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## **Band structure and spin texture of Bi<sub>2</sub>Se<sub>3</sub> 3***d* **ferromagnetic metal interface**

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The spin-helical surface states in a three-dimensional topological insulator (TI), such as  $Bi_2Se_3$ , are predicted to have superior efficiency in converting charge current into spin polarization. This property is said to be responsible for the giant spin-orbit torques observed in ferromagnetic metal/TI structures. In this work, using first-principles and model tight-binding calculations, we investigate the interface between the topological insulator  $Bi_2Se_3$ and 3*d*-transition ferromagnetic metals Ni and Co. We find that the difference in the work functions of the topological insulator and the ferromagnetic metals shift the topological surface states down about 0.5 eV below the Fermi energy where the hybridization of these surface states with the metal bands destroys their helical spin structure. The band alignment of  $Bi<sub>2</sub>Se<sub>3</sub>$  and Ni (Co) places the Fermi energy far in the conduction band of bulk Bi<sub>2</sub>Se<sub>3</sub>, where the spin of the carriers is aligned with the magnetization in the metal. Our results indicate that the topological surface states are unlikely to be responsible for the huge spin-orbit torque effect observed experimentally in these systems.

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#### **I. INTRODUCTION**

Topological insulators (TIs) represent a state of matter which is insulating in the bulk, but exhibits gapless surface states protected by time reversal symmetry  $[1-3]$ . Threedimensional (3D) TIs have been discovered among the  $Bi<sub>2</sub>Se<sub>3</sub>$ family of materials. Their properties were elaborated from first-principles calculations  $[4-7]$  and the signature Dirac cone was observed experimentally in the angle-resolved photoemission spectroscopy (APRES) experiments [\[8–10\]](#page-6-0). A key feature of carriers in the topologically protected surface state is the locking between their spin and momentum, which are constrained to be perpendicular by the strong spin-orbit coupling (SOC) [\[2,3\]](#page-6-0). This property has been proposed as the foundation of applications based on TIs.

Magnetization switching in nanoscale devices induced by the electric current is one of the most researched applications in recent years [\[11\]](#page-6-0). In particular, the magnetization switching via spin-orbit torque (SOT) has been demonstrated in ferromagnetic (FM) layers interfaced with heavy metals with strong SOC, such as Pt  $[12,13]$  or Ta  $[14]$ . There are two physical mechanisms contributing to SOT. First, when the charge current passes along the FM layer, the SOT is produced by the interfacial Rashba SOC [\[12\]](#page-6-0). Second, when the current passes along the adjacent metal layer, the bulk spin Hall effect (SHE) in that layer produces spin accumulation at the interface exerting SOT on the magnetization of the ferromagnet [\[14\]](#page-6-0).

It has been proposed that the spin-helical surface states of TIs would be more efficient than heavy metals with strong SOC in converting charge to spin current and producing SOT [\[15\]](#page-6-0). Indeed, there have been reports of giant SOT arising at the interface between a topological insulator and ferromagnet (NiFe or CoFeB) [\[16,17\]](#page-6-0) or another magnetically doped topological insulator (Cr-doped BiSbTe<sub>3</sub>)  $[18]$ . The explanation for this high efficiency is rooted in the assumption that the charge current is carried predominantly by the surface state of the TI and the spin accumulation produced by the spin-momentum locking is much larger than it would be in nontopological materials with SOC of a similar magnitude [\[16](#page-6-0)[,19,20\]](#page-7-0).

