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Numerically Predicting Seepage Gradient Forces and Erosion: Sensitivity to Soil Hydraulic Properties

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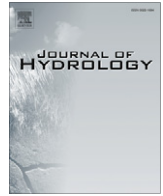
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Numerically predicting seepage gradient forces and erosion: Sensitivity to soil hydraulic properties

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SUMMARY

Research has suggested that streambank seepage can be an important mechanism of bank instability; however, limited information is available on the level of soil characterization necessary to accurately predict seepage gradient forces and erosion. The objective of this research was to quantify the expected range of predicted seepage gradients for various degrees of site characterization. Uncertainty analysis on seepage gradient predictions was performed relative to variability in soil hydraulic properties. A two-dimensional unsaturated/saturated groundwater flow model was used to simulate a homogeneous soil layer for sand and loamy sand soils packed at various bulk densities, ρ_b . A pedotransfer function (ROSETTA), designed to estimate unsaturated hydraulic properties from surrogate soil data (i.e., texture and bulk density), was used to derive the saturated hydraulic conductivity, K_s , and water retention parameters for various levels of site information (i.e., only textural class; percent sand, silt, and clay (%SSC); %SSC and ρ_b ; and %SSC, ρ_b , and K_s). Statistical distributions were derived for each soil hydraulic parameter and Monte Carlo simulations were performed to generate distributions of maximum seepage gradient. The deviation in predicted seepage gradient was calculated using assumed baseline conditions. Ranges in predicted soil hydraulic parameters and maximum seepage gradients were considerably reduced when using %SSC as compared to soil texture. Therefore, at a minimum, soil samples should be taken for particle size analysis. For ρ_b between 1450 and 1500 kg m⁻³, soil hydraulic parameters could be derived using ROSETTA and inputting %SSC, with little additional benefit provided by measuring ρ_b and/or K_s . When the ρ_b was less than 1450–1500 kg m⁻³, inputting ρ_b and/or K_s consistently reduced the magnitude of deviations from the baseline and therefore should be measured from undisturbed soil samples. The opposite was observed for ρ_b greater than 1450–1500 kg m⁻³ due to discrepancies between ROSETTA-derived and actual values of soil hydraulic parameters other than K_s . Considerable deviations (i.e., around 20%) were observed in seepage gradients under this scenario. When ROSETTA-derived and actual values of soil hydraulic parameters more closely matched, inputting ρ_b and/or K_s benefitted seepage gradient predictions as deviations in seepage gradients were less than 5% for the sand and loamy sand soils. Therefore, it is vital to quantify all soil hydraulic parameters for high ρ_b soils and textures with a wide range in %SSC.

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1. Introduction

Streambank failures result in loss of land, increased stream sediment loads, and increased nutrient loads if soil nutrient levels are high. Long-term data from Goodwin Creek, Mississippi, show that up to 85% of the sediment leaving the catchment

emanated not from the adjacent fields (cropland constituted around 10% of the area) but from the streambanks and beds (Grissinger et al., 1991; Simon and Darby, 1997; Wilson et al., 2007). Other research has also demonstrated that streambank erosion contributes significantly to total sediment loading in streams (Bull and Kirkby, 1997; Simon and Darby, 1999; Sekely et al., 2002; Evans et al., 2006). However, the relative importance of various mechanisms of streambank erosion remains unclear (Hooke, 1979; Odgaard, 1991; Fox et al., 2007a,b; Fox and Wilson, 2010).

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At least three groundwater mechanisms of streambank erosion and failure have been observed (Fox and Wilson, 2010). First, an increase in soil moisture can reduce cohesion and soil frictional strength (Darby and Thorne, 1996; Crosta and di Prisco, 1999; Rinaldi and Casagli, 1999; Simon et al., 1999). The importance of this instability mechanism has led to work by Darby et al. (2007), Rinaldi et al. (2008), and Langendoen et al. (2009) in linking groundwater flow, fluvial hydraulics, and streambank stability models.

