; Kahler and Brutsaert, 2006]. On a daily scale, Kahler and Brutsaert [2006] found that \( ET_s \) is better than the total soil moisture content or antecedent precipitation index in capturing the availability of land surface moisture. By using the notation \( ET_s/ET_w = ET_s^{\ast +} \), \( ET_p/ET_w = ET_p^{\ast +} \), and \( ET_p/ET_w = ET_{pw} \), (2) and (3) can be written as

\[
ET_{pw} = \frac{(1+c)ET_{sh}}{1+cET_{sh}} \tag{4}
\]

\[
ET_p^{\ast +} = \frac{1+c}{1+cET_{sh}} \tag{5}
\]

According to Brutsaert and Stricker [1979], the \( ET_p \) term can generally be defined by the Penman [1948] equation

\[
ET_p = \frac{\Delta (R_n - G)}{(\Delta + \gamma)} + \frac{f(U)(e_o - e_a)}{(\Delta + \gamma)} \tag{6}
\]

where \( \Delta \) is the slope of the saturation vapor pressure curve at air temperature (kPa °C\(^{-1}\)), \( \gamma \) is the psychrometric constant (kPa °C\(^{-1}\)). \( R_n \) and \( G \) are net radiation and soil heat flux into the ground in units of mm d\(^{-1}\). \( e_o \) and \( e_a \) are the saturation and actual vapor pressure of the air (kPa), respectively. \( R(U) \) is the so-called Rome wind function [Brutsaert, 1982]

\[
f(U) = 2.6(1+0.54 U_2) \tag{7}
\]

a modification of Penman’s [1948] original empirical linear equation. \( U_2 \) is the wind speed (m s\(^{-1}\)) at 2 m height and \( R(U) \) is given in mm d\(^{-1}\) kPa\(^{-1}\).

Similarly, pan evaporation (\( E_{pan} \)) can also be regarded as an indicator of \( ET_p \), i.e.,

\[
ET_p = c E_{pan} \tag{8}
\]

where \( c \) is the so-called pan coefficient. The value of \( c \) depends not only on the environmental conditions but also on the pan type. There are a series of values for \( c \) for different pans around the world in the literature [e.g., Brutsaert, 2013; Pettijohn and Salvucci, 2009]. However, Kahler and Brutsaert [2006] are followed in adopting a value of unity for \( c = 1 \) in the present study. The same was also employed by Szilagyi [2007] and Pettijohn and Salvucci [2009]. The reasons for this assumption are twofold: (i) one of the goals of the present study is the evaluation of pan evaporation as \( ET_p \) within the CR theory, rather than the calibration of \( c \) for a specific pan type or area within the TP; (ii) when \( ET_p \) is replaced by \( c E_{pan} \) in equation (1), the uncertainty of the CR-based method of estimating \( ET_s \) could be compensated by the calibration of \( c \), as was pointed out by Kahler and Brutsaert [2006].

\( ET_w \) is closely approximated by the Priestley-Taylor equation [Priestley and Taylor, 1972] because it is mostly a function of available energy \( (R_n - G) \), satisfying the concept of wet environment evapotranspiration as defined by Bouchet [1963]

\[
ET_w = \frac{\Delta (R_n - G)}{\Delta + \gamma} \tag{9}
\]

Here \( ET_w \) is the wet environment evapotranspiration rate (mm d\(^{-1}\)), \( x \) is the dimensionless Priestley-Taylor coefficient, commonly having a default value of 1.26 [Priestley and Taylor, 1972], while other variables remain as in (6).