Due to the importance of the spin texture of the surface state, the question arises of its robustness when TI is interfaced with a metal. The spin texture of the pure surface state in  $Bi<sub>2</sub>Se<sub>3</sub>$ has been studied in model and first-principles calculations  $[6,7,21,22]$  $[6,7,21,22]$ . It has been shown theoretically that the surface state is robust with respect to disorder, if the perturbation is sufficiently small [\[23\]](#page-7-0), as well as with respect to moderate doping with Mn atoms [\[24\]](#page-7-0). Similarly, it has been demonstrated from model calculations that at TI/metal interfaces the surface state survives, provided that the bonding is weak [\[19\]](#page-7-0). The surface transport in  $Bi<sub>2</sub>Se<sub>3</sub>$  has been confirmed experimentally by measuring the thickness dependence of the conductance of TI slabs [\[25\]](#page-7-0). Spin polarization has been probed by injecting energetic electrons in  $Bi<sub>2</sub>Se<sub>3</sub> [26]$  $Bi<sub>2</sub>Se<sub>3</sub> [26]$ . However, band gap opening and magnetization reorientation associated with Mn doping have been reported [\[27\]](#page-7-0). In addition, first-principles calculations revealed that the TI surface states at the Bi<sub>2</sub>Se<sub>3</sub>/MnSe interface are gapped due to proximity of the magnetic insulator MnSe [\[28,29\]](#page-7-0).

Thus, the existing studies of the robustness of the spinhelical surface states are mostly limited, so far, to dilute doping with impurities, weak coupling regime, or TI/FM insulator interface. The properties of TI/FM metal interfaces have not been studied in sufficient detail. In this paper we use density-functional calculations to investigate the electronic and magnetic structure of  $Bi<sub>2</sub>Se<sub>3</sub>$  interfaces with the FM metals Ni and Co. In order to elucidate the mechanism of the interaction of the TI surface state with the FM metal, we complement the first-principles calculations with tight-binding model studies of TI/FM metal and insulator interfaces. Our results show that the strong hybridization at the TI/FM metal interface largely destroys the topologically protected state with its spin-helical structure.

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<span id="page-2-0"></span>

FIG. 1. (a) Supercell structure of  $Bi<sub>2</sub>Se<sub>3</sub>(3QLs)/Ni<sub>2</sub>Co(6 MLs)$ . (b) Alternative interface terminations at  $Bi<sub>2</sub>Se<sub>3</sub>$  (0001) and Ni, Co (111) interface. (c) Band dispersion of  $3QL-Bi<sub>2</sub>Se<sub>3</sub>$  (0001) slab along the high symmetry lines with the inset showing bands around the Fermi energy (left). Spin texture of TI surface states at  $E = E_F +$ 0.2 eV and  $E = E_F + 0.4$  eV (right).

#### **II. FIRST-PRINCIPLES CALCULATIONS**

The atomic structure model for the  $Bi<sub>2</sub>Se<sub>3</sub>/Ni(111)$  interface is shown in Fig.  $1(a)$ . The Bi<sub>2</sub>Se<sub>3</sub> has hexagonal symmetry and the atomic structure along the (0001) direction consists of quintuple layers (QLs) of two Bi layers sandwiched between three Se layers. We use the experimental lattice constants  $a = 4.138$  Å and  $c = 28.640$  Å [[6\]](#page-6-0). The  $\sqrt{3} \times \sqrt{3}$  rotated (111) surface of the fcc Ni matches the  $Bi<sub>2</sub>Se<sub>3</sub>$  with less than 4.1% mismatch. The two interface terminations considered are shown in Fig.  $1(b)$ . The same structural model is used for constructing the Bi2Se3*/*Co(111) interface.

The calculations are carried out by using the Vienna *ab initio* simulation package (VASP) [\[30\]](#page-7-0). The Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation is used for the exchange-correlation potential [\[31\]](#page-7-0). The calculations are performed in the presence of SOC  $[32,33]$ . The selfconsistency cycle is run using  $16 \times 16 \times 1$  *k*-point grid in the Brillouin zone and the plane-wave energy cutoff of 450 eV. The density of states (DOS) and the magnetocrystalline anisotropy energy (MAE) are calculated with a finer  $32 \times 32 \times 1$  *k*-point

TABLE I. Calculated interface properties: the equilibrium interface layer distance  $d_0$ , work of separation  $W_{\text{sep}}$ , and MAE. The corresponding reference values for (Ni,Co)/Gr(graphene) and Fe/MgO interface are listed for comparison.