The second and third mechanisms relate to seepage flow through soil layers towards the stream. Hagerty (1991a,b) discussed the difficulty of identifying sites with seepage in the field, especially since seepage is often intermittent. It is largely unknown whether sites with potential for seepage erosion can be predicted during a field reconnaissance based on easily defined soil properties (e.g., texture). Seepage often results from a perched water table above a restrictive layer. Wilson et al. (2007) observed a two and a half order of magnitude difference in vertical saturated hydraulic conductivity (K_s) in a bank profile that resulted in a perched water table and seepage. This difference was the result of only a 16% change in clay content between layers. Wilson et al. (2007) also noted that such layers may be thin alluvial deposits of 5–10 cm. Fox et al. (2007a) noted much smaller differences (around one order of magnitude) in vertical K_s among soil layers that also resulted in seepage.

When seepage occurs, seepage gradient forces (SF) exert body forces on streambank sediment proportional to the hydraulic gradient (Lobkovsky et al., 2004; Chu-Agor et al., 2009):

$$SF = \gamma_w i V \quad (1)$$

where γ_w is the unit weight of water, i is the seepage gradient, and V is the volume of the soil mass. Also, undercutting due to seepage exfiltration can add to streambank instability (Fox et al., 2006; Wilson et al., 2007; Cancienne et al., 2008; Chu-Agor et al., 2008a,b; Lindow et al., 2009). At the point where water exits the bank, erosion can occur producing cave-like features called seepage undercuts (Chu-Agor et al., 2008a, 2009). As these undercuts become larger, supporting material is lost which can lead to cantilever failures. This process has been noted to occur in numerous geographical locations (Fox et al., 2007a,b; Wilson et al., 2007) and its importance on stability has been highlighted in recent research (Cancienne et al., 2008; Chu-Agor et al., 2008a,b). Empirical models have recently been proposed that relate the seepage erosion rate to the ground water flow gradient and mimic excess shear stress equations used for fluvial erosion:

$$E_{rs} = k_{se} [i - i_{cr}]^a \quad (2)$$

where E_{rs} is the seepage erosion rate (i.e., mass of sediment per bank face area of the undercut per time, $\text{kg m}^{-2} \text{s}^{-1}$), k_{se} is the seepage erosion erodibility coefficient ($\text{kg m}^{-2} \text{s}^{-1}$), a is a power term typically assumed to be unity (Fox et al. (2007a) reports $a = 1$ for field measurements and Chu-Agor et al. (2009) reports $a = 1.2$ based on laboratory experiments), i is the hydraulic gradient based on the groundwater steady-state velocity, and i_{cr} is the critical gradient, which was estimated by Chu-Agor et al. (2009) based on laboratory experiments for sand and loamy sand soils. Eq. (2) was based on average hydraulic gradients (i.e., based on two or fewer measurements of the water table elevation along a transect in the near-bank ground water) to simplify application of the function to field scenarios (Fox and Wilson, 2010).

For both seepage gradient forces and erosion, it is the maximum seepage gradient (i_{max}), which typically occurs near the outflow boundary (i.e., streambank face), that leads to the maximum seepage force in Eq. (1) and the maximum potential for seepage erosion at the bank face. Predicting i_{max} requires the simulation of the ground water flow dynamics in the streambank. Variably saturated

flow models integrated with bank stability models are used to predict bank failure (Chu-Agor et al., 2008a,b); however, an improved understanding of the soil conditions under which seepage mechanisms become prevalent is needed (Langendoen et al., 2008). Groundwater seepage is driven by several soil hydraulic properties. A critical issue facing ground water flow models has always been estimation of the representative K_s due to the multitude of factors that influence K_s (Masrouri et al., 2008). This parameter has been suggested to vary more than any other engineering soil parameter (Cedergren, 1967), ranging over nine orders of magnitude for different materials. Ideally, data on water retention and hydraulic conductivity functions, among other soil properties, are needed to adequately model seepage. However, these data often are not available and are uneconomical and/or laborious to acquire.

While measured hydraulic parameters are ideal for modeling unsaturated flow, pedotransfer functions (PTFs) are a convenient option for estimating missing parameters based on readily available soil data (Nemes and Rawls, 2004). The use of one such computer program, ROSETTA, is highlighted in this paper. ROSETTA is a neural network model that predicts hydraulic parameters (residual water content (θ_r), saturated water content (θ_s), van Genuchten (1980) parameters (α and n), and K_s) for various levels of soil data (Schaap et al., 2001). ROSETTA is composed of five hierarchical PTFs for five levels of input data: (1) soil texture only; (2) percent sand, silt, and clay (%SSC); (3) %SSC and bulk density (ρ_b); and the previous parameters with water pressure at (4) field capacity and (5) at wilting point. In many cases, soil texture may be the only soil physical description available for a particular site.