4. Site Description, Measurement, and Data Preparation

Alpine steppe is a very typical land cover in TP. It occupies nearly 1/3 of TP with total area of ~800,000 km\(^2\) [Miehe et al., 2011]. From a climatological point, it is principally distributed in the frigid and dry areas of TP [Yang et al., 2009] with altitude ranging from 4500 to 5500 m asl [Wang et al., 2014]. In the present research, an automatic climate observation system (ACOS) was established in September 2011 in the Shanghu alpine steppe (SAS) area (Figure 2), the hinterland of the Qiangtang plateau of the TP. The altitude of the observation site is 4947 m asl. Present alpine steppe was dominated by Stipa purpurea and Carex moocroftii. In the growing season, the mean canopy height and vegetation coverage are 0.03 m and 30%, respectively. The
soil of the homogeneous, flat area around ACOS, with a fetch in excess of 1 km for the prevailing wind is predominantly sandy loam. This region is characterized by a frigid semiarid climate [Zheng et al., 2013]. ACOS records reveal a mean annual temperature of $-4^\circ C$ from October 2011 to September 2013, with July temperatures of about $7^\circ C$, down to approximately $-15^\circ C$ in January. Records from the CMA station closest to the SAS reported annual precipitation of $\sim 333$ mm [Zheng et al., 2013] and annual $E_T$ of $\sim 1000$ mm [Wang et al., 2013]. The rainy season (June to September) accounts for more than 85% of the total annual precipitation. Since the glacier equilibrium line altitude in this region is roughly 5800 m asl [Yao et al., 2012], the present research represents the highest altitude in situ observations made in the alpine steppe ecosystem.

Table 1 displays details of the in situ observations of air temperature/humidity, pressure, wind speed/direction, radiation, soil heat flux, and soil temperature. All data were obtained as 10 min averages. Since the soil heat flux plate measured soil heat flux at a depth of 0.03 m, the temperature integration method [Oliphant et al., 2004] was used to interpolate heat storage between 0 and 0.03 m, using soil temperatures at depths of 0 and 0.05 m. Thus, the ground heat flux values, $G$, in the present study indeed represent heat fluxes into the ground surface rather than at a depth of 0.03 m. $G$ accounted for $\sim 7\%$ of $R_n$ at SAS on average (June to September), which is consistent with the theoretical proportion [Brutsaert, 2005], indicating reliable observational data.

In order to eliminate high-frequency noise, the raw 10 min measurements were processed to half-hourly average values. Then the half-hourly $E_T$ values were derived using the energy balance Bowen ratio method [Allen et al., 2011]. Finally, the 48 half-hourly $E_T$ values of the day were aggregated to calculate daily $E_T$. Although the recommended period of the CR application is 3–5 days [Morton, 1983], recent research indicate that daily $E_T$ can also be estimated accurately by CR theory [Han et al., 2013, 2014; Kahler and Brutsaert, 2006], consequently all evaluations in the present study are performed on a daily basis. Our aim is to investigate $E_T$ in the growing season (from October to May air temperature is typically below $0^\circ C$, and precipitation as well as plant physiological activity are also at a minimum). Data in the present study are therefore taken from the period of 4 June to 30 September in 2012 and 2013. Note that the observations (including pan evaporation data below) of 2013 were used to calibrate the parameter values in sections 5 and 6, while data of 2012 were employed to test the effectiveness of the CR-based method in estimating the daily actual evapotranspiration rates in section 7.

As was mentioned above, pan evaporation is a proxy of $E_T$. Daily pan
evaporation data from the same period (4 June to 30 September in 2012 and 2013) of two CMA meteorological stations in the relative vicinity of SAS were also utilized. One is the station at Naqu (28.71°N, 92.06°E, 4520 m asl, Figure 2), the other is at Amdo (32.25°N, 91.67°E, 4690 m asl, Figure 2), located 360 and 290 km to the southeast of the SAS, respectively. The pan at the Naqu is the China E601B model (for a photo, see Figure 1 in Ohmura and Wild [2002]), which is similar to the Russian GGI-3000 pan [World Meteorological Organization (WMO), 2008]. It is made of fiberglass with a depth of 0.687 m and a diameter of 0.618 m. The E601B pan is buried in the soil with its orifice 0.3 m above the ground surface [Xiong et al., 2012]. The pan at Amdo is the China D20 model (for a photo, see Figure 2 in Yang and Yang [2012]), made of copper with a depth of 0.1 m and a diameter of 0.2 m. The D20 pan is installed on a platform 0.7 m above the ground and has a rim acting as a bird guard. According to the WMO’s [2008] pan classification, the E601B pan (at Naqu) is a sunken pan, while the D20 pan (at Amdo) is an aboveground pan. Although these two stations are located at a somewhat lower altitude than SAS, the climatological background of both Naqu and Amdo are comparable to that of the SAS [Zheng et al., 2013]. It is therefore assumed that the main environmental factors influencing the pan evaporation rates at these stations and the actual ET$_a$ rates at the SAS are, to a large extent, similar. Figure 3 displays the variation of daily $E_{\text{pan}}$ of these two stations from 4 June to September in 2013. The variability of the $E_{\text{pan}}$ rates at these two stations match well, however, their magnitude express an obvious difference.

