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Evaluation of the streambed leakage concept in analytical models using data from three pumping tests

Stefan J. Kollet · Vitaly A. Zlotnik

Abstract Two-dimensional analytical models of pumping induced drawdown and stream depletion account for the streambed properties and stream geometry. Using data from three pumping tests performed under various hydrologic conditions, the following hypotheses were tested: (1) a partially penetrating stream at a certain distance from the pumping well can be represented by the streambed leakage term in the analytical models; (2) in the streambed leakage term, the streambed conductance coefficient $\lambda = (WK')/m'$ accounts for the average stream width W , the streambed thickness m' , and hydraulic conductivity K' . The first hypothesis was tested by comparing results from tests under flow and no-flow stream conditions. The second hypothesis was tested by comparing results from two tests under low and high streamflow conditions. Similar estimates of the hydraulic conductivity and storativity for all tests indicate the validity of the streambed leakage term. The drawdown data of the test under low- and high-flow conditions (varying W) do not follow the predictions of the analytical models, which results in inconsistent λ estimates. Thus, for different hydrologic conditions, λ cannot be scaled solely by the stream width W . One possible explanation for this result is streambed dynamics caused by the changes in the stream stage.

Résumé Les rabattements dans les nappes et cours d'eau générés par des modèles analytiques de pompages en deux dimensions dépendent des propriétés du lit du cours d'eau considéré et de sa géométrie. En utilisant les données de

trois essais de pompages effectués en conditions hydrologiques contrastées, les hypothèses suivantes ont été testées: (1) un ruisseau à pénétration partielle situé à une certaine distance du puits de pompage peut être exprimé par le terme de drainance dans les modèles analytiques; (2) dans le terme de drainance du lit du cours d'eau, le coefficient de conductivité du lit $\lambda = (WK')/m'$ représente la largeur moyenne du cours d'eau W , l'épaisseur du lit m' , et la perméabilité K' . La première hypothèse a été testée en comparant les résultats des tests en conditions d'assèchement et d'écoulement. Pour éprouver la seconde hypothèse, les résultats de deux tests en conditions d'étiage et de hautes eaux ont été comparés. Sur l'ensemble des tests, la concordance entre les perméabilités calculées a permis de valider le terme de drainance du cours d'eau. Les rabattements observés en conditions d'étiage et de hautes eaux (W variable) ne suivent pas les prédictions des modèles analytiques, fournissant au final des estimations discordantes de λ . Aussi, dans le cas de conditions hydrologiques différentes, la seule largeur du cours d'eau ne suffit pas à estimer λ . Une explication possible de ce résultat réside dans la dynamique du lit causée par les variations de niveau du cours d'eau.

Resumen Modelos analíticos en dos dimensiones de descenso inducido por bombeo y de agotamiento de la corriente del río representan las propiedades del lecho del río y la geometría del mismo. Usando datos de tres ensayos de bombeo llevados a cabo bajo condiciones hidrológicas variadas, se probaron las siguientes hipótesis: (1) puede representarse un río parcialmente penetrante a una cierta distancia del pozo de bombeo por el término de goteo a través del lecho del río en los modelos analíticos; (2) en el término de goteo a través del lecho del río, el coeficiente de conductancia del lecho del río $\lambda = (WK')/m'$ representa el ancho promedio del río W , la potencia del lecho del río m' , y la conductividad hidráulica K' . La primera hipótesis fue comprobada comparando los resultados de pruebas bajo condiciones de flujo y no flujo de corriente. La segunda hipótesis fue probada comparando los resultados de dos pruebas bajo condiciones de corriente altas y bajas. Estimaciones similares de la conductividad hidráulica y el almacenamiento para todas las pruebas apuntan hacia la validez del término de goteo a través del lecho del río. Los datos de descensos de la prueba bajo condiciones de flujo altos y bajos (variando W)

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no siguen las predicciones de los modelos analíticos, lo que resulta en estimaciones inconsistentes de λ . Así, para condiciones hidrológicas diferentes, λ no puede ser escalada solamente con el ancho de la corriente W . Una posible explicación para este resultado es la dinámica del lecho del río causada por los cambios en el nivel del río.

