

The effect of belowground resources on light-affected allometry in six
Bornean tree species: Supplementary materials.

Katherine D. Heineman^{1*}, Ethan Jensen¹, Autumn Shapland¹, Brett Bogenrief¹, Sylvester Tan³, Richard Rebarber², and Sabrina E. Russo¹.

1 School of Biological Sciences, University of Nebraska-Lincoln, Nebraska, 68508, USA

2 Department of Mathematics, University of Nebraska-Lincoln, Nebraska, 68508, USA

3 Center for Tropical Forest Science and Forest Research Centre, Sarawak Forestry Corporation, Kuching, Sarawak, Malaysia

*Author for correspondence: kheineman@life.illinois.edu

Fig SM1. Spatial distributions of six tree species on a 52-ha forest dynamics plot at Lambir Hills National Park, Sarawak, Borneo. Colors represent soil-types defined in Davies *et al.* 2005 listed here in order of increasing soil fertility: grey = sandy loam, light green = loam, green = fine loam, and dark green = clay.

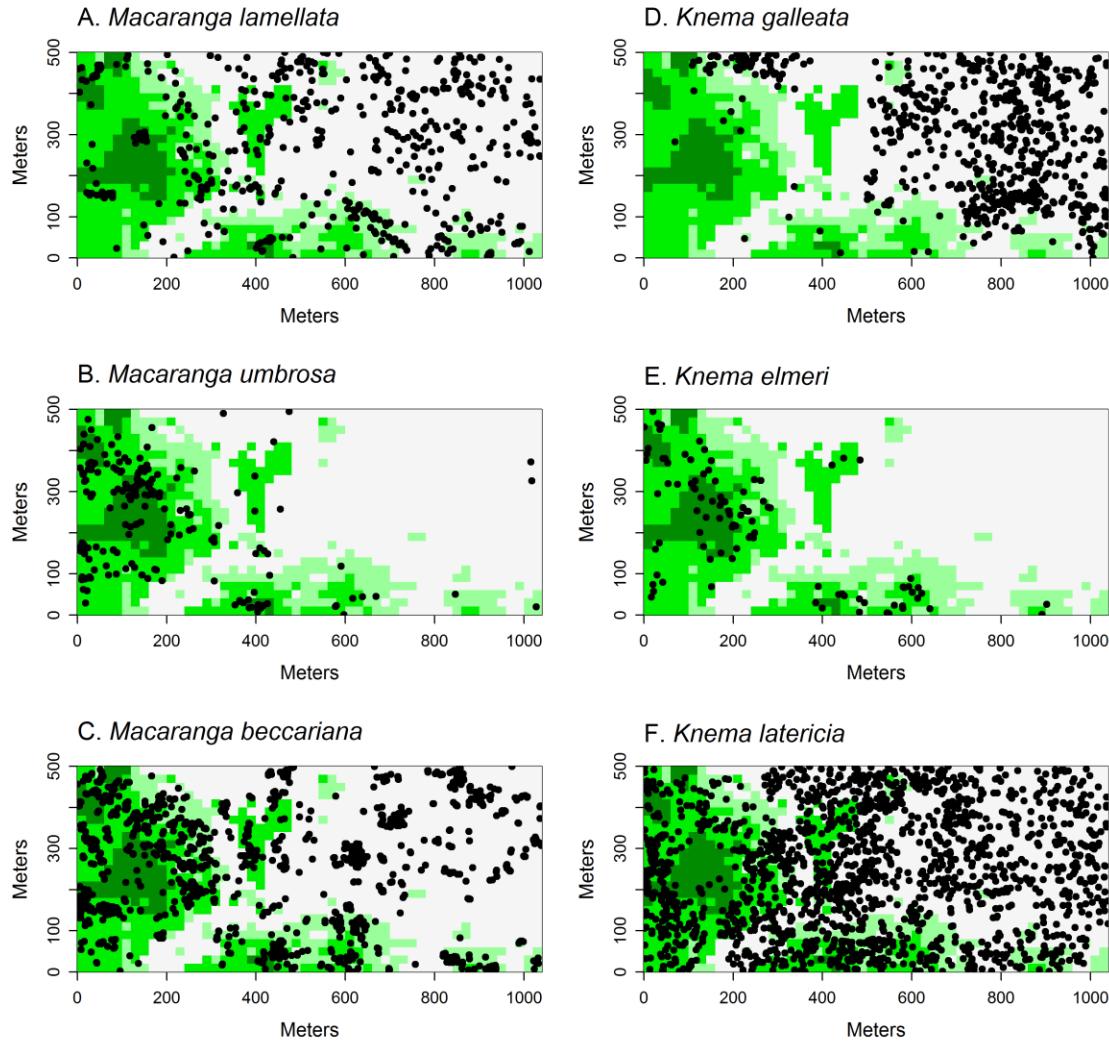


Table SM2. For models of height-diameter (DBH), crown area-DBH, and crown depth-height allometry in six Bornean tree species, AIC values were compared between log-transformed data fitted in ordinary least squares regression (OLS) and for non-log transformed data fitted in nonlinear least squares regression (NLS). See methods section in main text for details.

