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The Effects of Belowground Resources on Aboveground Allometric Growth in Bornean Tree Species

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1. Introduction

In any forest, the allometry of tree growth, that is, relative changes in tree size and shape, is both a cause and a consequence of variation in resource availability. Trees with wide, spreading crowns simultaneously preempt light interception and shade out nearby competitors (Canham et al., 1994; Weiner, 1990). Adequate availability of soil resources enables allocation to rapid height growth, allowing faster-growing species to over-top their neighbors and grow into a better light environment (Coomes et al., 2009; King, 1981, 1990a; Kohyama, 1987; Tilman, 1988). Allometries can therefore be viewed as evolutionary outcomes reflecting dynamic strategies of competition for above- and belowground resources (Halle et al., 1978; Horn, 1971), as well as plastic responses to a spatially and temporally variable environment (Clark, 2010; Dietze et al., 2008).

Variation in allometric growth can promote coexistence among species and, consequently, can be viewed as maintaining diversity in plant communities (Grubb, 1977; Kohyama...
et al., 1999). Along resource gradients in forests, tree species are observed to have different growth strategies (e.g., Kobe, 1999), in part because adaptations that promote survival in resource-poor environments may reduce competitive ability when resources are more abundant, and, conversely, because of the survival-costs of fast growth (Chapin et al., 1993; Grime, 1979; Rose et al., 2009). Therefore, competitive growth strategies, which allow trees to rapidly overtop and shadeout their neighbors, may be selected for in environments that are relatively less limited in resources, whereas conservative strategies that sacrifice rapid growth maybe favored in more resource-limited environments (Chapin et al., 1993; Grime, 1979; Rose et al., 2009). Tradeoffs in demographic rates among tree species provide evidence for these proposed strategies, since tree species aggregating where resources are abundant experience heightened growth, but lower survival rates, relative to trees that cluster where light (Kobe et al., 1995; Poorter and Arets, 2003) and soil resources (Russo et al., 2008) are scarce. Thus, as adaptations for resource acquisition, tree allometries can be viewed as influencing species distributions along resource gradients (Givnish, 1995; Kobe, 1999). One explanation for such patterns is that species’ distributions along gradients defined by soil resources (e.g., mineral nutrients and water) is that as belowground resources become relatively more available, aboveground competition for light intensifies (resource competition theory; Newman, 1973; Tilman, 1988). Under this hypothesis, tree species characteristic of soils with greater resource supply rates should have a more competitive strategy of faster aboveground growth rates, as compared with species characteristic of soils with reduced resource supply rates (Newman, 1973; Tilman, 1988). Although it is well-known that tree species found primarily on soils with greater resource availability have faster diameter growth rates than those on resource-poor sites (e.g., Russo et al., 2005), competition for light is better defined in terms of growth in tree height and crown area (King, 1990b). Yet, how growth in these aboveground dimensions varies with belowground resource availability is less well known, particularly in tropical forests, even though the allometric adaptations linked with growth strategies in high versus low light environments are well documented (e.g., King, 1994; Kohyama, 1987, 1991; Poorter et al., 2003). Forestry models to quantify site index in temperate forests indicate that dominant canopy trees are generally taller at a given age on more resource-rich sites, although habitat factors contributing to forest productivity are not always clearly identifiable (e.g., Broadfoot, 1969; Carmean, 1979; Monsurud, 1984; Weiskittel et al., 2007). However, height-age relationships are difficult to determine in a seasonal tropical forests (Vanclay, 1992), and site indices typically exclude subcanopy species, which constitute a substantial proportion of the diversity of tropical forests (Ashton and Hall, 1992).

Here we examine soil-related patterns of variation in allometric growth in subcanopy tropical tree species and consider how these patterns reflect hypothesized differences in competitive strategies of tree species along resource gradients. We used empirically parameterized models of height and crown area growth to compare tree species’ competitive strategies along an edaphic gradient in a Bornean rainforest. Height and crown allometries and mean wood density were quantified in six subcanopy tree species from the mixed-dipterocarp tropical rain forest of Lambir Hills National Park (hereafter, Lambir) in Malaysian Borneo. There is strong floristic contrast along the edaphic gradient at Lambir because most tree species are found on only one or two soil habitats (Figure SMI, Davies et al., 2005). Here, we focus on the two extremes of this gradient: the resource-rich soil class, consisting of the two moist, relatively nutrient-rich soils types, clay and fine loam (with sampling preference for clay), which were contrasted with the better-drained, nutrient-poor sandy loam (Baillie et al., 2006). Additionally, consistent with resource competition theory, light availability varies inversely to soil resources, with the forest understory on sandy loam receiving on average 20% more total mean daily photosynthetic photon flux density than on the clay (Russo et al., 2010; S.E. Russo, unpub. data), suggesting that the intensity of competition for light is greater on clay than on sandy loam. We therefore expected trees’ allometric growth strategies to differ between these soil habitats due to variation in above- and belowground resources.

Our study species represent two genera contrasting in shade tolerance: Macaranga (Euphorbiaceae), a light-demanding genus, and Knema (Myristicaceae), a shade-tolerant genus. From each genus, we selected one clay and one sandy loam specialist species, forming a phylogenetically-controlled interspecific contrast of allometries to test whether tree species of divergent soil specialization also had divergent allometric growth strategies. We also evaluated whether any soil-related differences that we found were consistent across shade-tolerance groupings, since light-demanding species are generally more responsive to environmental variability (Bazzaz, 1979), and soil nutrients are often more limiting to their growth, compared to late successional, shade-tolerant species (Newman, 1973; Coomes and Grubb, 1998). Interspecific variation in allometry results from both adaptive variation and plastic responses to the environment. Therefore, we sampled one generalist species from each genus on both soil habitats to assess population-level variation in allometric growth. We predicted that tree allometry would vary with soil resources in accordance with resource competition theory (Newman, 1973; Tilman, 1988). Tree species specializing on the moister, more fertile clay-fine loam soil at Lambir were expected to have faster rates of height and crown area growth, compared to specialists of the drier, less fertile sandy loam. In other words, clay specialists should be taller and have more spreading crowns at a given age because their growth strategy is for light-preemption. They should also have shallower crowns to avoid self-shading within the crown (Horn, 1971). We further expected clay specialists to have reduced height safety factors (i.e. to be taller at a given diameter; sensu Niklas, 1992) and to exhibit wider crowns at a given size because where competition for light is greatest, structural stability should be relatively less important than height growth and crown expansion. We predicted that populations of generalist species growing on each soil type would exhibit similar patterns of soil-related variation in allometric growth strategies as soil specialists.