Keywords Groundwater/surface-water relations · Hydraulic testing · Hydraulic properties · Groundwater hydraulics

Introduction

Over the last decade, studies of groundwater–surface-water interactions in alluvial valleys have expanded to a broad variety of physical, chemical, and biological processes at various scales that range from a ripple in the stream channel to a watershed—e.g., Packman and Bencala (2000), Harvey and Wagner (2000), Woessner (2000), Kasahara and Wondzell (2003), Cardenas et al. (2004). These studies utilized laboratory, field, and modeling approaches to derive properties of the streambed. In spite of the recent progress in streambed characterization, the problem of in situ determination of the hydraulic conductivity distribution and alluvial architecture (delineation of the streambed) remains. Small-scale hydraulic testing and geophysics (Bierkens and Weerts 1994; Butler et al. 2002; Cardenas and Zlotnik 2003; Ritzi et al. 2004) can be used with upscaling to obtain these parameters at scales commensurate to modeling applications. However, these types of studies are labor-intensive and time-consuming and are, thus, limited to site scales of 10^0 – 10^1 m.

The conductance concept, where an average streambed thickness and hydraulic conductivity is used, is widely accepted in large-scale models of stream–aquifer interactions (Anderson and Woessner 1992). Therefore, it is appealing to utilize this concept implemented in commonly applied modeling tools—e.g., MODFLOW, McDonald and Harbaugh (1996)—as an alternative to detailed streambed characterization in the following context. Models that explicitly incorporate the streambed thickness m' , average hydraulic conductivity K' , and stream width W , are used for parameter identification via inverse modeling. This identification yields “apparent” parameter estimates that control integral large-scale fluxes across the stream–aquifer interface. The choice between analytical and numerical models for this approach depends on the complexity of the hydrogeologic conditions and availability of field data. In many situations, with relatively scarce field data and simple site geometry, analytical models may be appropriate.

In applications, analytical models for simulating stream depletion are of paramount interest. These models were designed to evaluate effects of groundwater abstraction on stream runoff in alluvial aquifers (see a brief review by Zlotnik 2004). Streambed properties are among the major factors controlling the seepage magnitude across the channel bed. Because aquifer drawdown and water losses

from the stream can be used to identify the streambed properties, pumping test data including drawdown in multiple piezometers and flow and stage data from stream-gauging stations are needed.

In natural streams, streamflow discharge measurements and seepage meters have been applied with limited success due to relatively large measurement errors (Kaleris 1986; Sophocleous et al. 1988; Nyholm et al. 2003). Typically, the accuracy in stream discharge measurements is stated to be on the order of 5–10% of the actual streamflows (Hirsch and Costa 2004). To detect the effect of a well pumping at a constant rate of 6,000 m³/day, the average seepage rate across the streambed has to be significantly larger than 10% of the actual stream discharge. Therefore, applications of this approach are limited to the streams with discharges smaller than 1.4 m³/s under the assumption that 100% of the pumped water originates from the stream, which might not be the case. Because accurate discharge data can be obtained in special situations only (e.g., Hunt et al. 2001; Nyholm et al. 2002), this study is limited to drawdown data analysis. For example, in the study presented here, the pumping tests were performed with a constant rate of 6,480 m³/day. For the pumping test under low streamflow conditions, stream depletion rates were estimated to range from 20 to 50% of the pumping rate after 6 days of pumping (Kollet and Zlotnik 2003), which corresponds to 7–17% of the stream discharge (Fig. 1). Thus, it would not be feasible with the current technology to detect objectively the effect of pumping on discharge of the Prairie Creek, Nebraska, USA (Fig. 2) using direct measurements.

Three-dimensional analytical models of pumping tests near a stream are not available yet. Early two-dimensional

Fig. 1 Stream discharge during the pumping tests under low-flow conditions, PT_{low}, and high-flow conditions, PT_{high}, of Prairie Creek, Nebraska, USA, at the test site

Fig. 2 Prairie Creek test site in Nebraska, USA: **a** site location, **b** instrumentation and location of cross section A-A', and **c** hydrogeologic cross section A-A' (not to scale). The shaded area indicates the active channel and the white arrow indicates direction of streamflow; *x* and *y* indicate origin and orientation of the coordinate system of the applied analytical solutions (**b**). The cross section shows boundaries of the hydrogeologic units, positions of the piezometer screens and the pumping well (PW). Note the location of the piezometers at shallow, intermediate, and deep aquifer depths. Modified from Kollet and Zlotnik (2003)

analytical models of pumping-induced stream depletion were based on the image-well theory (Theis 1941; Glover and Balmer 1954). Major assumptions were those of a straight stream that fully penetrates the homogeneous aquifer. Later, Hantush (1965) introduced the concept of streambed conductance that approximates the stream-aquifer interface as a layer of uniform thickness and relatively low permeability. This concept was developed more out of mathematical convenience than sedimentologic concepts, but it is still widely applied (Anderson and Woessner 1992). Numerical studies found that the assumption of a fully penetrating stream may lead to an overestimation of stream depletion, and the solutions are highly sensitive to changes in the streambed conductance coefficient (e.g., Sophocleous et al. 1995; Conrad and Beljin 1996). However, no insight was provided in the

validity of the streambed conductance concept in stream-aquifer models.