Interface		$Bi2Se3/Ni$ $Bi2Se3/Co$ $Gr/Ni$ $Gr/Co$ $Fe/MgO$			
Mismatch	$4.1\%$	$4.7\%$		$1.3\%$ 1.9%	$-3.8\%$
$d_0(\AA)$	2.05	2.11	2.05	2.05	2.167
$W_{\rm sep}$ (J/m <sup>2</sup> )	1.10	1.08	0.386		$0.495$ $0.97-1.36$
MAE (erg/cm <sup>2</sup> )	$-2.18$	0.52			$1 - 1.5$

grid. The QL-QL distance is fixed to the experimental value to avoid the necessity of including the van derWaals interaction in our calculations. All other atomic coordinates and the supercell dimension along the *c*-axis direction are allowed to relax until the force on all atoms is less than  $1 \text{ meV}/\text{\AA}$ .

First, we calculate the band structure of a free-standing  $3QL-Bi<sub>2</sub>Se<sub>3</sub>$  (0001) slab. The results are displayed in Fig. 1(c). There are two surface states localized at the top and bottom surfaces of the slab, which have the opposite spin helicities [\[7\]](#page-6-0). We note that due to the finite thickness of the slab, the coupling between the two surface states produces a band gap at the  $\Gamma$  point [see inset of Fig. 1(c)]. The spin of each Bloch state is evaluated through the expectation value of the spin operator  $S_{n,\mu}(\vec{k}) = \frac{\hbar}{2} \langle \psi_n(\vec{k}) | \sigma_\mu | \psi_n(\vec{k}) \rangle$  ( $\mu = x, y, z$ ). The calculated spin textures corresponding to the top surface states of the slab at 0.2 and 0.4 eV above the Fermi energy are shown in Fig. 1(c) (right panels). The spins lie entirely in the plane with the out-of-plane component  $S<sub>z</sub>$  being negligible. The important consequence of such a spin texture is that it carries spin density when charge current flows on the surface, resulting in the transport spin polarization [\[16\]](#page-6-0).

Next, consider the  $Bi<sub>2</sub>Se<sub>3</sub>/Ni(Co)$  supercell which contains 3 QLs of  $Bi<sub>2</sub>Se<sub>3</sub>$  and 6 monolayers (MLs) of Ni or Co [Fig.  $1(a)$ ]. The A-type interface is found to be more energetically favorable [Fig.  $1(b)$ ] with a lower total energy by 0.5 eV. In Table I we summarize the properties of the interface, and to put them in perspective, compare them to the wellstudied graphene/Ni(Co) [\[34\]](#page-7-0) and Fe/MgO [\[35\]](#page-7-0) interfaces. The calculated equilibrium interface distances between Se and Ni (Co) planes is 2.05 (2.10) Å. The work of separation  $W_{\text{sep}}$ for Bi2Se3*/*Ni(Co) is larger than that for graphene/Ni(Co) and comparable to that for the CoFe/MgO interface, which indicates strong bonding at the Bi2Se3*/*Ni(Co) interface. The MAE per interface is calculated as  $MAE = \frac{1}{2}(E_{M_x} - E_{M_z})$ , where  $E_{M_x}$  and  $E_{M_y}$  are the total energies for magnetization pointing along the *x* and *z* directions, respectively. Within this definition, positive MAE implies the easy axis pointing along *z* direction (i.e., perpendicular anisotropy). As is evident from Table I, the  $Bi<sub>2</sub>Se<sub>3</sub>/Ni(111)$  interface exhibits in-plane anisotropy, whereas the  $Bi<sub>2</sub>Se<sub>3</sub>/Co(111)$  interface exhibits out-of-plane (perpendicular) anisotropy.