2. Materials and methods

2.1. Study site and species

Data were collected from the lowland, mixed-dipterocarp forest of Lambir Hills National Park in Sarawak, Malaysia (4°11’N, 114°01’E). Lambir receives ca. 3,000 mm of rainfall each year with > 100 mm of precipitation each month (Watson, 1985). The 52-ha forest dynamics plot at Lambir, established in 1991, is situated in the most diverse forest known in the Old World tropics (Ashton and Hall, 1992; Lee et al., 2002). Using standard methods (Condit, 1998a,b), all woody stems in the plot ≥ 1 cm in diameter at breast height (DBH, 1.3 m) are tagged, mapped, identified to species, and measured for DBH with re-censuses every five years. The gradient of soils at Lambir ranges from relatively nutrient-poor, well-drained, and humus-rich, sandstone-based coarse loams to relatively more fertile, moist, and humus-poor, shale-derived clay soils (Baillie et al., 2006; Lee et al., 2002). From this gradient, Davies et al. (2005) defined four soil types listed in order of increasing fertility: sandy loam, loam, fine loam, and clay. On the Lambir plot, each 20 m × 20 m subplot was categorized into one of the four soil types based on total C, N, and Pand ex-
changeable K, Ca, Mg and elevation at a 20 m × 20 m scale (Davies et al., 2005). Mineral nutrient concentrations and properties of each soil type are reported in Baillie et al. (2006) and Tan et al. (2009), and soil volumetric water contents for sandy loam and clay soils are reported in Russo et al. (2010).

Davies et al. (2005) identified tree species at Lambir showing spatial distribution patterns biased with respect to these four soil types using a stochastic point-process model that replicates small-scale (e.g. dispersal-driven) spatial aggregation while reducing large-scale (e.g. habitat-driven) aggregation, thereby taking into account spatial autocorrelation (Plotkin et al., 2000). These analyses indicated that the majority of species at Lambir display statistically significant associations with one or two soil types (soil specialists), and fewer species occur with similar abundances on all soil types (generalists). Soil specialization categories defined by Davies et al. (2005) within the Lambir plot are largely consistent with analyses of floristic differences among soil habitats at larger spatial scales within the region (Potts et al., 2002). Our six study species (Table 1) represent four soil specialists and two generalists, as categorized by analyses in Davies et al. (2005), from two genera differing in light-defined regeneration niche: *Macaranga* (Euphorbiaceae), a genus of faster-growing and light-demanding trees (Davies et al., 1998), and *Knema* (Myristicaceae), a genus of slower-growing, shade-tolerant trees (deWilde, 2000). These genera were selected to evaluate whether soil-related differences in aboveground growth are consistent across regeneration niches. From each genus, we chose one clay specialist and one sandy loam because, to the extent that these genera are reciprocally monophyletic, paired congener species phylogenetically-controlled interspecific comparison of allometric growth among soil types. For generalists, we sampled individuals on both sandy loam and clay-fine loam to quantify population-level variation in allometric growth among soil habitats. All study species are monopodial, subcanopy trees at maturity.

### 2.2. Tree allometry sampling and measurements

Trees sampled for allometry spanned the range of diameters for the study species in the Lambir plot and nearby forest (1.0–24.6 cm, Table 1). All individuals sampled from sandy loam, the most abundant soil habitat at Lambir, were selected randomly from the plot with the exception of the five largest trees from each species, which were systematically included to ensure sampling of the full range of diameters. However, since clay soil is less prevalent at Lambir, there are fewer individuals to sample within the plot. Therefore, clay specialists, *M. lamellata* and *K. elmeri*, and individuals from generalist *M. beccariana* growing on clay were exhaustively sampled from the plot, and we supplemented the sample size for these species from (1) trees located within the plot adjacent to clay on soil classified as fine loam, the soil type most similar to clay in soil texture, and we supplemented the sample size for these species from (1) trees located within the plot adjacent to clay on soil classified as fine loam, the soil type most similar to clay in soil texture, waterholding capacity, and fertility (Baillie et al., 2006) and (2) with trees on nearby clay soil located off the plot. Of trees randomly selected from the plot, ca. 3% were excluded from our study because they had either severely bent stems or crowns too difficult to distinguish from the surrounding foliage.

For each tree, we measured DBH, vertical stem height, height to the lowest leaf, and eight crown radii. Height was measured with measuring tape for trees ≤ 2 m tall. For taller trees leaning < 5° from vertical, stem height was estimated using trigonometry from the perpendicular distance from the observer’s eye to the stem (measured using a laser range finder or measuring tape) and the tangents of the angles to the top leaf and base of the tree (measured using a clinometer). For trees leaning > 5° from vertical (~8% of our sample), the distances and the sines of the angles from the observer to the top leaf and tree base were used to calculate height. Height to the lowest leaf was estimated the same way and used to calculate crown depth (stem height-height to lowest leaf). Crown radii were measured in eight directions (N, NE, E, SE, S, SW, W, and NW) as the distance from the stem to the outermost leaf. Crown area (CA) was then calculated as the summed area of eight triangles (CA = ∑(radius)² tan(22.5°)).

### 2.3. Wood properties

Wood density (ρ) for each species was quantified from trees (> 3 cm in DBH) sampled off-plot. For trees > 6 cm in DBH, trees were cored at breast height with an increment borer (5-mm in diameter) to a depth equal to one half of the DBH. Wood samples from trees < 6 cm in DBH were taken from branch seg-

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**Table 1.** Study species, including soil specialization, regeneration niche, and number of individuals sampled for height and crown allometries (N) and wood density (W), and abundance on the Lambir plot. Modulus of elasticity was approximated as a function of wood density (see methods). For generalists, demographic information is listed for each species overall and for individuals on sandy loam and clay. For each species, the individual with the largest DBH recorded in the 2003 Lambir census was included in our sample.