Only recently, analytical models were improved to take into account partial stream penetration, a finite stream width, and also large-scale aquifer heterogeneity (Hunt 1999; Zlotnik et al. 1999; Butler et al. 2001). Yet, these two-dimensional models also rely on the application of the streambed conductance concept. A newer model by Hunt (2003) is not applicable in this study, because it is valid for semi-confined or leaky aquifer conditions only and the aquifer in this study is unconfined (Kollet and Zlotnik 2005a).

Simultaneously, with the advent of improved analytical models, results of two well-designed field studies aimed at a field verification of the theory were published (Hunt et al. 2001; Nyholm et al. 2002 and 2003). These studies

utilized pumping test data and stream discharge measurements for the inverse prediction of stream depletion rates and concluded that stream depletion rates are identifiable, though highly uncertain. These studies were performed along a drain and a small stream with widths of about 2 m and discharges less than 0.45 m³/s, far from conditions encountered in many natural stream-aquifer systems. Additionally, the observation networks used were not fully three-dimensional, thus, providing only limited insight into the response of the stream-aquifer system.

In studies of stream-aquifer interactions, water temperature has been used as a tracer to determine the direction of groundwater flow and flow velocities (e.g. Stallman 1965; Lapham 1989; Taniguchi 1993; Silliman and Booth 1993; Constantz et al. 2003; Brewster 2004). However, few studies of stream-aquifer interactions studied the effect of temperature on the kinematic viscosity of the water and, thus, the hydraulic conductivity. Constantz et al. (1994) discussed diurnal temperature effects on seepage rates. That study demonstrated qualitatively that the effect of temperature was the main reason for the variability in daily streamflow losses. Ronan et al. (1998) also studied diurnal fluctuations in seepage rates and included numerical modeling results in their study. Bravo and Jiang (2002) applied a coupled groundwater flow and heat transport model to account for the dependence of water density and viscosity on temperature. Using synthetic and field data, they solved the inverse problem based on head and temperature data. The objective of this study is to examine the validity of the streambed leakage and conductance concept in two-dimensional flow models using drawdown and stream water-temperature data from three pumping tests performed under distinct hydrologic conditions.

Model outline and hydrologic framework

Hunt (1999) and Butler et al. (2001) presented two-dimensional models of stream-aquifer interactions as a correction to the two-dimensional Theis (1935) solution for drawdown in a homogeneous confined aquifer (in the following, these models will be referred to as Hunt and BZT models). This correction can be illustrated by the Hunt model for drawdown, $s(x,y,t)$, as

$$s(x,y,t) = \frac{Q}{4\pi T} \left\{ E_1 \left[\frac{(\ell - x)^2 + y^2}{4Tt/S} \right] - \int_0^\infty e^{-\theta} E_1 \left[\frac{(\ell + |x| + 2T\theta/\lambda)^2 + y^2}{4Tt/S} \right] d\theta \right\},$$

$$(-\infty < x < \infty, -\infty < y < \infty, 0 < t < \infty)$$
(1)

On the right-hand side of Eq. (1), the first term is the Theis (1935) solution for drawdown in a confined aquifer and the second term describes the streambed leakage; x,y (L) are Cartesian coordinates; t (T) is time; Q (L³/T) is the

pumping rate; $T = Kb$ (L²/T) is the transmissivity; K (L/T) is the hydraulic conductivity; b (L) is the saturated aquifer thickness; S (–) is the aquifer storativity; ℓ (L) is the distance between the pumping well and stream (located along the y -axis); λ (L/T) is the streambed conductance coefficient; and θ is the dummy variable of integration. In this study, the term aquifer storativity refers to the specific yield of the aquifer material, because the models were applied only to the late time drawdown data (e.g. Neuman 1972).

Generally, λ may be approximated as

$$\lambda \approx (WK')/m', \quad (2)$$

where W (L) is the average stream width, K' (L/T) is the hydraulic conductivity, and m' (L) is thickness of the streambed sediments (Hunt et al. 2001; Zlotnik 2004). Note that the presence of a “low conductivity streambed layer” ($K' \ll K$) is essential for the validity of the models, because this layer facilitates the partially penetrating stream, while applying the Dupuit assumptions.

Equation (1) states that deviations in measured drawdown from the Theis (1935) solution caused by the presence of a stream may be readily quantified via the streambed leakage term. The practical validity of this solution may be tested by applying Eq. (1) to pumping test data collected in the absence and presence of a stream using identical monitoring networks and appropriate boundary conditions. Aquifer parameter estimates such as the transmissivity T and storativity S , must be identical under both hydrologic conditions.