| Species | Height-DBH AIC | | Crown Area-DBH AIC | | Crown Depth-Height AIC | |
|----------------------|----------------|-------|--------------------|-------|------------------------|-------|
| | OLS | NLS | OLS | NLS | OLS | NLS |
| <i>K. galeata</i> | 129.8 | 150.7 | 144.3 | 190.2 | 109.4 | 116.2 |
| <i>K. elmeri</i> | 109.0 | 119.2 | 172.7 | 225 | 97.5 | 113.3 |
| <i>M. lamellata</i> | 140.5 | 165.8 | 168.5 | 195 | 100.9 | 129 |
| <i>M. umbrosa</i> | 170.2 | 169.6 | 179 | 284.4 | 113.8 | 147.8 |
| <i>K. latericia</i> | 260.4 | 270 | 273.5 | 384.8 | 215.1 | 215 |
| sandy loam | 146.7 | 137.3 | 139.1 | 191.3 | 115.6 | 97.3 |
| clay-fine loam | 111.9 | 131.4 | 135.5 | 196.2 | 105.2 | 118.8 |
| <i>M. beccariana</i> | 363.0 | 386.2 | 442.6 | 542.7 | 274.1 | 281.5 |
| sandy loam | 185.6 | 190.5 | 233.5 | 261.5 | 158.1 | 149.3 |
| clay-fine loam | 199.5 | 197.5 | 214.1 | 282.7 | 118.2 | 133.7 |

Table SM3. For allometric relationships modeled in the form $\ln(X) = b*\ln(Y) + \ln(a)$, we present parameters (intercept = $\ln(a)$; slope = b) with 95% confidence intervals fitted in major-axis regression for six Bornean tree species. For soil generalists, *K. latericia* and *M. beccariana*, we list overall species parameters followed by parameters fitted for conspecific populations sampled on sandy loam and clay-fine loam, respectively.

| Species | Height-DBH | | | | | | Crown Area-DBH | | | | | |
|----------------------|------------|-------|-------|-------|-------|-------|----------------|-------|-------|-------|-------|-------|
| | intercept | | | slope | | | intercept | | | slope | | |
| | mean | lower | upper | mean | lower | upper | mean | lower | upper | mean | lower | upper |
| <i>K. galeata</i> | 0.87 | 0.71 | 1.03 | 0.83 | 0.74 | 0.92 | -0.6 | -1.13 | -0.06 | 1.24 | 0.97 | 1.61 |
| <i>K. elmeri</i> | 0.62 | 0.46 | 0.79 | 0.76 | 0.68 | 0.84 | -0.67 | -1.15 | -0.2 | 1.55 | 1.34 | 1.81 |
| <i>M. lamellata</i> | 0.85 | 0.69 | 1.02 | 0.89 | 0.78 | 1.03 | -1.05 | -1.62 | -0.48 | 1.94 | 1.56 | 2.49 |
| <i>M. umbrosa</i> | 0.72 | 0.52 | 0.92 | 0.9 | 0.75 | 1.07 | -2.27 | -3.07 | -1.47 | 2.55 | 2.03 | 3.36 |
| <i>K. latericia</i> | 0.49 | 0.45 | 0.73 | 0.89 | 0.79 | 1.00 | -1.30 | -1.64 | -0.96 | 1.83 | 1.61 | 2.10 |
| sandy loam | 0.7 | 0.49 | 0.9 | 0.86 | 0.73 | 1.00 | -1.43 | -1.88 | -0.99 | 1.81 | 1.55 | 2.14 |
| clay-fine loam | 0.51 | 0.32 | 0.71 | 0.89 | 0.75 | 1.06 | -1.2 | -1.75 | -0.65 | 1.89 | 1.52 | 2.42 |
| <i>M. beccariana</i> | 1.17 | 1.00 | 1.34 | 0.66 | 0.58 | 0.75 | -1.95 | -2.47 | -1.44 | 2.05 | 1.81 | 2.34 |
| sandy loam | 1.3 | 1.02 | 1.57 | 0.61 | 0.49 | 0.75 | -1.91 | -2.81 | -1.01 | 2.01 | 1.64 | 2.53 |
| clay-fine loam | 1.14 | 0.92 | 1.37 | 0.66 | 0.54 | 0.79 | -2.02 | -2.72 | -1.32 | 2.12 | 1.79 | 2.57 |