Figures  $2(a)$  and  $2(b)$  show the band structure of the Bi<sub>2</sub>Se<sub>3</sub>/Ni(111) and Bi<sub>2</sub>Se<sub>3</sub>/Co(111) supercells, respectively. Here the bands are projected onto  $Bi<sub>2</sub>Se<sub>3</sub>$  and Ni (Co), as indicated by the color. Due to the large electrostatic mismatch, charge flows from the metal into the conduction band of  $Bi<sub>2</sub>Se<sub>3</sub>$ , as seen from the relatively large DOS on the first

<span id="page-3-0"></span>

FIG. 2. Band structure and corresponding density of states (DOS) of the  $Bi_2Se_3/Ni(111)$  (a) and  $Bi_2Se_3/Co(111)$  (b) interfaces. The color intensity is proportional to the projected weight of the bands on  $Bi_2Se_3$  (red) and Ni(Co) (white). The black dots indicate the position of the Dirac cone in a stand-alone Bi<sub>2</sub>Se<sub>3</sub> (0001) surface. (c) and (d) The total spin (indicated by vectors) and spin components  $(S_x, S_y, S_z)$  indicated in color at  $E = E_F$  around the Brillouin zone center for  $Bi_2Se_3/Ni(111)$  and  $Bi_2Se_3/Co(111)$ , respectively.

QL of the TI [Figs.  $2(a)$  and  $2(b)$ , right panels]. Comparing the  $Bi<sub>2</sub>Se<sub>3</sub>$  bands in the supercells [Figs.  $2(a)$  and  $2(b)$ , red color] with those of the free-standing slab [Fig.  $1(c)$ ], we observe that the remnant of the Dirac cone appears about 0.5 eV below the Fermi level. The position of the Dirac cone can be explained by the mismatch of the work functions of  $Bi<sub>2</sub>Se<sub>3</sub>(0001)$  and Ni(Co)(111). As seen from Table II, the calculated work function of  $Bi<sub>2</sub>Se<sub>3</sub>$  is 0.48 (0.51) eV higher than that of Ni (Co). Thus, the Dirac point falls fairly deep in the conduction band of the metals. This circumstance explains the fairly modest MAE calculated at these interfaces (Table [I\)](#page-2-0). The MAE is expected to be most pronounced when the Dirac cone is around the Fermi level.

Furthermore, we study the effect of the hybridization on the spin texture. Here and below we consider the magnetization of the ferromagnet (Ni or Co) pointing perpendicular to the plane,

TABLE II. Work functions of  $Bi<sub>2</sub>Se<sub>3</sub>$  (0001), Co (111), and Ni (111) slabs. The atomic structure of the Ni and Co slabs is taken from the relaxed  $Bi<sub>2</sub>Se<sub>3</sub>/Ni(Co)$  supercell structure.

Material	$3OL-Bi2Se3$ Ni slab Co slab Gr			
$W$ (eV) GGA+SOC (This work)	5.67	5.19	5.16	
$Wref$ (eV) $LDA + NSOC$		-5.47	5.44	4.48
$W_{\text{expt}}$ (eV)		5.35	5 O	46

i.e., along the *z* direction. First, we look at the spin texture around the Fermi energy. The  $S_x$ ,  $S_y$ , and  $S_z$  projections for the spin of the bands at the Fermi energy near the Brillouin zone center are shown in Figs.  $2(c)$  and  $2(d)$  for Ni and Co, respectively. We see that the spin is pointing along the magnetization direction of the ferromagnet and the in-plane spin components  $S_{\parallel}$  show a complicated spin texture with absolute values one order of magnitude smaller than S*z*. This result is not surprising due to absence of the Dirac states at the Fermi energy. The electrostatic mismatch at the interface places the Fermi energy far in the conduction band of the bulk  $Bi<sub>2</sub>Se<sub>3</sub>$  where the hybridization between the TI and FM states induces an exchange splitting of the TI spin bands with an effective exchange field pointing along the FM magnetization. Transport as well as SOT properties are largely controlled by the Fermi surface, and therefore this result indicates that it is unlikely that the topological states contribute to these properties in the Bi<sub>2</sub>Se<sub>3</sub>/Co(Ni) (111) system.