5. Local Calibration and Verification of the Key Parameter Values in CR at SAS

5.1. Alternative Formulation of the Wind Function for Calculating ET$_p$

Although the original wind function of Penman [1948] does not require boundary layer flow characterization, the ability of (6) with (7) to describe ET$_p$ accurately may depend on local environmental conditions. Linacre [1993] suggested that any wind function should be expressed by a certain range rather than a fixed formula. As both ET$_p$ and $E_{\text{pan}}$ rates are sensitive to wind speed in water-limited environments [Hobbins et al., 2001b; van Heerwaarden et al., 2010], it may be necessary to replace (7) with a more appropriate method. For daily (or longer) periods, atmospheric stability is often assumed to be neutral, hence Brutsaert and Stricker [1979] suggested the calculation of $f(U)$ via the Monin-Obukhov Similarity (MOS) theory [Monin and Obukhov, 1954] as

$$f(U) = \frac{0.622k \rho U_z}{\rho \ln \left( \frac{z_v - d}{z_m} - \psi_v \right)}$$  \hspace{1cm} (10)

$$U_z = \frac{U_{2_h} k}{\ln \left( \frac{z_v - d}{z_{om}} \right)}$$  \hspace{1cm} (11)

where $k$ is the von Karman constant (0.4), $\rho$ is the density of air (kg m$^{-3}$), $P$ is the air pressure (kPa), $t = 1d = 86,400$s, and $z_1$ is the height of humidity measurements (2 m in the present study). $d$ is displacement height (m), often taken to be $2h/3$ [Brutsaert, 2005], where $h$ is the mean canopy height (0.03 m at SAS). $U_z$ is the friction velocity (m s$^{-1}$), $U_{2_h}$ is the wind speed (m s$^{-1}$) at a height of $2_h$ (2 m in the present study), and $z_{om}$ is momentum roughness length (m) assumed to equal $h/8$ [Brutsaert, 2005]. $z_{ov}$ is the water vapor roughness length (m) and typically expressed as $z_{ov} = z_{om} \exp(-kB \nu^{-1})$, where $kB$ is a dimensionless number and can be assumed to equal 2 for a homogeneously vegetated surface [Pettijohn and Salvucci,
As Penman’s Rome wind function (7) was parameterized with wind measurements at a height of 2 m above ground equaling \( z_o \) in (11), a direct comparison between the two wind functions is displayed in Figure 4. The result indicates that (7) tends to overestimate \( f(U) \) when the mean daily wind speed is lower than 3.7 m s\(^{-1}\), but it underestimates it in stronger winds. Based on our observations, 67% of the daily wind speed values from June to September in 2013 at SAS were less than 3.7 m s\(^{-1}\). This suggests that the Penman Rome wind function (7) probably overestimates \( f(U) \) (and hence \( ET_w \)) in most days of the growing season at SAS. In order to distinguish \( ET_w \) based on (6) and (7), we denoted potential evapotranspiration as “\( ET_{p-c} \)” when the estimate was based on (6), with \( f(U) \) calculated by the MOS method (10).

5.2. Local Derivation of \( \Delta \) and \( z \) for Calculating \( ET_w \)

Since the Priestley-Taylor equation’s parameter value, \( \alpha \), was calibrated in a wet environment [Priestley and Taylor, 1972], Szilagyi and Jozsa (2008) proposed that the \( \Delta \) in (9) should be evaluated at the air temperature of the wet environment (\( T_{\text{wet}} \)) rather than the actual air temperature (\( T_a \)). This modification is especially significant when it is applied in arid/semiarid regions because of the possible large difference between \( T_{\text{wet}} \) and \( T_a \) under water-limited conditions [Huntington et al., 2011]. Also, previous studies have indicated that Brutsaert and Stricker’s [1979] AA model, based on a symmetric CR, tends to overestimate \( ET_w \) in arid and semiarid regions when \( ET_w \) is evaluated by \( T_a \) [Szilagyi et al., 2009; Szilagyi and Jozsa, 2008] since an overestimation of \( ET_w \) also yields an overestimation of \( ET_a \) as can be seen from (1)—applying \( \varepsilon = 1 \)—after rearrangement [Huntington et al., 2011], viz. \( ET_a = 2ET_w - ET_p \).