<table>
<thead>
<tr>
<th>Scientific name</th>
<th>Family</th>
<th>Soil specialization</th>
<th>Regeneration niche</th>
<th>DBH range (cm)</th>
<th>Height range (m)</th>
<th>N(W)</th>
<th>Abundance</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Knema galeata</em></td>
<td>Myristicaceae</td>
<td>Sandy loam</td>
<td>ST</td>
<td>1.0-20.6</td>
<td>2.2-28.8</td>
<td>31 (5)</td>
<td>709</td>
</tr>
<tr>
<td><em>Knema elmeri</em></td>
<td>Myristicaceae</td>
<td>Clay</td>
<td>ST</td>
<td>1.0-24.6</td>
<td>1.6-24.9</td>
<td>29 (8)</td>
<td>31</td>
</tr>
<tr>
<td><em>Macaranga lanellata</em></td>
<td>Euphorbiaceae</td>
<td>Sandy loam</td>
<td>LD</td>
<td>0.9-11.0</td>
<td>1.9-23.5</td>
<td>37(11)</td>
<td>344</td>
</tr>
<tr>
<td><em>Macaranga lanellata</em></td>
<td>Euphorbiaceae</td>
<td>Clay</td>
<td>LD</td>
<td>1.1-13.9</td>
<td>2.4-18.5</td>
<td>44(4)</td>
<td>68</td>
</tr>
<tr>
<td><em>Knema latericia</em></td>
<td>Myristicaceae</td>
<td>Generalist</td>
<td>ST</td>
<td>1.3-17.1</td>
<td>1.8-24.4</td>
<td>71 (5)</td>
<td>1078</td>
</tr>
<tr>
<td>Sandy loam</td>
<td></td>
<td>Clay-fine loam</td>
<td></td>
<td>1.3-17.1</td>
<td>1.8-24.4</td>
<td>36 (1)</td>
<td>1007</td>
</tr>
<tr>
<td>Clay-fine loam</td>
<td></td>
<td>Macaranga beccariana</td>
<td>Euphorbiaceae</td>
<td>1.9-16.4</td>
<td>4.0-25.9</td>
<td>79 (18)</td>
<td>656</td>
</tr>
<tr>
<td>Sandy loam</td>
<td></td>
<td>Euphorbiaceae</td>
<td>Generalist</td>
<td>2.4-16.0</td>
<td>5.6-21.7</td>
<td>38 (11)</td>
<td>553</td>
</tr>
<tr>
<td>Clay-fine loam</td>
<td></td>
<td>Macaranga beccariana</td>
<td>0.318 -1755</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Scientific name</th>
<th>Wood density (kg/m³)</th>
<th>Modulus of elasticity (N/m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Knema galeata</em></td>
<td>0.655</td>
<td>-1744</td>
</tr>
<tr>
<td><em>Knema elmeri</em></td>
<td>0.549</td>
<td>-1748</td>
</tr>
<tr>
<td><em>Macaranga lanellata</em></td>
<td>0.628</td>
<td>-1745</td>
</tr>
<tr>
<td><em>Macaranga umbrosa</em></td>
<td>0.507</td>
<td>-1749</td>
</tr>
<tr>
<td><em>Knema latericia</em></td>
<td>0.596</td>
<td>-1746</td>
</tr>
<tr>
<td>Sandy loam</td>
<td>Clay-fine loam</td>
<td>Macaranga beccariana 0.318 -1755</td>
</tr>
<tr>
<td>Sandy loam</td>
<td>Clay-fine loam</td>
<td>Macaranga beccariana 0.318 -1755</td>
</tr>
</tbody>
</table>

Abbreviations: ST = shade-tolerant, LD = light-demanding.
ments 10 cm in length and > 1 cm in diameter. After extraction, cores and branch segments were placed in drinking straws and resealable bags, respectively, and stored cold until they were processed (within 48 h of collection). Bark was removed from all core and branch samples, and cores were cut into segments ≤ 5 cm in length to allow weighting of specific gravity estimates to account for differences in density between older and younger wood. Each segment was submerged in water in a pre-tared graduated cylinder, and fresh volume was determined from the mass of water displaced. Each segment was dried to constant mass at 60°C. Wood density (p) in kg/m³ was calculated for each tree as: \( p = \frac{\sum_i (M_i/V_i)(L_i^2 - L_i^2)}{\sum_i L_i} \) for n segments, where \( L_i \) is the length, \( M_i \) is the mass, and \( V_i \) is the volume of segment \( i \), and \( L_{\text{seg}} \) is the length of the entire wood sample.

We predicted Young’s modulus of elasticity (E) and green wood density (S) for each species based on our estimates of specific gravity. To predict E from p, we fit the relationship between species average E and p values reported in the literature for 30 tropical tree species (van Gelder et al., 2006) and 127 commercially important timber species (United States Department of Agriculture, 1999) using ordinary least squares regression. Of the models tested, the following third-order polynomial explained the greatest proportion of variation in \( E \) due to \( p \) (\( R^2 = 0.76 \)):

\[ E(p) = -1767 + 4.01 \times 10^{-5} \times p - 34.63 \times p \]

where \( E \) is in units of \( \text{kg/m}^2 \) and \( p \) is in units of \( \text{Nm}^2 \). We used predicted wood density \( S \) in kg/m³ as:

\[ S = \pi \times p(1 + c/100) \]

where \( S \) is the density of water (1,000 kg/m³) and \( c \) is percent wood moisture content (Simpson, 1993). We used species-specific values of \( c \) reported in Suzuki (1999).

Critical height (H\(_c\)), the theoretical height at which a tree of a given DBH would buckle under its own weight, was calculated as:

\[ H_c = \frac{0.792E/(\rho g)^{1/3}}{\text{DBH}^{5/3}} \]

(Greenhill, 1881), where \( g \) is the gravitational force per unit mass on Earth (9.8 N/kg). A height safety factor, defined as the ratio of \( H_c \) to realized height \( H \) (sensu Niklas, 1992), was used as a metric of tree mechanical stability.

2.4. Allometric models and analysis

We used these data to (1) quantify parameters for height-DBH, crown area-DBH, and crown depth-height allometry for our six study species, (2) to test the interspecific and intraspecific effects of soil resource variation and regeneration niche on allometry and height safety factors, and (3) to predict height and crown growth over time using allometric parameters and diameter growth rates. All mathematical modeling and statistical analysis was performed in the statistical software package, R (The R Core Development Team, 2009).

2.4.1. Allometric scaling relationships

Allometric scaling relationships were modeled as power functions of the form \( Y = aX^b \), where \( X \) is the independent variable, \( Y \) is the response variable, and \( a \) and \( b \) are fitted parameters. Stem height (H) and crown area (CA) were modeled as functions of DBH, and crown depth (CD) was modeled as a function of H since this trait most closely correlates with the crown’s position in the vertical light gradient.

Since trees often reach an asymptotic height (\( H_{\text{max}} \)), we also tested the fit of the H-DBH allometry using the function: \( H = H_{\text{max}}[1-\exp(-aDBH)] \) (Thomas, 1996). This model failed to converge for all but one species, K. elmeri, as no other species reached an asymptotic height, and so power functions were used.