Unfortunately, it is not possible to simply “turn on” and “turn off” a stream, especially under natural flow conditions, in order to perform the two pumping tests. Artificial test settings such as pumping tests along engineered ditches, may be seen as an alternative, yet they cannot serve as a substitute for studies of real-world stream-aquifer systems.

During the time period 1999–2001, a climatic opportunity emerged in the Platte River watershed, east-central Nebraska, USA, to perform pumping tests under distinct hydrologic conditions. Because of variable weather conditions, the meandering Prairie Creek near Columbus, Nebraska underwent transitions from low stream discharge (May 2000) to completely dry conditions (August 2000) and to relatively high stream discharge (June 2001). Figure 1 shows the stream discharge curves during the pumping test PT_{low} that was started in May 2000 and PT_{high} that was started in June 2001. The stream discharge was estimated utilizing the velocity-area concept and the velocities were measured using the 6/10th method (Rantz and others 1982).

The specific objectives of this study are to test the hypotheses that (1) the streambed leakage term accounts for a partially penetrating stream; and (2) the streambed conductance coefficient λ accounts for the average stream width and a streambed hydraulic conductivity and thickness. These hypotheses are tested by comparing the

results from the analysis of the pumping tests under no-flow and flow conditions of the stream and varying stream width.

Because the temperature of the infiltrating stream water was higher than the groundwater temperature, stream water temperature was monitored to assess the effect of the temperature on the hydraulic conductivity and possible impact on the analysis results. Note that two of the pumping tests have been partially analyzed and discussed previously. The pumping test under low-flow conditions was analyzed using the aforementioned two-dimensional analytical models of stream–aquifer interactions (Kollet and Zlotnik 2003). The test under no-flow conditions was analyzed using three-dimensional analytical and numerical models for aquifer heterogeneity interpretation (Kollet and Zlotnik 2005b). The study presented here provides a unique systematic analysis of stream–aquifer interactions under pumping and distinct hydrologic conditions.

The Prairie Creek test site and performance of pumping tests

The Prairie Creek test site is located along the naturally meandering Prairie Creek, Platte River watershed, east-central Nebraska, USA (Fig. 2). Prairie Creek is very shallow; the stream penetrates less than 5% of the saturated thickness of the underlying aquifer. The stream discharge is highly variable (0–50 m³/s under drought and spring runoff conditions). The width of Prairie Creek reaches approximately 25 m under bankfull flow. At the site, the unconfined aquifer has an average saturated thickness of about 17 m and consists of poorly sorted fine to coarse sand and gravel. The sediments are associated with the braided river depositional environment from paleochannels of the Platte River.

A high-capacity pumping well and eight piezometer clusters are present at the site. Each cluster contains three piezometers screened at shallow, intermediate, and deep aquifer depths. The completion depths of the piezometers in each cluster are indicated with the suffixes ‘s’ for shallow, ‘i’ for intermediate, and ‘d’ for deep (e.g., C1s: shallow piezometer of cluster 1). The pumping well is completed at the aquifer base at a depth of about 19.5 m with a casing diameter of 40 cm at a distance of 57 m from the stream. The screened interval extends from about 4.9 to 19.5 m aquifer depth and covers more than 80% of the saturated aquifer thickness under non-pumping conditions.

Three long-term pumping tests were performed at the Prairie Creek test site under distinct hydrologic conditions (Table 1). The test under low stream discharge conditions (PT_{low}) continued for 144 hours. The test under high stream discharge conditions and almost bankfull flow of Prairie Creek (PT_{high}) continued for 147 hours. During these tests, the pumped water was discharged back into the flowing stream at a distance of about 300 m downstream from the test site. Note the difference in the stream widths between the PT_{low} and PT_{high} tests. The test under dry stream conditions (PT) continued for 72 hours.

Table 1 Summary of pumping test characteristics at the Prairie Creek site

Pumping test characteristics	PT	PT _{low}	PT _{high}
Starting date	08/08/2000	30/05/2000	01/06/2001
Duration (hours)	72	144	147
Pumping rate (m ³ /day)	6,480	6,480	6,480
Mean stream discharge (m ³ /s)	0.0	0.25	1.65
Stream width (m)	0.0	10	20

This notation, PT_{low}, PT_{high}, and PT, will be used consistently in the ensuing analysis and discussion.