Now we discuss the remnant of the Dirac states lying at about 0.5 eV below the Fermi energy. As seen from Figs.  $3(a)$ and  $3(b)$ , only the upper branch of the original topological state remains. The lower branch is smeared out both for Bi<sub>2</sub>Se<sub>3</sub>/Ni and  $Bi<sub>2</sub>Se<sub>3</sub>/Co$  interfaces. The upper branch consists of two subbands [indicated by black and green solid lines in Figs.  $3(a)$ ] and  $3(b)$ ], originating from the two interfaces in the supercell structure. The degeneracy of these subbands is lifted due to

<span id="page-4-0"></span>

FIG. 3. Band structure of the  $Bi_2Se_3/Ni(111)$  (a) and  $Bi_2Se_3/Co(111)$  (b) interfaces around the remnant Dirac state. The color intensity is proportional to the projected weight of the bands on  $Bi_2Se_3$  (red) and Ni(Co) (white). The black and green solid lines indicate the remnant of Dirac state at Bi<sub>2</sub>Se<sub>3</sub>/Co(Ni) interface. The dashed blue line indicates the TI surface state shifted according to the calculated work function mismatch. (c) and (d) The layer resolved band weight of the interface at the  $\Gamma$  point. The arrows indicate the magnetic moment direction in ferromagnetic metals Ni and Co. (e) and (f) The spin texture of remnant Dirac states at the  $Bi_2Se_3/Ni(111)$  and  $Bi_2Se_3/Co(111)$  interfaces at  $E = E_F - 0.45$  eV and  $E = E_F - 0.5$  eV as indicated by the horizontal dash black line in (a) and (b), respectively.

the effective exchange field produced by the magnetization of the ferromagnet pointing in the opposite direction with respect to the normal to each TI surface. The Dirac states at the  $Bi<sub>2</sub>Se<sub>3</sub>/Ni$  interface are hybridized stronger with the metal bands (due to their overlap with the Dirac states), as compared to the  $Bi<sub>2</sub>Se<sub>3</sub>/Co$  interface where the hybridization is weaker. By looking at the layer resolved band weight of these states at the  $\Gamma$  point [Figs. 3(c) and 3(d)], we see that the bands have higher weight at the interfaces, as expected for surface (interface) states. In case of Bi<sub>2</sub>Se<sub>3</sub>/Ni, however, each of the two bands has nearly equal weight at the two interfaces [Fig. 3(c)], whereas in case of Bi2Se3*/*Co each of the two bands is peaked at one of the two interfaces [Fig.  $3(d)$ ]. The latter behavior is expected for the topologically protected surface states, whereas the former indicates that the two surface states are mixed through hybridization with the metal states.

Based on this result we can expect that the corresponding spin texture of the remnant Dirac bands in  $Bi<sub>2</sub>Se<sub>3</sub>/Ni$  and  $Bi<sub>2</sub>Se<sub>3</sub>/Co$  will be different. Indeed, as is evident from Fig. 3(e) the spin texture of the Dirac state in  $Bi<sub>2</sub>Se<sub>3</sub>/Ni$  is completely destroyed, so that it has negligible in-plane spin components  $S_x$  and  $S_y$ , whereas the  $S_z$  component is large. For  $Bi_2Se_3/Co$ , however, as seen from Fig.  $3(f)$ , the spin texture of the Dirac state is largely preserved and the interface state has a helical spin structure with negligible  $S<sub>z</sub>$  component. We note however that in either case, due to of the remanent Dirac states lying far below the Fermi energy, they are not expected to contribute to the spin-dependent transport and SOT.

<span id="page-5-0"></span>

FIG. 4. (a) Schematic diagram of the band structure of a topological insulator (TI) and a ferromagnet (FM). (b) Bloch spectral density of a stand-alone TI surface. (c) Spectral density of TI/FM insulator interface for  $\varepsilon_0 = 3.5$ ,  $t_0 = -0.5$  eV,  $\Delta = 0.5$  eV, and interface coupling strength  $\xi = t/t_0 = 0.5$ , 1, and 2. (d) Spectral density of TI/FM metal interface for  $\varepsilon_0 = 2.5$ ,  $t_0 = -0.5$  eV,  $\Delta = 0.5$  eV.