Allometric power functions can be linearized by taking the log of both sides: \( \ln(Y) = b \times \ln(X) + \ln(a) \). Allometric parameters could be fit either to linearized models using ordinary least squares (OLS) regression or to unlogged power functions using nonlinear least squares (NLS) regression, both assuming a normal error distribution. We tested which of these modeling approaches provided a better fit to our allometric data using Akaïke’s Information Criterion (AIC) (Table SM2). The AICs of the log-log linear regression models (hereafter, linear models) were compared to those from the NLS models by adding two times the sum of the logged response variables to the linear model AIC value. The AICs for the linearized models were lower than for nonlinear models in at least five of the six study species for each allometric relationship, and so the linearized models were used in all cases. The residuals of these models met the assumption of normality.

Although major axis (MA) regression is recommended for fitting allometric relationships (Warton et al., 2006), we fit linearized models using OLS regression because we were interested in estimating the main and interactive effects of soil type and regeneration niche on allometric relationships, which is more readily accomplished using OLS methods. We report in Table SM3 the slope and elevation parameters with 95% confidence intervals fit in MA regression using the smatr package (Warton and Ormerod, 2007) in R statistical programming software. Type II tests of fixed effects (Fox, 2008) were performed with the car package (Fox et al., 2009) in R. Each allometric model included the three-way interaction between a covariate (DBH or height) and two factors, soil (clay/silt loam or sandy loam) and regeneration niche (shade-tolerant, K. elmeri, or light-demanding, Macaranga). A type II test of effects is appropriate in this situation because the result of the test is invariant to the order that the effects are entered into the model (Fox, 2008). Models analyzing interspecific variation in allometry included the four specialist species, and the factor “soil” contrasted congeners of differing soil specialization. Models testing intraspecific variation included both generalist species, and the factor “soil” instead contrasted populations of conspecifics growing distinct soil habitats. Similar models were used to evaluate height safety factor, however, safety factor and its covariable DBH were not logged since this trait is not typically modeled as a power function.

2.4.2. Allometric growth models

We developed species-specific models of height and crown growth rates using diameter growth rate models, parameterized using censuses in 1992, 1997, and 2003 from the Lambir plot, which were then scaled using the fitted parameters for height and crown allometries. Specifically, instantaneous diameter growth rate (G) of a tree was modeled as a power function of diameter (Enquist et al., 1999; Muller-Landau et al., 2006):

\[ G(D) = dD/dt = aD^b \]

(1)

To find \( D \) at given time (\( D_t \)), we used the approach in Muller-Landau et al. (2006) and integrated Equation (1), yielding

\[ D_t = (D_0^{1-b} + a(1 - b))^{-1/b} + \varepsilon_i \]

(2)

for tree i where \( D_0 \) is the initial diameter of the tree, \( t \) is intercensus period in years, and \( \varepsilon_i \) is the deviation of \( D_t \) from its predicted value. Since intercensus period varied between trees, we scaled errors with time as in Russo et al. (2007). To obtain an expression predicting tree height (\( H_t \)) given an initial diameter (\( D_0 \)), we used an approach similar to Coomes et al. (2009) and substituted the expression for \( D_t \) (Equation (2)) for \( D \) in the H-D allometric power function (\( H = aD^b \)). Because our goal was prediction, the allometric parameters \( a \) and \( b \) used in this model were fit using NLS regression, rather than OLS regression, to avoid the error in back-transformation of parameters.

\[ H_t = a(D_0^{1-b} + a(1 - b))^{-1/(1-b)} \]

(3)

Instantaneous height growth rate (\( dh/dt \)) was expressed as a function of diameter by using the chain rule to multiply the derivative of the H-D power function (\( dh/dD \)) by diameter growth rate (Equation (1)) to give

\[ \frac{dh}{dt} = \frac{dH}{dD} \frac{dD}{dt} = (abD^{b-1})aD^b \]

(4)
The methods used to derive Equations (3) and (4) were similarly applied to crown area-diameter allometry to yield CA, and dCA/dt.

The growth-diameter scaling relationship (Equation (2)) for each specialist species and individuals of generalist species on the same soil type were fit using the Neider-Mead simplex search algorithm (Neider and Mead, 1965) as implemented in the function optim in R. We varied initial parameter values to reduce the risk of finding a local maximum.

The longevity of each species was estimated to provide time axes for Ht and CA, projections. Longevity was estimated for each species as in Laurance et al. (2004) by dividing the maximum DBH by the median, upper quartile and upper decile of species diameter growth rates and averaging these values. Longevity estimates and parameters used for projection of height and crown area growth are reported in Table SM4.

Our models project growth for trees that maintain average growth rates and allometries throughout life. They thus do not account for variation in growth rates or allometries among individuals (Clark, 2010) and over a tree’s life-span, due to, for example, variation in the relationship between height and diameter growth rates between dominant and suppressed trees (Sumida et al., 1997) or temporal autocorrelation of growth rates (Kohyama et al., 2005). Nevertheless, as a tool used to examine mean differences in tree growth and form between soil habitats, our models provide insight into the competitive strategies that tree species exhibit along resource gradients.

3. Results

3.1. Allometric relationships

The influence of soil type and regeneration niche varied in strength among allometric relationships and between interspecific and intraspecific comparisons. Parameters of the allometric models for each species are presented in Table SM5.

3.1.1. Height

Stem DBH, soil specialization, and regeneration niche together explained a large proportion of the variation among soil specialists in stem height (R² = 0.88; Figure 1a and b), accounting for 5% more variance than was explained by DBH alone (R² = 0.83). The sandy loam specialists, M. galeata and M. lamellata, were each significantly taller at the smallest diameters than the congeneric clay specialists, K. elmeri and M. lamellata (F₁,₅₆ = 55.49, P < 0.001 and F₁,₇₇ = 4.92, P < 0.029, respectively, Table SM5). The magnitude of this difference was significantly greater for shade-tolerant species than light-demanding species (significant soil by regeneration niche interaction, Table 2). The biological significance of this interaction is evidenced by comparing the predicted stem height of each species at 10 cm DBH: the shade-tolerant sandy loam specialist, K. galeata, is predicted to be 3.3 m taller than the clay specialist, K. elmeri (9.6 m vs. 6.3 m), while light-demanding sandy loam specialist M. lamellata is predicted to be only 1.2 m taller than clay specialist M. lamellata (9.8 m vs. 8.6 m). For the comparison of regeneration niche between clay specialists, the light-demanding species was taller at a given diameter than the shade-tolerant species (M. lamellata vs. K. elmeri, F₁,₅₆ = 19.45, P < 0.001); however, there was no significant difference in the intercepts of the sandy loam specialists M. lamellata and K. galeata (F₁,₆₄ = 0.5485, P = 0.462; Table SM5). Neither of the two-way interaction of DBH with either soil specialization or regeneration niche, nor the three-way interaction between DBH, soil specialization, and regeneration niche was statistically significant (Table 2), indicating that these four species shared a common trajectory of change in height with DBH.