Before and during the three pumping tests, hydraulic head was monitored via pressure sensors in a number of piezometers (PT: C2s,i,d; C3s,i,d; C4s,i,d; C5s,i,d; PT_{low}: C2s,i,d; C4s,i,d; C5s,i,d; PT_{high}: C2s,i; C3s,i; C4s,i; C5s,i; C6s,i; C7s,i; C8s,i). In the remaining piezometers, hydraulic head measurements were taken manually. Water-level data collected before the start of pumping were used to derive the ambient groundwater flow direction that is indicated with the arrows in Fig. 2. The general direction did not change significantly among the different tests. Data from permanent and temporary piezometers in the stream showed that the stream reach at the site was initially under losing and gaining conditions for the tests PT_{low} and PT_{high}, respectively. It cannot be excluded, however, that during PT_{low} and PT_{high}, there were also gaining and losing areas along the streambed, respectively, because of small scale heterogeneity near the stream–aquifer interface. Because the applied governing equations are linear and based on the superposition principle, drawdowns can be calculated regardless of whether different portions of the stream are gaining or losing water. Data collected during the actual tests indicate that the water table adjacent to the stream edge never dropped below the streambed. Thus, the stream was always in direct hydraulic connection with the aquifer during the PT_{low} and PT_{high} tests.

Time-drawdown data and analysis

Examples of time-drawdown curves measured in the shallow, intermediate, and deep piezometers of cluster C2 at the point bar and cluster C5 at the cut bank are shown in Fig. 3. The measured time-drawdown behavior is characteristic of unconfined aquifers and exhibits the three distinct drawdown phases that are attributed to the interaction of compressible aquifer storage and the vertical movement of the free water-table surface in the unconfined aquifer (Neuman 1972 and 1974).

Comparison of the curves shows that the drawdowns up to 200 min (~0.1 day) of pumping are similar because water is mainly released from compressible aquifer storage. At cluster C5, differences at very early times (~0.01 day) are caused by fluctuations of the water column in the piezometer that are not resolved enough, because of the relatively large measurement interval of

Fig. 3 Drawdown in the piezometers of the clusters C2 and C5 during the pumping tests PT, PT_{low}, and PT_{high}. *s* shallow; *i* intermediate; and *d* deep

2 min. With continuing pumping, the boundary condition at the stream and induced seepage become important. As expected, maximum drawdown is observed during PT for large time periods. The differences in the drawdown magnitudes between the test without streamflow, PT, and both tests with streamflow, PT_{low} and PT_{high}, are mainly caused by seepage from the stream.

Comparison of data from PT_{low} and PT_{high} indicates that slightly larger drawdown was observed under high-flow conditions at Prairie Creek. This observation is not

intuitive, because one would expect increased seepage rates under higher flow stages and larger stream widths, which, in turn, reduce drawdown in the aquifer (Eqs. 1 and 2). Possible explanations for this drawdown behavior are provided in the Discussion section. For large times, the discrepancies in drawdown between PT_{low} and PT_{high} diminish notably.

Water-table recovery after pumping cessation was monitored over a relatively short time period compared to the pumping duration. Recovery phases of PT_{low} and

Table 2 Constants used in inverse modeling of pumping test data

Test	Constants (input)			
	Q (m ³ /day)	W (m)	ℓ (m)	b (m)
PT _{low}	6,480	10	57	16.9
PT	6,480	NA	NA	17.0
PT _{high}	6,480	20	47	17.2

Q pumping rate; W stream width; ℓ distance between the pumping well and the stream; b aquifer thickness; NA not applicable

PT_{high} show identical behavior. The early recovery phase of PT reveals qualitatively similar behavior. Note that recovery data were not utilized in the analysis because of unknown backflow into the well from the discharge pipes immediately after pumping cessation (no check-valve was used during the pumping tests).

For the analysis using two-dimensional analytical models that are based on the Dupuit assumptions, the data collected in the piezometers of the three-dimensional monitoring network were vertically averaged at the individual clusters C1–C8 (see approach by Kollet et al. 2002). This averaging resulted in eight depth-averaged time-drawdown curves, one for each cluster. In this study, the entire drawdown data from all piezometer clusters were analyzed simultaneously for the all three pumping tests (global cluster analysis). This type of analysis yields a single parameter vector.

Parameter identification

Data analysis was performed via inverse modeling using two-dimensional models. All models were applied to the late time-drawdown data ($t > 1.25$ days), when elastic storage effects cease and the vertical velocity of the declining water table becomes negligible.

Table 2 contains the constants that were used in the analysis to determine the hydraulic properties of the aquifer and the hypothetical streambed. The Hunt model of a homogeneous aquifer was used for interpreting the two-dimensional vertically averaged time-drawdown data. Minor variations of the saturated thickness b between the different tests were taken into account in determining the transmissivity values. Therefore, three fitting parameters were used to reproduce the observed drawdown in the case of PT_{low} and PT_{high}: the hydraulic conductivity, K , the aquifer storativity, S , and streambed conductance, λ , per unit stream length. In the case of the PT test in the

absence of flow in Prairie Creek, the Theis (1935) model was used, and the number of fitting parameters reduces to two, namely K and S .