The objective of this research was to quantify the expected range of predicted seepage gradients given various levels of site characterization including known, or measured, data compared to assumed values. This paper addresses seeps through a sand or loamy sand conductive layer that did not involve preferential flow through a biological or structural channel. Seeps due to preferential flow have been observed along streambanks (i.e., Fox et al., 2007a; Fox and Wilson, 2010) but were outside the scope of this investigation. This research utilized soil hydraulic parameters measured from a set of laboratory experiments on two soils susceptible to seepage (sand and loamy sand) and packed at three different ρ_b (Chu-Agor et al., 2008b).

2. Materials and methods

2.1. Simulating seepage

A homogenous, single-layer profile 10-cm high and 100-cm long with a 0% slope was numerically modeled for unsaturated and saturated flow (Fig. 1). The dimensions of the layer, specifically the 10-cm seepage layer height, were selected so as to mimic natural seepage layers observed in field experiments (Fox et al., 2006; Wilson et al., 2007). A MATLAB program (Langendoen et al., 2008) was used to solve the two-dimensional Richard's equation:

$$\left(\frac{\theta}{\phi} S_s + C \right) \frac{\partial h(x, z, t)}{\partial t} = \frac{\partial}{\partial x} \left[K(h) \frac{\partial h(x, z, t)}{\partial x} \right] + \frac{\partial}{\partial z} \left[K(h) \frac{\partial h(x, z, t)}{\partial z} \right] \quad (3)$$

where h is the pressure head, $K(h)$ is the hydraulic conductivity, θ is the water content, ϕ is the porosity, S_s is the specific storage, C is the specific moisture capacity, x is the lateral dimension, z is the vertical dimension, and t is time. Following the approach of Celia et al. (1990), Langendoen et al. (2008) approximated Eq. (3) on a cell-centered finite difference grid using a modified Picard iteration scheme coupled with a backward Euler approximation in time. The water retention function, $\theta(h)$, was defined using the van Genuchten (1980) model, and $K(h)$ was defined using the combination of the

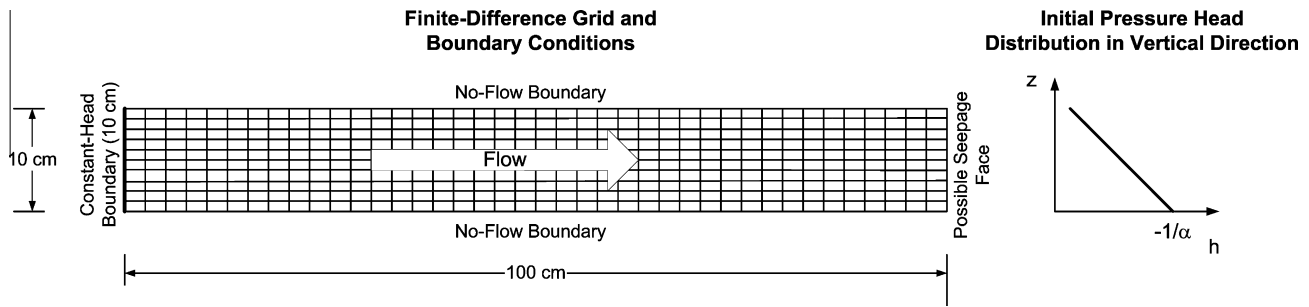


Fig. 1. Homogeneous, single-layer soil profile, including depiction of finite difference grids, boundary conditions, and initial conditions, modeled in MATLAB. The initial pressure head for all cells at the bottom of the grid was set equal to $-1/\alpha$, where α is the van Genuchten (1980) parameter, with a vertical, hydrostatic pressure distribution with elevation.

van Genuchten (1980) model with the Mualem (1976) pore-size distribution model:

$$\theta(h) = \begin{cases} \theta_r + \frac{\theta_s - \theta_r}{[1 + |\alpha h|]^m} & h < 0 \\ \theta_s & h \geq 0 \end{cases} \quad (4)$$

$$K(h) = K_s S_e [1 - (1 - S_e^{1/m})^m]^2 \quad (5)$$

where S_e is the effective saturation, α (L^{-1}) and n are empirical parameters, $m = 1 - 1/n$, θ_s is the saturated water content, and θ_r is the residual water content.