For generalists, stem DBH, regeneration strategy, and soil type together explained a large proportion of the variation in stem height (R² = 0.87; Figure 2a and b), accounting for 14% more variation than was explained by DBH alone (R² = 0.73). Soil type had a significant effect on stem height (significant main effect of soil, Table 2), indicating that generalists displayed some intraspecific variation in height allometry in response to variation in belowground resources. In parallel to soil specialists, individuals of K. latericia growing on sandy loam were significantly taller at a given diameter than those on clay-fine loam (F₁,₆₀ = 6.118, P = 0.016, Table SM5). The same trend emerged between M. beccariana populations, although the difference was not statistically significant (F₁,₅₇ = 2.786, P = 0.099, Table SM5). The predicted height at 10 cm DBH for individuals of K. latericia on sandy loam was 14.0 m versus 12.4 m on clay-fine loam, and for M. beccariana, the predicted height of individuals on sandy loam was 14.8 m versus 14.3 m on clay-fine loam. The significant interaction between regeneration niche and DBH (Table 2), indicated that these two species have different trajectories of change in height with DBH: M. beccariana was taller than K. latericia at small diameters, however, K. latericia approached the height of M. beccariana growing on larger diameters (Table SM5). The amount of within species variation in height allometry due to soil resources did not differ between generalists: neither the two-way interaction involving soil, nor the three-way interaction was significant (Table 2).

3.1.2. Crown area

Among soil specialists, DBH, soil specialization, and regeneration niche explained a substantial proportion of variation in crown area (R² = 0.74; Figure 1c and d) and accounted for 7% more variance than was explained by DBH alone (R² = 0.67). Soil specialization had a significant effect on crown area, but there was a significant interaction between soil specialization and regeneration niche (Table 2) indicating that the soil-related difference in initial crown area was greater between light-demanding than shade-tolerant specialists (P = 0.002, Table SM5). Among shade-tolerant species, the sandy loam specialist, K. galeata, had a significantly greater intercept than the clay specialist, K. elmeri (F₁,₅₆ = 11.75, P = 0.001), and among light-demanding species, sandy loam specialist M. lamellata had a significantly greater intercept than clay specialist, M. lamellata (F₁,₇₉ = 8.147, P = 0.006; Table SM5). The significant soil by DBH interaction indicated that the trajectory of change in crown area with DBH varied significantly due to soil specialization (Table 2): clay specialist K. elmeri had a significantly larger slope than K. galeata (F₁,₅₆ = 6.620, P = 0.013), but the slopes did not differ significantly between light-demanding specialists M. lamellata and M. latericia (F₁,₇₇ = 0.6675, P = 0.416). Consequently, crown area was significantly greater on clay-fine loam than sandy loam over most of the observed diameters among K. latericia specialists, whereas the opposite was true of Macaranga specialists. In addition to variation due to soil specialization, the crown area-DBH allometry also differed due to regeneration niche (significant regeneration niche-DBH interaction, Table 2). For sandy loam specialists, M. lamellata had a significantly greater slope than K. galeata (F₁,₆₀ = 5.570, P = 0.021), but the clay specialists K. elmeri and M. lamellata did not differ in slope (F₁,₆₀ = 1.474, P = 0.229; Table SM5). The three-way interaction between DBH, soil specialization, and regeneration niche was not significant (Table 2). For generalists, DBH, soil type, and regeneration niche together explained a large proportion of variation in crown area allometry (R² = 0.80; Figure 2c and d), accounting for 4% more variance than was explained by DBH alone (R² = 0.76); however, there were no significant effects involving soil type or regeneration niche (Table 2). Thus, little within species variation in crown area allometry was explained by soil type or regeneration niche.
Figure 1. Height-diameter (DBH) and crown area-DBH allometric relationships for four Bornean tree species, including two pairs of congeneric tree species contrasting in soil habitat specialization representing shade-tolerant (*Knema*) and light-demanding (*Macaranga*) regeneration niches. Lines were fit using ordinary least squares regression.

Table 2. Type II tests of effects for linearized power function models of height, crown area, and crown depth allometry. Each model included a covariate of size (DBH or height) and two factors, soil (sandy loam or clay) and regeneration niche (regen; light-demanding or shade-tolerant), with all interactions. In “Specialist” models, the factor “soil” contrasts related species of differing soil specializations; in “Generalist” models, “soil” contrasts individuals of the same species on different soil types. Bold typeface highlights statistically significant factors.

<table>
<thead>
<tr>
<th>Trait</th>
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<th>Generalists</th>
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3.1.3. Crown depth

Among soil specialist species, height, soil specialization, and regeneration niche accounted for approximately half of the observed variation in crown depth ($R^2 = 0.49$; Figure 3a and b), accounting for 13% more variance than was explained by height alone ($R^2 = 0.36$). The interaction between soil specialization and regeneration niche was significant (Table 2): in the shade-tolerant genus, clay specialist *K. elmeri* had significantly deeper crowns at small heights than sandy loam specialist, *K. galeata* ($F_{1,56} = 20.04, P < 0.001$), but initial crown depth did not differ between light-demanding specialists ($F_{1,77} = 0.0445, P = 0.833$, Table SM5). Neither of the two-way interactions of height with soil specialization or regeneration niche, nor the three-way interaction, was statistically significant (Table 2), indicating a shared trajectory of change in crown depth with height.

Height, soil, and regeneration niche explained a similar proportion of variation in crown depth among generalists as they did among soil specialists ($R^2 = 0.49$; Figure 3c and d), accounting for 15% more variation than was explained by height alone ($R^2 = 0.44$). Significant intraspecific variation in crown depth due to soil resources was not observed in either generalist, as neither the main effect of soil type nor its interactions with height or regeneration niche was significant (Table 2). The significant interaction between height and regeneration niche (Table 2) arose because crown depth increased more rapidly with height in *M. beccariana* than *K. latericia* ($P < 0.001$, Table SM5).

3.1.4. Height safety factor

For soil specialists, DBH, soil, and regeneration niche explained a small proportion of the variation in height safety factor ($R^2 = 0.24$; Figure 4). The height safety factor declined significantly with DBH among soil specialists (Table 2, SM5). In addition, soil specialization had a significant effect on mechanical stability: the sandy loam specialists, *K. galeata* and *M. lamellata*, both grew closer to their critical heights than did the clay specialist congeners, *K. elmeri* and *M. lamellata* (Figure 4). A significant interaction between soil and regeneration niche (Table 2) arose because this difference was significant between *Knema* specialists ($F_{1,56} = 43.71, P < 0.001$) but not *Macaranga* specialists ($F_{1,77} = 2.710, P = 0.104$). No interaction with DBH was significant; thus, all four species showed parallel changes in height safety factor with increasing diameter.