In order to see how the topological surface state recovers when the interface coupling strength is decreasing, we have calculated the band structure of  $Bi<sub>2</sub>Se<sub>3</sub>/Ni(111)$  while gradually increasing the interface distance between TI and the ferromagnet with respect to equilibrium by *δd* (Fig. [1\(a\),](#page-2-0) Supplemental Material [\[36\]](#page-7-0)). We find that with the increasing separation the hybridization decreases and, respectively, the Dirac cone becomes more pronounced and moves up in energy. When the interface separation is increased to be  $\delta d = 3.0 \text{ Å}$ , the dispersions expected for the topological surface states appear with a 30 meV gap due to the magnetic proximity effect. However, the helical spin texture is still not recovered (Figs.  $1(b)$  and  $1(c)$ , Supplemental Material [\[36\]](#page-7-0)). Thus, even a very weak interface coupling seems to be detrimental to the spin texture of the surface state of the TI. Only at interface separations of as large as  $\delta d = 8$  Å, the surface state resembles that of a free slab.

#### **III. TIGHT-BINDING MODEL**

The band structure obtained from first-principles calculations give little room to explore different scenarios, e.g., band alignment. For that purpose, we construct a representative tight-binding (TB) model to carry out calculations of general TI/FM interfaces [Fig.  $4(a)$ ]. The TI is described using a four-band low-energy effective Hamiltonian of  $Bi<sub>2</sub>Se<sub>3</sub>$  as

TABLE III. Four-band-model tight-binding parameters for  $Bi<sub>2</sub>Se<sub>3</sub>$ .

	$M_0$ (eV) $M_1$ (eV $\AA^2$ ) $M_2$ (eV $\AA^2$ ) $A_0$ (eV $\AA$ ) $B_0$ (eV $\AA$ )			
$-0.28$	6.86	44.5	3.33	2.26

derived in  $[36]$ . The basis consists of the  $p<sub>z</sub>$  states on Bi and Se with total moment  $J_z = \pm \frac{1}{2}$ , labeled  $|P1^+, \frac{1}{2}\rangle$ ,  $|P2^-, \frac{1}{2}\rangle$ ,  $|P1^+_-$ ,  $-\frac{1}{2}$ , and  $|P2^-_+$ ,  $-\frac{1}{2}$ . In this basis, the TI Hamiltonian is

$$
H_{\rm TI} = \sum_{n} [H_{n,n} C_n^+ C_n + (H_{n,n+1} C_n^+ C_{n+1} + \text{H.c.})], \quad (1)
$$

where *n* labels layers in the *z* direction and

$$
H_{n,n}(\mathbf{k}) = \left[ M_2 \left( k_x^2 + k_y^2 \right) + M_0 + \frac{M_1}{2a^2} \right] \Gamma_5 + A_0 \left( k_y \Gamma_1 - k_x \Gamma_2 \right),
$$
 (2)

$$
H_{n,n+1}(\mathbf{k}) = \left(-\frac{M_1}{4a^2}\Gamma_5 - \frac{B_0}{2a}i\Gamma_4\right).
$$
 (3)

Here  $\Gamma_{1,2,3} = \sigma_{1,2,3} \otimes \tau_1$  and  $\Gamma_{4,5} = I \otimes \tau_{2,3}$ , where  $\sigma_{1,2,3}$ and  $\tau_{1,2,3}$  are the Pauli matrices in spin and orbital space, respectively. The parameters  $M_{0,1,2}$ ,  $B_0$ , and  $A_0$  are taken from [\[37\]](#page-7-0) and listed in Table III. The lattice constant is assumed to be  $a = 3.5$  Å. For simplicity, we ignore the electron-hole asymmetry term in the Hamiltonian.