Boundary conditions included a zero-flux boundary for the top and bottom boundaries and a constant-head (10 cm) boundary condition to simulate a fixed water table (WT) on the side opposite the bank face, potentially induced by recharge to the seepage layer through infiltration or upslope ground water flow. Since seepage usually initiates following the wetting up of the bank profile (Fox et al., 2007a), initial pressure head conditions were simulated in the 10-cm profile as near saturation (i.e., $-1/\alpha$) at the bottom and hydrostatic (decreased linearly) with elevation (Fig. 1). Simulations were performed until quasi steady state flow, defined as the time when the cumulative non-zero seepage outflow per unit width of the layer, Q' (cm^2/s), deviated by no more than $10^{-6} cm^2/s$ between time steps. The simulation time step was adjusted to minimize mass balance errors and was typically on the order of 10 s for each simulation.

2.2. Seepage Erosion Uncertainty Analysis

Chu-Agor et al. (2008b) performed seepage flow experiments with repacked soil banks at numerous ρ_b in the laboratory. During the experiments, triplicate samples were extracted from the repacked soil block setup and were analyzed in the laboratory to determine particle size distribution and soil hydraulic properties

Table 2

Monte Carlo analysis scenarios simulating soil layers based on laboratory analysis of water retention parameters for sand and loamy sand.

Soil type	Scenario number	Available data
<i>Sand</i>		
	1	Texture only
	2	%SSC ^a (99.3% sand, 0.7% silt, 0.0% clay)
	3	%SSC + $\rho_b^b = 1300 kg m^{-3}$
	4	%SSC + $\rho_b = 1300 kg m^{-3}$ + measured K_s^c
	5	Baseline: measured soil hydraulic parameters at $\rho_b = 1300 kg m^{-3}$
	6	%SSC + $\rho_b = 1450 kg m^{-3}$
	7	%SSC + $\rho_b = 1450 kg m^{-3}$ + measured K_s
	8	Baseline: measured soil hydraulic parameters at $\rho_b = 1450 kg m^{-3}$
	9	%SSC + $\rho_b = 1600 kg m^{-3}$
	10	%SSC + $\rho_b = 1600 kg m^{-3}$ + measured K_s
	11	Baseline: measured soil hydraulic parameters at $\rho_b = 1600 kg m^{-3}$
<i>Loamy sand</i>		
	12	Texture only
	13	%SSC (84.5% sand, 13.4% silt, 2.1% clay)
	14	%SSC + $\rho_b = 1500 kg m^{-3}$
	15	%SSC + $\rho_b = 1500 kg m^{-3}$ + measured K_s
	16	Baseline: measured soil hydraulic parameters at $\rho_b = 1500 kg m^{-3}$
	17	%SSC + $\rho_b = 1600 kg m^{-3}$
	18	%SSC + $\rho_b = 1600 kg m^{-3}$ + measured K_s
	19	Baseline: measured soil hydraulic parameters at $\rho_b = 1600 kg m^{-3}$
	20	%SSC + $\rho_b = 1700 kg m^{-3}$
	21	%SSC + $\rho_b = 1700 kg m^{-3}$ + measured K_s
	22	Baseline: measured soil hydraulic parameters at $\rho_b = 1700 kg m^{-3}$

^a %SSC = Percent sand, silt, and clay.

^b ρ_b = Bulk density.

^c K_s = Saturated hydraulic conductivity.

Table 1

Soil hydraulic parameters estimated using RETC from pressure plate experiments for the sand and loamy sand soils at various bulk densities. Values reported are the average of triplicate replications. Data originally reported by Chu-Agor et al. (2008b).

Soil type	Bulk density, ρ_b ($kg m^{-3}$)	Soil hydraulic parameters ^a					
		θ_r ($cm^3 cm^{-3}$)	θ_s ($cm^3 cm^{-3}$)	α (cm^{-1})	n	R^2 for water retention curve fit	K_s ($cm s^{-1}$)
<i>Sand</i> ^b							
	1300	0.06	0.51	0.048	1.22	0.92	0.028
	1450	0.05	0.46	0.026	1.28	0.96	0.017
	1600	0.05	0.40	0.031	1.33	0.94	0.008
<i>Loamy sand</i> ^b							
	1500	0.04	0.43	0.017	1.27	0.90	0.003
	1600	0.04	0.40	0.026	1.23	0.94	0.001
	1700	0.06	0.36	0.019	1.33	0.96	0.001

^a θ_r , θ_s = Residual and saturated water content; α , n = van Genuchten (1980) parameters; K_s = saturated hydraulic conductivity.