For generalists, a slightly larger fraction of variation in safety factor was explained by DBH, soil, and regeneration niche ($R^2 = 0.29$; Figure 4). For generalists, soil resources had a significant effect on the height safety factor (Table 2): individuals on sandy loam grew closer to their buckling height on average than conspecifics on clay-fine loam (Table SM5), but this difference was not statistically significant within either the shade-tolerant generalist, *K. latericia* ($F_{1,67} = 3.111, P = 0.026$) or light-demanding generalist, *M. beccariana* ($F_{1,75} = 3.295, P = 0.0735$). A significant interaction between DBH and regeneration niche (Table 2) arose because height safety factor decreased significantly with size in *M. beccariana* ($F_{1,75} = 5.865, P = 0.018$) and *K. latericia* ($F_{1,67} = 7.256, P = 0.009$, Table SM5). Neither the two-way interaction between regeneration niche and soil nor the three-way interaction was significant, indicating that the amount of within species variation in height safety factor due to soil resources did not vary between genera.

Figure 2. Height-diameter (DBH) and crown area-DBH allometric relationships for Bornean tree species, including two generalist tree species that were sampled on both sandy loam and clay-fine loam habitats and represented shade-tolerant (*K. latericia*) and light-demanding (*M. beccariana*) regeneration niches. Lines were fit using ordinary least squares regression.
3.2. Dynamic allometric models

We projected stem height and crown area growth over time periods corresponding to an estimate of the lifespan of each tree species (specialists) and populations on each soil type (generalists) to predict the effect of soil resources on allometric growth rates (Table SM5, Figure 5).

Overall, models of allometric height growth for specialists and generalists (Figure 5a-d) supported our prediction that trees on the more fertile, moister clay-fine loam soil would have faster height growth rates than trees of the same age on sandy loam. Although sandy loam specialists were taller at younger ages, they were eventually surpassed in height by clay specialists (Figure 5a and b). In both pairs of specialists, our models showed that clay specialists would overtake sandy loam specialists in height after about fifty years. Among *Knema* specialists, both species grew to approximately the same maximum height, but the shorter-lived, clay specialist, *K. elmeri*, reached this height more quickly than did the longer-lived, sandy loam specialist, *K. galeata*. *Macaranga* specialists were similar in height over the lifespan of the sandy loam specialist *M. lamellata*, but with a longer lifespan, the clay specialist *M. lamellata* reached a larger maximum height. A similar pattern held for generalists: individuals on clay-fine loam were taller than those on sandy loam at all ages except for the earliest (Figure 5c and d). Our models of generalists showed that populations on clay-fine loam would overtake those on sandy loam within 25 years in *K. lateritia* and within 5 years in *M. beccariana*. The projected difference in height between conspecifics of the same age on contrasting soil types was greater.

Figure 3. Crown depth-height allometry allometric relationships for six Bornean tree species including (a and b) two pairs of congeneric tree species contrasting in soil habitat specialization (c and d) and two generalists sampled on both sandy loam and clay-fine loam habitats. Species represented shade-tolerant (*Knema*) and light-demanding (*Macaranga*) regeneration niches. Lines were fit using ordinary least squares regression.

Figure 4. Interspecific and intraspecific comparisons of tree height safety factor for six Bornean tree species, including two pairs of congeneric tree species contrasting in soil habitat specialization and two generalists sampled on both sandy loam and clay-fine loam habitats. Species represented shade-tolerant (*Knema*) and light-demanding (*Macaranga*) regeneration niches. The asterisk represents a significant difference in height safety factor between soil types $P < 0.05$. 
in *M. beccariana* than in *K. latericia*, supporting our prediction that light-demanding species would exhibit greater intra-specific variation in aboveground growth rate due to soil resources than shade-tolerant species.

Models of crown area growth (Figure 5e-h) predicted that trees growing on clay-fine loam soil generally would exhibit greater crown area at a given age than trees on sandy loam, consistent with our prediction. Models of specialists demonstrated that the crown of clay specialist *K. elmeri* was larger at 1 cm DBH, grew more rapidly over time, and reached a larger maximum area than sandy loam specialist, *K. galeata* (Figure 5e). In contrast, *Macaranga* specialists shared a similar crown growth trajectory for their first fifty years of growth, but clay specialist *M. lamellata* eventually surpassed sandy loam specialist *M. lamellata* and reached a larger maximum crown area (Figure 5f). Models for both generalists showed that conspecifics had approximately the same initial crown area regardless of soil type, but populations on clay-fine loam spread their crowns more quickly and attained a greater maximum crown area than those on sandy loam (Figure 5g and h). Models projected greater differences between sandy loam and clay-fine loam populations in crown area with age in the light-demanding generalist *M. beccariana* than in the shade-tolerant generalist *K. latericia*, implying greater within species variation in crown growth due to soil resources.

Models predicting the change in height and crown area growth rates with DBH varied in shape among species (Figure 6). For *Knema* specialists, both height and crown area growth rates were more similar at initial diameters but diverged slowly with increasing diameter, with *K. elmeri* increasing and *K. galeata* decreasing slightly in growth rate (Figure 6a and e). Between *Macaranga* specialists, *M. lamellata* had higher initial height and crown area growth rates, but was overtaken by *M. lamellata* in both by ca. 3 cm DBH (Figure 6b and f). Individuals of *K. latericia* on the two soil types differed only subtly in growth rates. In height growth rate (Figure 6c), individuals on clay-fine loam grew faster initially but were surpassed in growth rate by sandy loam individuals by 11 cm DBH. Crown area models demonstrated that individuals of *K. latericia* on both soil types also have similar growth rate across all diameters (Figure 6g). The height growth rate in *M. beccariana* decreased exponentially over a range of diameters (Figure 6d), whereas the crown area curve was an increasing function (Figure 6h). In both comparisons, the individuals on clay-fine loam grew faster than those on sandy loam.