Unfortunately, it is not straightforward to determine \( T_{\text{wet}} \) from nonhumid observations. Szilagyi and Jozsa [2008] proposed obtaining \( T_{\text{wet}} \) by approximating it with the wet environment surface temperature, \( T_{\text{wes}} \), of a plot-sized wet patch, surrounded by water-limited conditions (arguing that the \( T_{\text{wes}} \) of the small wet patch is the same as that of an extensive wet area over which an equilibrium vertical temperature profile with typically small gradients develops, hence \( T_{\text{wes}} \approx T_{\text{wet}} \) as

\[
\beta_{\text{wes}} = \frac{Rn - G - ET_{p-c}}{ET_{p-c}} \approx \frac{T_{\text{wes}} - T_a}{e_s(T_{\text{wes}}) - e_a} \tag{12}
\]

where \( \beta_{\text{wes}} \) is the Bowen ratio of the wet patch (assuming that available energy for the wet patch is close to that of the drying surface), \( T_a \) is the actual air temperature in the surrounding water-limited environment, with actual vapor pressure of \( e_a \) at \( T_a \) and \( e_s(T_{\text{wes}}) \) being the saturated vapor pressure at \( T_{\text{wes}} \approx T_{\text{wet}} \), respectively. Equation (12) works, because over a small wet patch, air temperature and vapor pressure are only minimally affected by the presence of the wet surface, allowing for insertion of the measured, water-limited \( T_a \) and \( e_a \) values. In a recent study, Szilagyi and Schepers [2014] demonstrated the existence of a near-constant wet surface temperature over irrigated crops, supporting the above rationale behind (12).

Normally for this small wet patch, the \( \beta_{\text{wes}} \) is negative when the air is not near saturation, that is, we get the sensible heat flux downward fueling the latent heat flux, thus \( T_{\text{wes}} \) is typically lower than \( T_a \). Note that when the air is close to saturation, \( T_{\text{wes}} \) can be larger than \( T_a \); in such cases \( T_{\text{wes}} \) should be capped by \( T_a \) [Huntington et al., 2011; McMahon et al., 2013; Szilagyi, 2014]. With \( R_{\text{net}}, G, T_a \) and \( e_a \) measured by in situ observations,
$ET_{p-c}$ calculated by (6) and (10), the $T_{wes}$ ($\approx T_{wea}$) could therefore be obtained through an iterative process in (12). Similar to the shrublands of Nevada in the U.S. [Huntington et al., 2011], the difference between $T_a$ and $T_{wea}$ at SAS usually increases with the number of days of elevated $T_a$ (Figure 5).

With $T_{wea}$ estimated, (9) becomes

$$ET_{w-c} = 2\frac{A_{wea}(R_n - G)}{A_{wea} + \gamma}$$

(13)

where $A_{wea}$ (kPa °C$^{-1}$) is the slope of the saturation vapor pressure curve at $T_{wea}$, $ET_{w-c}$ now is the wet environment evapotranspiration rate calculated with $A_{wea}$ in place of $A$.

The most often cited value of 1.26 of the dimensionless Priestley-Taylor coefficient, $\alpha$, derived by Priestley and Taylor [1972], has no concrete physical significance because it was obtained as an average of a series of field experiments. It may therefore be necessary to specify $\alpha$ for local conditions [Hobbins et al., 2001b; Morton, 1983; Sugita et al., 2001; Xu and Singh, 2005]. Following Kahler and Brutsaert [2006], on wet days when $ET_a$ is close to $ET_{p-c}$ and therefore to $ET_{w-c}$, $\alpha$ can be estimated from the observed $ET_a$ values. In the present study, it is assumed that whenever $ET_a/ET_{p-c}$ is larger than 0.9, the $ET_{w-c}$ in (13) can be replaced by the observed $ET_a$; thus $\alpha$ could be recalculated. According to the observed data, there were 8 days in 2013 with $ET_a/ET_{p-c}$ ranging from 0.90 to 1.07, with a mean of 0.95 and a median of 0.92. Hence, an average $\alpha$ value of 1.13 was obtained from these 8 days. This value, smaller than the typically employed 1.26, is close to the fitted results of Szilagyi [2007] and Pettijohn and Salvucci [2006] who used daily flux data from a similar period of the year in the U.S. prairie. Yang et al. [2013] found a significant seasonal variation in the value of $\alpha$, being smaller in summer and larger in winter, mostly due to the impact of the monsoon. The observations in the present study come from June to September when the SAS was influenced by the Southern Asian monsoon, therefore the 1.13 value of $\alpha$ seems realistic.