Table SM3. (Continued).

| Species | Crown Depth-Height | | | | | |
|----------------------|--------------------|-------|-------|--------------|-------|-------|
| | <u>intercept</u> | | | <u>slope</u> | | |
| | mean | lower | upper | mean | lower | upper |
| <i>K. galleata</i> | -5.35 | -8.04 | -2.65 | 2.53 | 1.76 | 4.73 |
| <i>K. elmeri</i> | -1 | -1.52 | -0.5 | 1.05 | 0.83 | 1.33 |
| <i>M. lamellata</i> | -3.91 | -6.83 | -0.98 | 2.15 | 1.14 | 6.73 |
| <i>M. umbrosa</i> | -5.04 | -7.05 | -3.02 | 2.82 | 1.99 | 4.55 |
| <i>K. latericia</i> | -1.56 | -2.06 | -1.08 | 1.28 | 1.04 | 1.60 |
| sandy loam | -1.66 | -2.28 | -1.04 | 1.25 | 0.97 | 1.63 |
| clay-fine loam | -1.88 | -2.82 | -0.94 | 1.58 | 1.11 | 2.4 |
| <i>M. beccariana</i> | -5.53 | -7.05 | -4.02 | 2.60 | 2.08 | 3.38 |
| sandy loam | -8.29 | -11.8 | -4.76 | 3.59 | 2.57 | 5.75 |
| clay-fine loam | -4.44 | -6.25 | -2.64 | 2.19 | 1.58 | 3.32 |

Table SM4. Parameters for allometric power function models of diameter growth rate, height, and crown area allometry fit using nonlinear least squares regression used to predict height and crown area growth in six Bornean tree species. The longevity of each tree species was estimate to provide reasonable axes for growth projections.

| | Growth Rate-DBH | | Height-DBH | | Crown Area-DBH | | Estimated Longevity (years) |
|----------------------|-----------------|---------|------------|------|----------------|------|-----------------------------|
| Species | α | β | a | b | a | b | |
| <i>K. galeata</i> | 0.04 | 0.06 | 3.05 | 0.71 | 1.42 | 0.80 | 300 |
| <i>K. elmeri</i> | 0.33 | 0.07 | 1.76 | 0.78 | 2.18 | 0.96 | 165 |
| <i>M. lamellata</i> | 0.15 | -0.20 | 2.79 | 0.78 | 0.94 | 1.26 | 105 |
| <i>M. umbrosa</i> | 0.09 | 0.32 | 2.53 | 0.76 | 0.83 | 1.24 | 128 |
| <i>K. latericia</i> | | | | | | | 360 |
| sandy loam | 0.02 | 0.28 | 2.20 | 0.81 | 0.36 | 1.55 | - |
| clay-fine loam | 0.04 | 0.06 | 1.83 | 0.83 | 0.57 | 1.44 | - |
| <i>M. beccariana</i> | | | | | | | 28 |
| sandy loam | 0.38 | -0.09 | 5.0 | 0.48 | 0.55 | 1.43 | - |
| clay | 1.26 | -0.26 | 3.3 | 0.64 | 0.25 | 1.83 | - |

Table SM5. Parameters of allometric relationships ($\ln(X) = b*\ln(Y) + \ln(a)$) fit using ordinary least squares regression with 95% upper and lower confidence limits for six Bornean tree species (intercept = $\ln(a)$; slope = b). For generalists we list overall species parameters followed by parameters fitted for conspecific populations on sandy loam and clay-fine loam.