### 4. Discussion

Tree stems and crowns play key roles in competitive interactions in forests since they display light-harvesting organs (leaves) and, in doing so, preempt light from smaller individuals (Weiner, 1990). Because trees should be under selection to maximize growth rate, given survival (Givnish, 1988), tree species may evolve different height- and crown-growth strategies in response to resource availability, and there is abundant evidence that a diversity of such strategies exists (e.g., Halle et al., 1978; Horn, 1971; Kohyama and Hotta, 1990; Poorter et al., 2006). Aboveground growth can, however, be limited by belowground resource availability (Bungard et al., 2002; Burslem et al., 1996; Grubb et al., 1996; Latham, 1992; Turner, 1991), but the nature of this limitation is still debated (Coomes and Grubb, 1998). Competition for light may become more intense with increases in belowground resources, favoring tree species with faster aboveground growth rates on soil types with greater, relative to lesser, resource supply rates (Tilman, 1988). Overall, our height and crown growth models were consistent with this mode of competition: in the six Bornean trees species examined, soil-related habitat variation influenced both the overall rates of growth in height and crown area and their rates of change with tree size. Species specializing on the moister, more fertile clay soil extended their stems and crowns more rapidly than species specializing on the well-drained, less fertile sandy loam soil. Our results are consistent with other observations (e.g., Coomes and Allen, 2007) that soil resources, in addition to light, can affect aboveground competition with neighboring trees. In addition, understory light availability is lower on the clay than sandy loam soil (Russo et al., 2010; S.E. Russo, unpub. data). This difference is likely a result of the greater leaf areas of canopy trees on clay (Ash-
4.1. Soil-related differences in height and crown allometries and growth

Our height growth models projected that clay specialists would be taller than sandy loam specialists at the same age for most of their lifespans. Sandy loam specialists were, however, found to be taller at the youngest ages, but would be surpassed in height by clay specialists after approximately fifty years of growth. This result is inconsistent with trenching experiments in tropical forests that resulted in increased aboveground growth in seedlings experiencing reduced belowground resources that are both a cause and a consequence of the structural and functional features of the forest.
though our study species exhibited consistent patterns of soil-related variation in height-diameter scaling, the overarching trend was contrary to competition-based predictions, since sandy loam specialists generally had higher allometric intercepts than did clay specialists. In reconciling the findings that model-based dynamic growth, but not static, allometries were consistent with our predictions, an important consideration is that trees at a given diameter are older on sandy loam than on clay-fine loam soil, due to the slower diameter growth and lower mortality rates there (Russo et al., 2005). Thus, while trees of sandy loam specialists and generalists were largely found to be taller and to have wider crowns at a given diameter, once time is accounted for, these differences in allometric scaling relationships are insufficient to outweigh the differences in diameter growth rate, causing clay specialists to be taller and have wider crowns than sandy loam competitors of the same age. Allometric scaling relationships are static measures of tree structure and do not fully represent a tree’s ability to compete for resources over its lifetime. Differences in competitive interactions cannot be inferred only from allometric scaling relationships because the allometries must be scaled for tree growth and stem geometric growth, rather than static allometric scaling relationships, provide a better metric for testing hypotheses about possible competitive outcomes.

There was little statistically significant soil-related intra-specific variation in the static height and crown allometries of either generalist. Nevertheless, at least some of the interspecific differences in allometric growth between soil specialists may be due to plastic responses or genotypic variation associated with the local environment, in addition to adaptive variation. Variation in growth rates between conspecifics does not necessarily translate to differences in population dynamics (Yamada et al., 2007). Nevertheless, whether a result of adaptive or plastic responses, our results suggest that trees growing on a common soil-defined habitat conform to similar competitive strategies.

Significant inter- and intraspecific differences in height allometry were restricted to allometric coefficients, or linear model intercepts, supporting prior observations that allometric exponents, or linear model slopes, are relatively consistent (King, 1990a; Kohyama, 1987; Kohyama and Suzuki, 1990), although this has not been observed among tree species in New Zealand (Russo et al., 2007). Thus, species differ in average height at a given diameter rather than in trajectory of height growth with diameter. Predicted differences in stem height between soil specialists at 10 cm DBH range from 1.2 m (Macaranga spp.) to 3.3 m (Kheua spp.), which is biologically important considering that light availability increases exponentially with elevation in the canopy (Yocla, 1974). Differences in allometry between soil habitats tended to be more pronounced in the shade-tolerant genus, which might be because Macaranga regenerates in brighter environments and canopy openings (Davies et al., 1998), and so may be less affected by the differences in understory light between the soil types under a closed canopy. Although we examined saplings and adult trees, our findings are consistent with previous studies in other Bornean mixed dipterocarp forests that have found significant soil-related inter-and intraspecific variation in the aboveground allometries of seedlings growing in heath versus peat swamp forest species in Borneo (Nishimura and Suzuki, 2001) and have observed stand-level variation in height-diameter allometries between lowland forests differing in soil mineral nutrient and water content (Ashton and Hall, 1992; Grubb, 1989). Although we found significant soil-related differences in crown allometry, predictions of crown architecture based on current light environment (i.e., Horn, 1971) were not realized. Others propose that crown architecture does not conform to geometry expected in its current light environment (Poorter et al., 2003), and suggest instead that differences in crown geometry reflect primarily the regeneration niche (Kohyama, 1987) or adult stature (Kohyama et al., 2003) of a species or the plasticity of crown growth in a heterogeneous light environment (Dietze et al., 2008).

4.2. Soil-related differences in height safety factor

Not only were trees taller at a given diameter on sandy loam, they also grew closer to their critical buckling height than did trees on clay-fine loam soil. Both sandy loam specialists had greater wood density than their clay soil congeners. Although increased wood density itself reduces tree mechanical stability by increasing the force of gravity acting on the stem column, the associated increase in Young’s modulus of elasticity counteracts the destabilizing effect of increased density and causes the critical buckling height of a tree to increase (Fournier et al., 2006; van Gelder et al., 2006). For this reason, trees with greater wood densities may grow taller at a given diameter without buckling under their own weight, relative to similarly proportioned trees with lower wood density. However, after accounting for the denser wood of sandy loam specialists, we found that trees at a given height had a lower theoretical buckling height than related clay specialists, sandy loam specialists still grew closer to their critical height. Although trees are known to compete for light by increasing their height-to-diameter ratio in response to lateral shading (Henry and Thomas, 2002), trees on the better-lit sandy loam may nevertheless grow closer to their buckling height than trees on clay-fine loam if they possess a superior belowground support system. Trees on well-drained soils have been found to extend their roots to greater depths than trees on poorly-drained soils, thereby reducing the risk of mechanical toppling (Fraser, 1962).