The BZT model (Butler et al. 2001) was used in the global cluster analysis for simulating a piecewise-homogeneous aquifer that accounts for the meandering stream architecture of the modern Prairie Creek deposits. In the BZT model, the aquifer consists of three parallel, infinite strips: one underneath the stream and one for each stream bank. The stream banks in the model are named cut bank and point bar, which is consistent with the sedimentology at the site. The model assumes uniformity in S and a piecewise-uniform distribution of K from the point bar to the cut bank in an aquifer of infinite extent. In the applied BZT model, the point bar has a uniform but different hydraulic conductivity than the cut bank, because it consists of reworked and re-deposited alluvium of Prairie Creek, which migrates laterally due to the erosional and depositional process along the channel (Allen 1970). The resulting parameter vector includes four parameters: $K_{\text{point bar}}$, $K_{\text{cut bank}}$, λ , and S . The details on the application of piecewise-homogeneous aquifer model are provided in Kollet and Zlotnik (2003).

For nonlinear parameter optimization, the software package PEST2000 (Doherty 1994), which utilizes a Gauss-Marquardt-Levenberg algorithm, was linked to the analytical models. This algorithm minimizes the sum of equally weighted squared differences (residuals) between calculated and measured data. The logarithmic transformation of the parameter vectors was used for improvement of convergence (Hill 1998). Consecutive runs with varying initial parameter guesses were performed to test whether the global minimum of the sum of squared residuals function was reached.

Results of time-drawdown data analysis

In this section, the results from the drawdown data analysis are provided using the entire data set from all eight piezometer clusters simultaneously. Confidence limits, parameter correlation, and sensitivities, which would be beyond the scope of this study, have been discussed by Christensen (2000), Nyholm et al. (2002), and specifically, for the stream-aquifer system under investigation, by Kollet and Zlotnik (2003).

Table 3 Parameter estimates from the global cluster analyses (GCA) using the Hunt model (homogeneous aquifer) and BZT model (piecewise-homogeneous aquifer)

Applied model		K (m/day)			S (–)			λ (m/day)	
		PT	PT _{low}	PT _{high}	PT	PT _{low}	PT _{high}	PT _{low}	PT _{high}
Homogeneous		96	93	85	0.19	0.16	0.19	18.6	14.2
Piecewise-	Point bar	34	21	31					
					0.29	0.14	0.11	22.5	21.9
Homogeneous	Cut bank	108	115	107					

K aquifer hydraulic conductivity; S aquifer storativity; λ streambed conductance coefficient

Global cluster analysis, GCA

The parameter estimates from the simultaneous analysis of the entire data set are summarized in Table 3. The results of the GCA from all three tests PT_{low} , PT , and PT_{high} agree very well. Arithmetic mean values of the different parameters from the GCA results are as follows: $K \approx 92$ m/day, $S \approx 0.178$, and $\lambda \approx 16$ m/day. However, measured versus calculated data plots (Fig. 4) revealed a low degree of goodness of fit caused by trends in the data

matches (overestimation of the slope of the late time-drawdown curves).

An effort was made to consider large-scale aquifer heterogeneity using the BZT model of a piecewise-homogeneous aquifer (for details see Kollet and Zlotnik 2003). It can be argued that because of different depositional and erosional processes at the cut bank and point bar (meandering stream), differences are present in the hydrostratigraphy on a larger scale that might affect

Fig. 4 Measured versus calculated drawdown of the three pumping tests PT , PT_{low} , and PT_{high} from the global cluster analysis using the **a** homogeneous and **b** piecewise-homogeneous aquifer model

drawdown at the observation locations (Allen 1970). The aquifer was, therefore, divided into two sub-regions representing the point bar and the cut bank individually. Application of the sedimentologic rationale of the meandering stream architecture to the data of the different tests (PT_{low} , PT , and PT_{high}) resulted in excellent agreement in $K_{cut\ bank} \approx 110$ m/day, $K_{point\ bar} \approx 29$ m/day, and $\lambda \approx 22$ m/day. The $K_{point\ bar}$ estimates are in the bounds of the slug-test results from the point bar (Kollet and Zlotnik 2005a,b), though appear to be at the lower end of the distribution. The storativity value obtained from PT is $S = 0.29$ compared to $S \approx 0.125$ from the PT_{low} and PT_{high} tests (Table 3).