^b Sand: 99.3% sand, 0.7% silt, 0.0% clay; Loamy Sand: 84.5% sand, 13.4% silt, and 2.1% clay.

Table 3
Recommended statistical distributions and associated parameters (Meyer et al., 1997) for soil hydraulic parameters relative to soil type.

Soil type	Soil hydraulic parameter ^a	Distribution type	Distribution parameters ^b
Sand	θ_r	Lognormal	$\gamma, \zeta, A = \exp(\gamma - 3.09\zeta),$ $B = \exp(\gamma + 3.09\zeta)$
	θ_s	Normal	$\mu, \sigma, A = \mu - 3.09\sigma,$ $B = \mu + 3.09\sigma$
	α	Normal	$\mu, \sigma, A = \mu - 3.09\sigma,$ $B = \mu + 3.09\sigma$
	n	Lognormal	$\gamma, \zeta, A = \exp(\gamma - 3.09\zeta),$ $B = \exp(\gamma + 3.09\zeta)$
	K_s	Beta	q, r, A, B
Loamy sand	θ_r	Normal	$\mu, \sigma, A = \mu - 3.09\sigma,$ $B = \mu + 3.09\sigma$
	θ_s	Normal	$\mu, \sigma, A = \mu - 3.09\sigma,$ $B = \mu + 3.09\sigma$
	α	Lognormal	$\gamma, \zeta, A = \exp(\gamma - 3.09\zeta),$ $B = \exp(\gamma + 3.09\zeta)$
	n	Lognormal	$\gamma, \zeta, A = \exp(\gamma - 3.09\zeta),$ $B = \exp(\gamma + 3.09\zeta)$
	K_s	Beta	q, r, A, B

^a θ_r, θ_s = Residual and saturated water content; α, n = van Genuchten (1980) parameters; K_s = saturated hydraulic conductivity.

^b μ, σ = Average and standard deviation of the normal distribution; γ, ζ = parameters of the lognormal distribution; q, r = parameters controlling the shape of the beta distribution; A, B = lower and upper limits of the distributions.

(K_s and the soil water retention curve parameters) relative to ρ_b (Table 1).

Particle size analysis was determined by sieve analysis for particles larger than 0.075 mm and the hydrometer method for particles less than 0.075 mm (ASTM Standards D422-63). The K_s was determined on extracted soil cores with ρ_b of 1300, 1450, and 1600 kg m⁻³ for the sand and 1500, 1600, and 1700 kg m⁻³ for the loamy sand using a falling head permeameter (McWhorter and Sunada, 1977). Water retention was determined on the extracted soil cores using standard test methods (ASTM Standards D3152 and D2325). Water retention data were modeled with Retention Curve (RET) with the van Genuchten equation using the Mualem assumption (van Genuchten et al., 1991). A summary of the data for each soil type and ρ_b combination is outlined in Table 1, including the R^2 between the measured and fit $\theta(h)$ using RET (van Genuchten et al., 1991). As expected, a decrease in K_s and θ_s was observed with increased ρ_b (Table 1). Note also that n appeared lower than typical values reported in the literature for these soil types.

Table 4
ROSETTA soil hydraulic parameter and uncertainty estimates (in parentheses) for the sand and loamy sand soils.