The ferromagnet is described by a single-orbital TB Hamiltonian on a cubic lattice  $H_{\text{FM}}^{\uparrow,\downarrow}(\mathbf{k}) = \varepsilon_0 \mp \Delta + 2t_0(\cos k_x a +$  $\cos k_y a + \cos k_z a$ , where  $\varepsilon_0$  is the onside energy,  $\Delta$  is the exchange splitting, and  $t_0$  is the hoping integral. The Green's function of TI interfaced with a ferromagnet is evaluated from the Dyson equation  $G_{\text{TI}} = G_{\text{TI}}^0 + G_{\text{TI}}^0 \Sigma G_{\text{TI}}$ , where  $G_{\text{TI}}^0$  is the Green's function of the stand-alone TI. The self-energy due to the coupling across the interface  $\Sigma = \tau^{\dagger} G_{\text{FM}}^0 \tau$  is determined by the surface Green's function of the ferromagnet  $G_{FM}^0$  and the interface coupling matrix  $\tau$  which is determined by the interface hopping parameter *t* [\[38\]](#page-7-0). The band structure is evaluated in terms of the Bloch spectral density  $n(E, \mathbf{k}) =$  $-\frac{1}{\pi}$ Im[Tr( $G_{\text{TI}}$ )] in the 2D Brillouin zone.

We note that using a two-band effective Hamiltonian for topologically protected states can only be used in a weak coupling regime  $(\xi = t/t_0 \ll 1)$ . In this case we obtain the well-known expression  $H_{\text{eff}} = H_0 + J_{\text{eff}} \sigma_z$ , with  $J_{\text{eff}} = \xi^2 \Delta$ (see Supplemental Material [\[36\]](#page-7-0)). This effective Hamiltonian has been widely used to describe TI/FM insulator interfaces [\[28\]](#page-7-0). In a more general case the four-band model needs to be used to properly describe TI properties.

Figure 4(b) shows the band structure of the stand-alone TI surface indicating that the linear dispersion of the surface state is well reproduced [\[37\]](#page-7-0). Then we calculate the band structure of the TI/FM interface as a function of the interface coupling strength  $(\xi)$ . We distinguish two cases by varying the on-site energy (the Fermi energy) of the FM: (i) FM bands lie above the bulk band gap of  $Bi<sub>2</sub>Se<sub>3</sub>$ , and (ii) FM bands lie within the band gap of  $Bi<sub>2</sub>Se<sub>3</sub>$ . In the first case, the ferromagnet represents a FM insulator. The corresponding TI/FM insulator spectral density is plotted in Fig.  $4(c)$ . It is seen that, in the weak coupling <span id="page-6-0"></span>region, a band gap opens in the surface states as expected from the two-band model [\[28\]](#page-7-0). The stronger coupling pushes the surface bands down in energy eventually causing the lower branch of the Dirac cone to merge with the valence band. In the second case, the ferromagnet represents a FM metal with its bands aligned with the surface state [Fig.  $4(d)$ ]. Even a small amount of hybridization smears the surface state and, for moderate to strong hybridization, the surface state is essentially absorbed in the metal states. These results corroborate the first-principles findings.

### **IV. CONCLUSIONS**

Overall, our results indicate that the helical surface state of the TI is not robust upon the perturbation introduced by a ferromagnetic metal interface. Our first-principles and model studies of the Bi<sub>2</sub>Se<sub>3</sub>/Ni(111) and Bi<sub>2</sub>Se<sub>3</sub>/Co(111) interfaces demonstrate that different work functions of the TI and the FM metals lead to a charge transfer across the interface which shifts the topological surface states down about 0.5 eV below the Fermi energy. The hybridization of these surface states with the metal states at the TI/FM metal interface smears out the topological surface states and destroys their helical spin structure (to larger extent in case of Ni as compared to Co). The band alignment of  $Bi<sub>2</sub>Se<sub>3</sub>$  and Ni (Co) places the Fermi energy far in the conduction band of the bulk  $Bi<sub>2</sub>Se<sub>3</sub>$ , where there are

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no Dirac states and where the hybridization between the TI and FM states aligns the electrons spin with the ferromagnets magnetization. Our results indicate that the physical picture characterizing the coupling between the TI and the FM metals and its effect on the topological surface states is more intricate than the common notion of a magnetic exchange field breaking the time reversal symmetry and opening the gap in the surface states. These considerations have to be taken into account when interpreting the experimental data and designing applications contingent on the helical spin structure of the TI surface states.

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