When $ET_{p-c}$ is calculated by (6), coupled with the wind function of (10), and $ET_{w-c}$ is calculated via $A_{wea}$ in (13) with $\alpha = 1.13$, (1) can be rearranged for obtaining an estimate ($ET_{a-sim}$) of actual evapotranspiration as

$$ET_{a-sim} = \frac{(1 + e)ET_{w-c}/e}{ET_{p-c}/e}$$

(14)

6. The Relationship Between Actual and Potential Evapotranspiration

In order to check whether a CR exists at SAS on a daily scale, the relationship between daily $ET_a$ observed by the in situ ACOS, and the daily $ET_{p-c}$ is discussed below. $ET_a$ is first represented as $ET_{p-c}$ (i.e., calculated by (6) and (10)), then as $eC_{pan}$, with $e = 1$.

6.1. The Relationship Between Observed $ET_a$ and $ET_{p-c}$

Daily observed $ET_a$ and estimated $ET_{p-c}$ values are displayed in Figure 6a, against the humidity index, $ET_{hi}$ ($= ET_a/ET_{p-c}$). For a given $ET_{hi}$, the $ET_a$ and $ET_{p-c}$ values are scattered somewhat randomly due mainly to differences in net radiation. However, with $ET_{hi}$ increasing, $ET_a$ increases as well, while $ET_{p-c}$ does the opposite, indicating an inverse relationship with changes in surface moisture availability. Following Kahler and Brutsaert [2006], we inserted $ET_a$ $ET_{p-c}$ $ET_{w-c}$ into (4) and (5), and obtained the dimensionless form of $ET_a$ and $ET_{p-c}$ (Figure 6b). It is clear that the difference between $ET_a$ and $ET_{p-c}$ increases with the decrease in $ET_{hi}$, similar in shape to what Figure 1a depicts.

Since the estimation of $ET_{a-sim}$ using the CR is based on (14), a nested trial-and-error method was employed to optimize the value of $e$ to reach $\sum (ET_a - ET_{a-sim})^2 = \min [Szilagyi, 2007]$, where $ET_a$ is the observed daily value at SAS. The result, $e = 0.995$ (Figure 6b), indicates a symmetric CR in SAS when $ET_{p-c}$ is calculated using.
the Penman method, (6), with the wind function of (10); and $ET_{wc}$ is calculated using the Priestley-Taylor equation, with $\alpha = 1.13$ and $A_{\text{wca}}$ evaluated at $T_{\text{wca}}$. Our results contradict previous research which applied the default parameter value of wind function in (7) as well as $\alpha$ and evaluated $\Delta$ at $T_s$ in (9), and obtained an asymmetric CR in the semiarid and arid regions of the TP [Wang et al., 2013; Yang et al., 2011; Zhang et al., 2007]. In other words, the local determination of the parameter values within the CR is key to illuminating the true relationship between actual and potential evapotranspiration in the semiarid regions of the TP.

The observation site used for the present study is relatively homogeneous in its fetch in excess of 1 km for the prevailing wind, thus providing almost ideal conditions for the minimal energy advection requirement of the CR. This explains why the calibrated value of $\varepsilon$ equals 0.995, a value very close to unity. Our symmetric CR in the SAS is also in accordance with the findings of Huntington et al. [2011], who obtained a symmetric CR for Nevada shrublands through a similar calibration of the parameter values.

Since above three calibrations (wind function, $T_{\text{wca}}$ and $\alpha$) were carried out simultaneously to achieve a symmetric CR in the present study, it may be interesting to distinguish the relative importance of each calibration that when left out, leads to an asymmetric CR. This can be implemented by calibrating only two of three parameter values while keeping the other one unchanged and then searching for the optimized $\varepsilon$ for each scenario. Figure 7 illustrates that this way the CR becomes asymmetric (explaining why some [Wang et al., 2013; Yang et al., 2011; Zhang et al., 2007], applying no calibration, maintained an asymmetric CR in arid and semiarid region of the TP). Specifically, if the wind function was left uncalibrated, the $\varepsilon$ became 0.946; when $T_{\text{wca}}$ was left uncalibrated, the $\varepsilon$ became 0.886; and when the $\alpha = 1.26$ was employed, the $\varepsilon$ became 0.654. This suggests the local calibration of $\alpha$ is most important, followed by the $T_{\text{wca}}$ correction, while the wind function may play the smallest role in leading to an asymmetric CR.