Soil type	Type of input data	Soil hydraulic parameters ^a				
		θ_r (cm ³ cm ⁻³)	θ_s (cm ³ cm ⁻³)	$\log_{10}(\alpha) \log_{10}(\text{cm}^{-1})$	$\log_{10}(n)$	$\log_{10}(K_s) \log_{10}(\text{cm/d})$
Sand	Texture only	0.05 (0.03)	0.38 (0.06)	-1.453 (0.254)	0.50 (0.18)	2.81 (0.59)
	%SSC ^b	0.05 (0.01)	0.38 (0.01)	-1.457 (0.066)	0.63 (0.03)	3.12 (0.10)
	%SSC, $\rho_b^c = 1300 \text{ kg m}^{-3}$	0.05 (0.01)	0.45 (0.01)	-1.446 (0.086)	0.59 (0.04)	3.17 (0.13)
	%SSC, $\rho_b = 1450 \text{ kg m}^{-3}$	0.05 (0.01)	0.40 (0.01)	-1.505 (0.075)	0.65 (0.04)	3.18 (0.11)
	%SSC, $\rho_b = 1600 \text{ kg m}^{-3}$	0.05 (0.01)	0.35 (0.01)	-1.511 (0.086)	0.64 (0.03)	3.10 (0.12)
Loamy sand	Texture only	0.05 (0.04)	0.39 (0.07)	-1.500 (0.470)	0.24 (0.16)	2.00(0.64)
	%SSC ^a	0.04 (0.01)	0.39 (0.01)	-1.356 (0.063)	0.31(0.02)	2.23 (0.11)
	%SSC, $\rho_b = 1500 \text{ kg m}^{-3}$	0.04 (0.01)	0.38 (0.01)	-1.376 (0.067)	0.33 (0.02)	2.33 (0.12)
	%SSC, $\rho_b = 1600 \text{ kg m}^{-3}$	0.04 (0.01)	0.35 (0.01)	-1.366 (0.068)	0.33 (0.02)	2.21 (0.11)
	%SSC, $\rho_b = 1700 \text{ kg m}^{-3}$	0.04 (0.01)	0.33 (0.01)	-1.345 (0.085)	0.32 (0.03)	2.05 (0.11)

^a θ_r, θ_s = Residual and saturated water content; α, n = van Genuchten (1980) parameters; K_s = saturated hydraulic conductivity.

^b %SSC = Percent sand, silt, and clay: Sand: 99.3% sand, 0.7% silt, 0.0% clay; Loamy Sand: 84.5% sand, 13.4% silt, and 2.1% clay.

^c ρ_b = Bulk density.

In order to simulate the availability of several different soil data sets (i.e., texture only, %SSC, ρ_b , and K_s), several scenarios were simulated (Table 2). The hierarchy of soil data input included the following: (1) texture only such as the information gathered easily from a soil survey; (2) %SSC to simulate a simple laboratory test on a disturbed sample; (3) %SSC and ρ_b to simulate more intense laboratory tests on both disturbed and undisturbed samples; (4) %SSC, ρ_b , and K_s to simulate a greater level of soil characterization on both disturbed and undisturbed samples; and (5) quantification of all soil hydraulic parameters ($\theta_r, \theta_s, \alpha, n$, and K_s). Three ρ_b were simulated for both the sand and loamy sand leading to a total of 11 scenarios per soil type (Table 2).

Monte Carlo Analysis (MCA) was utilized to account for uncertainty in the input parameters (Hill and Tiedeman, 2007), dependent on ROSETTA input, on seepage gradient predictions. The average and uncertainty values provided by ROSETTA were used to generate statistical distributions of each soil hydraulic parameter based on the recommended statistical distributions of Meyer et al. (1997) as shown in Table 3. Distributions included the normal (Eq. (6)), lognormal (Eq. (7)), and beta (Eq. (8)) distributions:

$$f(x') = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{1}{2}\left(\frac{x' - \mu}{\sigma}\right)^2\right] \quad (6)$$

$$f(x') = \frac{1}{\sqrt{2\pi}\zeta x'} \exp\left[-\frac{1}{2}\left(\frac{\ln(x') - \gamma}{\zeta}\right)^2\right] \quad (7)$$

$$f(x') = \frac{1}{\beta(q, r)} \frac{(x' - A)^{q-1} (B - x')^{r-1}}{(B - A)^{q+r-1}} \quad (8)$$

where x' is the soil parameter, $f(x')$ is the probability density function, μ is the mean, σ is the variance, γ and ζ are parameters of the lognormal distribution (Eq. (7)), q and r are parameters of the beta distribution (Eq. (8)), and A and B are the lower and upper limits of the beta distribution. Lower and upper limits (A and B) for the normal and lognormal distributions were assumed to be the 0.001 and 0.999 quantiles following Meyer et al. (1997) and calculated as $\mu \pm 3.09\sigma$ for the normal distribution and $\exp(\gamma \pm 3.09\zeta)$ for the lognormal distribution.