In Fig. 4, the measured versus calculated data plots obtained from the analysis using the piecewise-homogeneous aquifer model show a strong improvement in the curve fits for the tests PT_{low} and PT_{high} , and basically no improvement for the PT test when compared to the results obtained with the homogeneous aquifer model.

Discussion

The results from the analyses of PT_{low} and PT_{high} with the two-dimensional models of stream-aquifer interactions show that the uniform aquifer model provides relatively consistent parameter estimates. It appears that simultaneous use of all data (global analysis) provides a good agreement of results from the analysis of the data from the different pumping tests under varying hydrologic conditions. The agreement of K and S obtained from global analyses using the two-dimensional Hunt and BZT models (Table 3) suggests the validity of the streambed leakage concept. However, the stream width between the test PT_{low} and PT_{high} increased two-fold in the field (Table 1), which should result in a two-fold increase in the streambed conductance coefficient $\lambda = (WK')/m'$ in the analysis. This is not the case, though; λ decreases slightly in the interpretation of the test PT_{high} . The reason for this decrease in λ is the slight increase in the measured drawdown during PT_{high} . This result is inconsistent with the rationale that a wider stream causes larger seepage rates and, thus, smaller drawdown in the aquifer. In the following, focus will be placed on two possible explanations for this inconsistency in observed drawdown between PT_{low} and PT_{high} : (1) the effect of temperature on the hydraulic conductivity due to infiltration of warmer stream water into the aquifer; (2) changes in the hydraulic streambed properties, because of erosional and depositional processes as the bed adjusts to varying stream stages, i.e., a dynamic streambed.

The temperature effect necessitates much higher temperatures of the infiltrating stream water during PT_{low} compared to PT_{high} to compensate for the doubling in the stream width. However, the collected stream water-temperature data do not exhibit such a difference. Although there are differences of more than 10°C in peak temperature values over short time periods, the

Fig. 5 Streamwater temperatures during the pumping tests PT_{low} and PT_{high}

average temperature difference is only about 3°C over the course of the tests (Fig. 5, Table 4). This low average temperature difference and associated change in the streambed hydraulic conductivity cannot account for a doubling in the stream width in $\lambda = (WK')/m'$, if a constant streambed thickness m' is assumed. Therefore, the second explanation dealing with a dynamic streambed is explored further below.

The analysis of the pumping test data using analytical models is based on the major assumption that the streambed sediments were the same among the different tests, which implies a non-dynamic streambed. This assumption is violated even under small changes in the stream stage, which cause an immediate adjustment of the bed topography—erosion and deposition during rising and falling stream stage, respectively (e.g., Bridge 1977). The stream stage during PT_{high} was larger compared to the stage during PT_{low} , which caused considerable erosion and ensuing re-deposition of sediments in the stream channel. Therefore, the assumption of the streambed being the same sedimentary body during both tests is doubtful. However, the question arises, whether the sediments that were exposed by erosion or re-deposited before and

Table 4 Statistics of streamwater temperature during pumping tests PT_{low} and PT_{high}

Test	Number of points	Temperature ($^\circ\text{C}$)			
		Mean	Min	Max	CV
PT_{low}	4,321	21.5	12.7	31.5	0.20
PT_{high}	1,874	17.9	13.1	23.0	0.16

The coefficient of variation, CV, is defined as the ration between the standard deviation and the mean

during PT_{high} were significantly different compared to PT_{low} . Visual inspection and comparison of the streambed during PT_{low} and a dry period after PT_{high} did not show significant mud draping, armoring, or any other major differences. This result is obvious, because the composition of the sediments derived from the source areas and transported by the river did not change between the different tests. However, it cannot be excluded that the streambed sediments right at the stream-aquifer interface were different enough during PT_{low} and PT_{high} to produce a significant difference in K' between the two different tests. After eliminating temperature as the major reason for the inconsistency in drawdown and λ estimates between PT_{low} and PT_{high} , changes in streambed sediments and, thus, the hydraulic connection between the stream and the aquifer appear to be one likely explanation. Unfortunately, there is no field data to corroborate this rationale at the Prairie Creek test site, but the principles used here are well known and commonly applied in sedimentology (Allen 1970; Bridge and Jarvis 1976; Fraser and Davis 1998).

It is instructive to check the magnitude of λ using independent estimates of characteristic parameters at the site. Experimental data of Cardenas and Zlotnik (2003), which were collected in the summer of the year 2000, yielded $K'=15\text{--}20$ m/day using various averaging techniques for hydraulic conductivity of the streambed sediments from constant-head injection tests. They also proposed to use the depths of scour surfaces as a proxy for the streambed thickness m' ; estimates of this value from ground-penetrating radar surveys indicate that m' varies between 2 and 3 m. With the stream width W varying between 10 and 20 m (Table 1), an estimate of $\lambda=(WK')/m'$ yields values between 60 and 100 m/day. These values exceed λ estimates from inverse modeling, which are summarized in Table 3, by a factor greater than 3. Thus, there is a significant overestimation in independently determined λ values from upscaled small-scale hydraulic test results compared to values inferred from pumping test data analysis, which may result in a 100% difference in seepage rate estimates.