6.2. The Relationship Between Observed $ET_a$ and $cE_{\text{pan}}$

With the assumption of $\varepsilon = 1$ in (8), the daily evaporation rates of the E601B pan at Naqu and the D20 pan at Amdo were used to evaluate the relationship with daily observed $ET_a$ of the SAS (Figure 8). The $E_{\text{pan}}$ values in both stations display an inverse relationship with the observed $ET_a$ at SAS when plotted against $ET_{HI}$ ($ET_a/cE_{\text{pan}}$). Moreover, the pan at Amdo (D20 aboveground pan) is more sensitive to changes in $ET_a$ than the one at Naqu (E601B sunken pan) (Figure 8). The reason for this phenomenon will be discussed later.

The CR between observed $ET_a$ and $E_{\text{pan}}$ at both Naqu and Amdo becomes more obvious when the dimensionless rates, $ET_a^* (= ET_a/ET_{wc})$ and $E_{\text{pan}}^* (= cE_{\text{pan}}/ET_{wc})$ are plotted against the humidity index, $ET_{HI}$ ($= ET_a/cE_{\text{pan}}$), in Figure 9. Employing the $E_{\text{pan}}$ data from the two stations and the $ET_a$ values at SAS from 4 June 2013 to 30 September 2013, the nested trial-and-error method was applied again to calibrate $\varepsilon$, which became 2.359 for the E601B sunken pan at Naqu, and 3.863 for the D20 aboveground pan at Amdo, both displaying an asymmetric CR when pan evaporation ($c = 1$) rates are used to represent $ET_p$ (Figure 9).

It is not surprising that $\varepsilon$ is larger than unity for the pans in the present study. This is especially true for the D20 aboveground pan because similar values have already been obtained with class-A aboveground pans,
employed as a proxy of ET [Kahler and Brutsaert, 2006; Pettijohn and Salvucci, 2009; Szilagyi, 2007; Szilagyi and Jozsa, 2008]. Clearly, the additional solar radiation received by the side of the aboveground pans and the significant heat advection from the surrounding environment due to the pans’ small orifice area boost the available energy to the pans. In addition, the dynamics of heat storage of water in the pans may also significantly impact the ET, especially on a daily scale [Roderick et al., 2009]. However, the value of ε for the D20 aboveground pan in the present study is somewhat smaller than the values reported for class-A

Figure 7. Normalized daily actual and estimated potential evapotranspiration rates plotted against the humidity index, same as in Figure 6b, but only two calibrations were implemented. For (a) without wind function replacement, namely ETa1 (∝ ETa/ETw-c), ETp1 (∝ ETp/ETw-c), ETw-c (∝ ETa/ETp); (b) without Tw-c calibration, namely ETa1 (∝ ETa/ETw-c-1), ETp1 (∝ ETp/ETw-c-1), ETw-c (∝ ETa/ETp-1); (c) without z calibration, namely ETa2 (∝ ETa/ETw-c-2), ETp2 (∝ ETp/ETw-c-2), ETw-c (∝ ETa/ETp-2). Note that the ETw-c was split to ETw-c-1 (z = 1.13, but Δ is based on Ta) and ETw-c-2 (Δw-c is based on Tw-c, but z = 1.26) to represent only z or Ta as being calibrated, respectively. The black curves represent (4) and (5) with a calibrated value of (a) 0.946, (b) 0.886, (c) 0.654 for ε, respectively.

Figure 8. Observed daily actual (ETa) and estimated daily potential [ETp = cETpan (c = 1)] evapotranspiration rates plotted against the humidity index (ETHI = ETa/cETpan) at SAS. The ETpan values are from (a) an E601B sunken pan at Naqu and from (b) a D20 aboveground pan at Amdo.
aboveground pans over the Konza Prairie ($\epsilon = 4.33$) and Little Washita River Basin ($\epsilon = 6.88$) in the U.S. by Kahler and Brutsaert [2006]. This may be caused by differences in the pans’ orifice areas and installation.