The more slender stem architecture exhibited by trees on sandy loam may also be related to their lower growth and mortality rates. In a study of the allometry of adult stature of Bornean trees, species with slower diameter growth rates had significantly thinner stems at a given height on average than fast-growing species (Sterck et al., 2001), which accords with our findings that specialists and populations of generalists on sandy loam grew closer to their critical height and were taller at a given diameter than the faster-growing trees on clay-fine loam. It has been hypothesized that slower-growing tree species having skinnier stems with denser wood reduce respiratory costs associated with surface area of the cambia, despite the fact that that thicker stems of equal strength can be constructed from softer wood for less total carbon (Anten and Schieving, 2010; Larjavaara and Muller-Landau, 2010). When we compared the metrics of trunk strength and construction costs used in Larjavaaraa and Muller-Landau (2010) between soil specialists, we found that, at the same height, sandy loam specialists had weaker, more cheaply made stems than clay specialists, despite their greater wood density (results not shown). Dense-wooded, but thin stems may therefore promote the survival of sandy loam specialists by minimizing carbon allocation to trunk construction and respiration, in addition to affording increased pathogen protection (e.g., Alverez-Clare and Kitajima, 2007).

Additionally, differences in stem construction between soil habitats have implications for the improved approximation of forest carbon stocks. With programs such as Reducing Emissions from Deforestation and Degradation (REDO) regarded as key to the mitigation of global climate change (UNFCCC, 2008), accurate estimation of carbon sequestration is an increasingly important aspect of forest management. In the six species examined here, soil habitat accounted for significant variation in two important components of forest biomass estimates: wood density, a known determinant of spatial biomass distributions (Baker et al., 2004), and allometric parameters, which contribute a large proportion of error to aboveground
biomass estimates (Chave et al., 2004). Therefore, analysis of an expanded suite of species is necessary to determine the scale and extent these patterns of soil-related patterns in tree architecture and, consequently, if soil type should be considered as a factor in models predicting forest biomass.

5. Conclusions

Characterizing the allometric growth strategies of trees along resource gradients as they compete for a better light environment provides insight into the mechanisms that cause species composition to vary among forest types. Our study is the first to examine variation in allometry and to model tree and crown growth strategies of adult-stature tropical trees with respect to belowground resources to test one possible mechanism by which soil-specific tree species distributions may arise. The competitive outcomes predicted by our models suggest that resource competition theory (Tilman, 1988) provides a viable mechanism that can at least partly explain how tree species characteristic of soils with low resource supply rates may be competitively excluded from more resource-rich sites (Ashton, 1992). Allometric scaling parameter growth models parameterized for more tree species and from other forests should be used to test the generality of our findings. Our results point to the importance of adaptive and plastic responses to both above and belowground resource availability in determining the allometric growth responses of trees and suggest that this diversity of responses has the potential to contribute to the coexistence of tree species by competition-based trade-off mechanisms (e.g., Hurtt: and Paglia, 1995; Paglia and Rees, 1998; Tilman, 1988) and by variation of allometric growth among individuals (Clark, 2010).

Acknowledgments — We are grateful to the Sarawak Forestry Corporation and Sarawak Forestry Department for permitting us to conduct research in Lambir Hills National Park. The 52-ha forest dynamics plot at Lambir is operated jointly by the Forest Department of Sarawak, Malaysia, Harvard University, USA (under NSF awards DB-9107247 and DEB-9629601 to P.S. Ashton), Osaka City University, Japan (under Monbusho grant 06041094 to T. Yamakura, 08NP0901 to S. Tamura and 09NP0901 to S. Sasaki). Funding was provided by the NSF-funded Research for Undergraduates in Theoretical Ecology (RUTE) program at the University of Nebraska-Lincoln, USA (DUE-0531920), a Sigma Xi Grant in Aid of Undergraduate Research, University of Nebraska-Lincoln School of Biological Sciences Undergraduate Special Funds, and the Functional Traits Project of the Center for Tropical Forest Science Arnold Arboretum Asia Program. We thank also David King and Chad Brassil for their constructive comments on previous versions of this manuscript and our field assistants Jugokukat and Lea Ali for their invaluable help and expertise.

Appendix A. Supplementary data is presented following the References.

References


Condit, R., 1998a. Tropical Forest Census Plots: Methods and Results from Barro Colorado Island, Panama and a Comparison with Other Plots. Springer, Berlin.


Greenhill, A.G., 1881. Determination of the greatest height consistent with stability that a vertical pole or mast can be made, and the greatest height to which a tree of given proportions can grow. Proceedings of the Cambridge Philosophical Society, volume 3, pp. 65-73.


The effect of belowground resources on light-affected allometry in six Bornean tree species: Supplementary materials.

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² Department of Mathematics, University of Nebraska-Lincoln, Nebraska, 68508, USA
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Fig SM1. Spatial distributions of six tree species on a 52-ha forest dynamics plot at Lambir Hills National Park, Sarawak, Borneo. Colors represent soil-types defined in Davies et al. 2005 listed here in order of increasing soil fertility: grey = sandy loam, light green = loam, green = fine loam, and dark green = clay.
Table SM2. For models of height-diameter (DBH), crown area-DBH, and crown depth-height allometry in six Bornean tree species, AIC values were compared between log-transformed data fitted in ordinary least squares regression (OLS) and for non-log transformed data fitted in nonlinear least squares regression (NLS). See methods section in main text for details.

<table>
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<tr>
<th>Species</th>
<th>Height-DBH AIC OLS</th>
<th>Height-DBH AIC NLS</th>
<th>Crown Area-DBH AIC OLS</th>
<th>Crown Area-DBH AIC NLS</th>
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<th>Crown Depth-Height AIC NLS</th>
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<td>109.4</td>
<td>116.2</td>
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Table SM3. For allometric relationships modeled in the form $\ln(X) = b \cdot \ln(Y) + \ln(a)$, we present parameters (intercept = $\ln(a)$; slope = $b$) with 95% confidence intervals fitted in major-axis regression for six Bornean tree species. For soil generalists, *K. latericia* and *M. beccariana*, we list overall species parameters followed by parameters fitted for conspecific populations sampled on sandy loam and clay-fine loam, respectively.

<table>
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<th>Height-DBH Intercept</th>
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<tr>
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Table SM3. (Continued).

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Table SM4. Parameters for allometric power function models of diameter growth rate, height, and crown area allometry fit using nonlinear least squares regression used to predict height and crown area growth in six Bornean tree species. The longevity of each tree species was estimate to provide reasonable axes for growth projections.

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<tr>
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<th>α</th>
<th>β</th>
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<th>b</th>
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<th>b</th>
<th>Estimated Longevity (years)</th>
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Table SM5. Parameters of allometric relationships \((\ln(X) = b\ln(Y) + \ln(a))\) fit using ordinary least squares regression with 95% upper and lower confidence limits for six Bornean tree species (intercept = \(\ln(a)\); slope = \(b\)). For generalists we list overall species parameters followed by parameters fitted for conspecific populations on sandy loam and clay-fine loam.

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