| Species | Height-DBH | | | | | | Crown Area-DBH | | | | | |
|----------------------|------------|-------|-------|-------|-------|-------|----------------|-------|-------|-------|-------|-------|
| | intercept | | | slope | | | intercept | | | slope | | |
| | mean | lower | upper | mean | lower | upper | mean | lower | upper | mean | lower | upper |
| <i>K. galeata</i> | 0.95 | 0.80 | 1.10 | 0.79 | 0.70 | 0.87 | -0.16 | -0.62 | 0.29 | 0.98 | 0.72 | 1.23 |
| <i>K. elmeri</i> | 0.66 | 0.49 | 0.83 | 0.74 | 0.66 | 0.82 | -0.40 | -0.84 | 0.05 | 1.40 | 1.17 | 1.62 |
| <i>M. lamellata</i> | 0.92 | 0.77 | 1.07 | 0.83 | 0.72 | 0.95 | -0.49 | -0.94 | -0.05 | 1.46 | 1.13 | 1.80 |
| <i>M. umbrosa</i> | 0.85 | 0.67 | 1.03 | 0.79 | 0.66 | 0.93 | -1.22 | -1.77 | -0.66 | 1.68 | 1.26 | 2.10 |
| <i>K. latericia</i> | 0.68 | 0.55 | 0.82 | 0.81 | 0.72 | 0.91 | -0.87 | -1.16 | -0.58 | 1.49 | 1.29 | 1.69 |
| sandy loam | 0.78 | 0.59 | 0.98 | 0.79 | 0.67 | 0.92 | -1.09 | -1.49 | -0.70 | 1.56 | 1.31 | 1.81 |
| clay-fine loam | 0.62 | 0.44 | 0.80 | 0.81 | 0.67 | 0.95 | -0.68 | -1.13 | -0.24 | 1.44 | 1.11 | 1.78 |
| <i>M. beccariana</i> | 1.28 | 1.12 | 1.44 | 0.60 | 0.52 | 0.68 | -1.19 | -1.60 | -0.77 | 1.65 | 1.44 | 1.86 |
| sandy loam | 1.41 | 1.15 | 1.67 | 0.55 | 0.43 | 0.68 | -1.02 | -1.72 | -0.33 | 1.57 | 1.23 | 1.89 |
| clay-fine loam | 1.24 | 1.03 | 1.45 | 0.60 | 0.49 | 0.72 | -1.29 | -1.86 | -0.72 | 1.71 | 1.40 | 2.01 |

Table SM5 (Continued).

| Species | Crown Depth-Height | | | | | | Safety Factor-DBH | | | | | |
|----------------------|--------------------|-------|-------|--------------|-------|-------|-------------------|-------|-------|--------------|-------|-------|
| | <u>intercept</u> | | | <u>slope</u> | | | <u>intercept</u> | | | <u>slope</u> | | |
| | mean | lower | upper | mean | lower | upper | mean | lower | upper | mean | lower | upper |
| <i>K. galleata</i> | -1.46 | -2.41 | -0.51 | 0.93 | 0.52 | 1.33 | 0.42 | 0.27 | 0.58 | -0.12 | -0.20 | -0.04 |
| <i>K. elmeri</i> | -0.7 | -1.15 | -0.24 | 0.89 | 0.68 | 1.10 | 0.71 | 0.54 | 0.87 | -0.07 | -0.16 | 0.01 |
| <i>M. lamellata</i> | -1.01 | -1.89 | -0.13 | 0.62 | 0.18 | 1.07 | 0.47 | 0.31 | 0.62 | -0.17 | -0.29 | -0.06 |
| <i>M. umbrosa</i> | -1.99 | -2.73 | -1.25 | 1.17 | 0.78 | 1.57 | 0.52 | 0.34 | 0.71 | -0.13 | -0.26 | 0.01 |
| <i>K. latericia</i> | -0.91 | -1.26 | -0.56 | 0.9 | 0.71 | 1.09 | 0.68 | 0.55 | 0.82 | -0.15 | -0.24 | -0.06 |
| sandy loam | -1.12 | -1.61 | -0.64 | 0.97 | 0.72 | 1.21 | 0.58 | 0.39 | 0.78 | -0.13 | -0.25 | -0.01 |
| clay-fine loam | -0.81 | -1.37 | -0.25 | 0.89 | 0.54 | 1.22 | 0.75 | 0.57 | 0.93 | -0.14 | -0.28 | 0.00 |
| <i>M. beccariana</i> | -2.6 | -3.42 | -1.78 | 1.39 | 1.06 | 1.72 | 0.12 | -0.03 | 0.28 | 0.07 | -0.01 | 0.14 |
| sandy loam | -3.5 | -5.1 | -1.91 | 1.74 | 1.12 | 2.36 | -0.01 | -0.27 | 0.25 | 0.11 | -0.01 | 0.23 |
| clay-fine loam | -2.11 | -3.08 | -1.13 | 1.18 | 0.76 | 1.59 | 0.16 | -0.05 | 0.37 | 0.06 | -0.05 | 0.17 |