As the orifice area of the E601B sunken pan is still only 0.3 m$^2$, the heat advection cannot be neglected. This leads to its $\epsilon$ larger than unity. The reason that the E601B pan is less sensitive than the D20 pan (Figures 8 and 9) is that it is a sunken pan which leads to reduced heat conduction through the side of the pan and therefore decreased diurnal heat storage effect. As shown above, the CR became symmetric when the Penman equation (using MOS for the wind function) was used to estimate $ET_{p-c}$. It should be noted that Penman [1948] validated his equation using two types of sunken pans: both having a diameter of 0.76 m, but their depths were 0.61 and 1.83 m, respectively. His wind function was later modified (to the so-called Rome wind function of [7]) to give better estimates for plot-sized ponds or wet surfaces, since his original wind function yielded higher $ET_p$ rates due to heat conduction and advection effects, significant for small evaporation pans.

7. Performance of the CR-Based Daily Actual Evapotranspiration Estimates

After deriving the optimized $\epsilon$ with observed data from 2013, it is important to test the effectiveness of the CR-based method in a different, verification time period, chosen to be 2012.

7.1. The Penman Method

As discussed in section 6.1, the CR became symmetric ($\epsilon = 0.995$) with the Penman equation using the MOS-derived wind function for the $ET_{p-c}$ estimates and $\Delta_{w-c}$ evaluated at $T_{w-c}$ for the $ET_{w-c}$ estimates. In order to test
the performance of the CR using its original parameter values, called the original AA model, i.e., $ET_a = 2ET_w - ET_p$ [Brutsaert and Stricker, 1979], (6), (7), and (9) were employed using the data of 2012 (Figure 10a). The daily $ET_a$ sim values are clearly larger than the observed daily $ET_a$ rates, although their correlation is good. The mean-absolute-error (MAE) and root-mean-square-error (RMSE) are as high as 0.86 and 0.994 mm, respectively. The Nash-Sutcliffe efficiency (NSE) coefficient is 0.352 (Table 2), indicating a poor performance of the original AA model. When the $w$ function in (6) was replaced by the MOS-based approach, (10), and $ET_w$ was evaluated at $T_{wab}$ using (13) with $c = 1.13$, the MAE and RMSE values decreased to 0.40 and 0.512 mm, respectively (Table 2). The NSE increased to 0.642, indicating a greatly improved agreement with observed daily $ET_a$ in 2012 (Figure 10b).

It is not true only for the SAS that the CR-based estimates can be improved with local calibration of the parameter values. For instance, Crago et al. [2010] confirmed that the MOS-based wind function performed better than Penman’s [1948], in their AA approach over a Kansas grassland [see Crago et al., 2010, Figures 2 and 3]. Besides, Huntington et al. [2011] compared the results of their CR-based $ET_a$ estimation method in the shrublands of Nevada, when $T_a$ was replaced by the Szilagyi and Jozsa [2008] estimate of $T_{wab}$ to calculate $ET_w$, and found that the latter improved the $ET_a$ estimates [see Huntington et al., 2011, Figure 9]. Recently, Szilagyi [2014] also found the bias of AA model in estimating $ET_a$ in a semiarid savanna in Botswana could be reduced from 53% to 23% when the $T_a$ was replaced with the $T_{wab}$ in calculating the $ET_w$. In the present study, the employment of an MOS-based wind function, local calibrated $c$, and $T_{wab}$ together may explain the success of $ET_a$ sim by (14) at SAS (Figure 10b).

### 7.2. The Pan Evaporation Method

As discussed in section 6.2, the CR is asymmetric with pan evaporation values for $ET_p$. By insertion of the $cE_{pan}$ ($c = 1$) values into $ET_p, cE_{pan}$ of (14), $ET_a$ sim in 2012 was calculated (Figure 11). Note that $c$ is 2.359 for the E601B pan and 3.863 for the D20 pan in (14). The Pearson correlation values between the observed $ET_a$ and $ET_a$ sim are 0.692 and 0.742 when the E601B and D20 pans are used, respectively. The performance of the E601B pan is not as good as that of the D20 pan (Figure 11). The former tends to overestimate $ET_a$ to some extent with MAE and RMSE values of 0.79 and 1.030 mm, respectively, and an NSE of 0.450 (Table 2). This maybe because the local advection influence on the E601B pan at Naqu station in 2012 and 2013 was