The effect of possible large-scale aquifer heterogeneity in the hydraulic conductivity was also demonstrated in this study following the approach by Kollet and Zlotnik (2003). By using a two-dimensional approximation of the point bar-cut bank hydrostratigraphy, which resulted in a simple piecewise-homogeneous model of the meandering stream architecture, better matches were obtained between the measured and calculated data for the PT_{low} and PT_{high} tests. However, the analysis of PT without stream discharge using the piecewise-homogeneous model did not improve the data match and resulted in much larger storativity estimates compared to the results from PT_{low} and PT_{high} (Fig. 4 and Table 3). Thus, the interpretation of the PT pumping test under dry stream conditions requires further discussion.

Prior to the PT test, the stream was completely dry over several weeks and the water table was about 10–20 cm below the streambed at the site. During PT, the pumped

water was discharged back into the dry stream channel at a distance greater than 200 m downstream from the site. Kollet and Zlotnik (2005a,b) showed that re-infiltration and resulting aquifer return flow was likely during the pumping test and studied the effect on parameter estimates. They used three-dimensional analytical (e.g., Neuman 1974) and numerical models in their analysis of PT. Their estimates of the hydraulic conductivity ($K\approx 100$ m/day) agree well when compared to results in the section [Results of time-drawdown data analysis](#), despite that simpler two-dimensional models were used in this study. In the case of PT, aquifer return flow had the largest effect on S estimates. Analysis of the data using models without aquifer return flow arrived at storativity estimates of $S\approx 0.3$ compared to $S\approx 0.12$ using models that incorporate aquifer return flow. From these results, it is concluded that aquifer return flow is the major reason for larger storativity estimates from PT test in this study. Incorporation of aquifer return flow resulted in maximum increase in the K estimates of some 15%, which suggest that neglecting this process in the analysis using two-dimensional models does not have a major effect on the K estimates and does not change the results and conclusions of this study. Note that shallow aquifer return flow cannot be approximated in the two-dimensional analytical models applied in this study, because these models are based on depth-averaged drawdown.

Summary and conclusions

Interpretation of a drawdown and temperature data set from three pumping tests performed at the Prairie Creek site provides insight into the validity of the streambed conductance concept as an integral characteristic for streambed properties and geometry. Three pumping tests were performed under different hydrologic conditions: high stream discharge (PT_{high}), low stream discharge (PT_{low}), and under drought conditions without stream discharge (PT). Analyses of the unique data set allows for the testing of the streambed leakage term in the Hunt and BZT models, which reduce to the Theis (1935) solution in absence of a stream. Comparison of the time-drawdown data from the PT_{low} and PT_{high} tests with the PT test indicates that the effect of the shallowly penetrating stream on drawdown responses is clearly detectable. Anomalies in drawdown responses between PT_{low} and PT_{high} (drawdown is generally larger when there is a larger stream width during PT_{high}) may be caused by the dynamics of the streambed (erosion and deposition). This result is directly reflected in the estimates of the conductance coefficient λ .

Simultaneous (global) analysis of all data from each test shows good agreement between estimates from different tests, but may lead to poor matches between calculated and measured data in individual clusters/piezometers. Application of a piecewise-homogeneous BZT model implicitly considering the meandering stream architecture of modern stream deposits improves these

matches, which may suggest large-scale aquifer heterogeneity on the point-bar scale.

The good agreement between the analysis results of the test data in the presence and absence of Prairie Creek, Nebraska, USA suggests the usefulness of the stream approximation in the two-dimensional Hunt and BZT models. However, the large change in the stream width from test PT_{low} to test PT_{high} was not reflected in estimates of the streambed conductance coefficient $\lambda = (WK')/m'$, because of similar drawdown during PT_{high} that occurred despite a two-fold increase in the stream width compared to PT_{low}. After eliminating temperature effects as the major reason for this inconsistency, streambed dynamics, i.e., the adjustment of the streambed topography to changes in the stream stage, were discussed as one possible explanation. The study clearly shows that λ is not scalable by the stream width W for different hydrologic conditions and apparently does not account for an average streambed hydraulic conductivity and thickness. This result has major implications for stream depletion predictions in hydrologic systems where the stream width strongly depends on the stream discharge.

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