### Table 2. Evaluation of the CR-Based Daily $ET_a$ Estimates in 2012

<table>
<thead>
<tr>
<th></th>
<th>$ET_p$ From Penman, Symmetric CR</th>
<th>$ET_p$ From Epan, Asymmetric CR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$2ET_w$ $ET_p$</td>
<td>$2ET_w-E_{pan}$ $(E601B)$</td>
</tr>
<tr>
<td>CC</td>
<td>0.804</td>
<td>0.692</td>
</tr>
<tr>
<td>NSE</td>
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<td>−0.450</td>
</tr>
<tr>
<td>MAE</td>
<td>0.86</td>
<td>0.79</td>
</tr>
<tr>
<td>RMSE</td>
<td>0.994</td>
<td>1.030</td>
</tr>
<tr>
<td></td>
<td>$ET_w$ $ET_p$</td>
<td>$ET_w-E_{pan}$ $(D20)$</td>
</tr>
<tr>
<td>CC</td>
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<td>0.742</td>
</tr>
<tr>
<td>NSE</td>
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<td>0.455</td>
</tr>
<tr>
<td>MAE</td>
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<td>0.48</td>
</tr>
<tr>
<td>RMSE</td>
<td>0.512</td>
<td>0.631</td>
</tr>
</tbody>
</table>

*CC, correlation coefficient; NSE, Nash-Sutcliffe efficiency coefficient; MAE, mean absolute error (mm); and RMSE, root-mean-square error (mm).
8. Conclusions

Although LeDrew [1979] argued that the CR theory could not be validated for a daily time scale, daily observed actual evapotranspiration and estimated potential evapotranspiration did indeed express complementarity in a semiarid alpine steppe of the TP. This is significant because, with the help of the CR theory, the ET<sub>a</sub> rates can be estimated from routine meteorological observations, even though TP is known as sparsely observational. Future work should determine the locally calibrated parameter values, similar to the present study, for different vegetation cover types and climatic regions of the TP for ET<sub>a</sub> estimation methods that employ the CR theory, and thus aiding the work toward a successful estimation of ET<sub>a</sub> for the entire TP.

With the MOS-based wind function for calculating ET<sub>P-C</sub>, a Priestley-Taylor coefficient value of α = 1.13, and estimated wet environment air temperature for calculating ET<sub>WC</sub>, the CR became symmetric in a high-altitude semiarid alpine steppe in the TP. Hence, it is believed that previous research [Wang et al., 2013; Yang et al., 2011; Zhang et al., 2007], claiming that the CR is asymmetric in the arid and semiarid regions of the TP, may have resulted simply from employing the original parameter values of the CR-based AA model. The application of the MOS-based wind function as well as an estimate of the wet-environment air temperature together with a local calibration of α, all emphasized by Brutsaert [2013], are all recommended as necessary building blocks for the correct evaluation of the CR within the TP. Among them, the local calibration of α is most important, followed by the T<sub>wea</sub> correction; while the replacement of the classical wind function with an MOS-based one plays the least important role in leading to a symmetric CR. The resulting daily ET<sub>a-sim</sub> estimates via the symmetric CR yielded good agreement with the observed daily ET<sub>a</sub> at the present semiarid alpine steppe.

Daily pan evaporation, E<sub>pan</sub>, from the two CMA stations employed, displayed a clear inverse trend in comparison with daily observed ET<sub>a</sub> of the SAS. Radiation received by the side of the pan, nonnegligible heat advection due to the pan’s small orifice area [Szilagyi and Jozsa, 2008] and the dynamics of heat storage of the pan water [Roderick et al., 2009] led to an asymmetric CR when using E<sub>pan</sub> for ET<sub>P</sub>. This is true not only for the D20 aboveground pan but also for the E601B sunken pan, because the effect of heat advection is still present for sunken pans, even if heat conduction is much reduced within the soil. Finally, the D20 aboveground pan performed better than the E601B sunken pan in estimating the actual evapotranspiration rate of a semiarid alpine steppe via the CR theory.

In summary, the benefit of a symmetric CR is that it dispenses with one parameter (α), thus allowing for a simpler calibration and application of the CR in estimating actual evapotranspiration [Brutsaert, 2005; Crago and Qualls, 2013]. While the current analysis of the CR with E<sub>pan</sub> does not contribute to the attainment of the symmetry, it provides important clue for historical reasons [Brutsaert and Parlange, 1998], since long time series of E<sub>pan</sub> measurements exist and may be helpful for detecting the trends of terrestrial ET<sub>a</sub> associated with the long-term climate change.

Acknowledgments

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