These distributions were used to generate input data for seepage layer simulations. The MCA generated distributions of steady-state \dot{Q} and maximum seepage velocity, v_{max} , in the simulation domain for each scenario. The v_{max} was converted into a steady-state maximum gradient, i_{max} , in the simulation domain:

$$i_{max} = \frac{v_{max}\phi}{K_s} \quad (9)$$

Table 5
Derived statistical distributions for the sand scenarios using the recommended distributions of Meyer et al. (1997) and ROSETTA-estimated parameters and uncertainty.

Scenario	Soil hydraulic parameters ^a				
	θ_r (cm ³ cm ⁻³)	θ_s (cm ³ cm ⁻³)	α (cm ⁻¹)	n	K_s (cm/s)
Texture only	$\gamma = -3.07$ $\zeta = 0.51$ A = 0.01 B = 0.23	$\mu = 0.38$ $\sigma = 0.06$ A = 0.21 B = 0.55	$\mu = 0.035$ $\sigma = 0.017$ A = 0.001 B = 0.088	$\gamma = 1.16$ $\zeta = 0.41$ A = 1.10 B = 11.43	$q = 0.433$ $r = 2.738$ A = 0.001 B = 0.110
%SSC ^b (99.3% sand, 0.7% silt, 0.0% clay)	$\gamma = -3.00$ $\zeta = 0.11$ A = 0.04 B = 0.07	$\mu = 0.38$ $\sigma = 0.01$ A = 0.35 B = 0.41	$\mu = 0.035$ $\sigma = 0.005$ A = 0.020 B = 0.050	$\gamma = 1.46$ $\zeta = 0.07$ A = 3.44 B = 5.36	$q = 6.151$ $r = 8.254$ A = 0.007 B = 0.026
%SSC + $\rho_b^c = 1300$ kg m ⁻³	$\gamma = -2.93$ $\zeta = 0.14$ A = 0.03 B = 0.08	$\mu = 0.45$ $\sigma = 0.01$ A = 0.41 B = 0.49	$\mu = 0.036$ $\sigma = 0.007$ A = 0.014 B = 0.058	$\gamma = 1.36$ $\zeta = 0.10$ A = 2.90 B = 5.21	$q = 3.149$ $r = 6.162$ A = 0.006 B = 0.0400
%SSC + $\rho_b = 1300$ kg m ⁻³ + measured K_s	“	“	“	“	0.028
Baseline: measured soil hydraulic parameters	0.06	0.51	0.048	1.22	0.028
%SSC + $\rho_b = 1450$ kg m ⁻³	$\gamma = -2.92$ $\zeta = 0.14$ A = 0.04 B = 0.08	$\mu = 0.40$ $\sigma = 0.01$ A = 0.37 B = 0.43	$\mu = 0.031$ $\sigma = 0.005$ A = 0.015 B = 0.048	$\gamma = 1.51$ $\zeta = 0.09$ A = 3.39 B = 6.00	$q = 3.299$ $r = 3.807$ A = 0.007 B = 0.030
%SSC + $\rho_b = 1450$ kg m ⁻³ + measured K_s	“	“	“	“	0.018
Baseline: measured soil hydraulic parameters	0.05	0.46	0.026	1.28	0.018
%SSC + $\rho_b = 1600$ kg m ⁻³	$\gamma = -2.97$ $\zeta = 0.14$ A = 0.03 B = 0.08	$\mu = 0.35$ $\sigma = 0.01$ A = 0.33 B = 0.38	$\mu = 0.031$ $\sigma = 0.006$ A = 0.012 B = 0.050	$\gamma = 1.48$ $\zeta = 0.07$ A = 3.54 B = 5.47	$q = 3.020$ $r = 4.426$ A = 0.006 B = 0.028
%SSC + $\rho_b = 1600$ kg m ⁻³ + measured K_s	“	“	“	“	0.008
Baseline: measured soil hydraulic parameters	0.05	0.40	0.031	1.33	0.008

^a θ_r , θ_s = Residual and saturated water content; α , n = van Genuchten (1980) parameters; K_s = saturated hydraulic conductivity.

^b %SSC = Percent sand, silt, and clay.

^c ρ_b = Bulk density.

Table 6
Derived statistical distributions for the loamy sand scenarios using the recommended distributions of Meyer et al. (1997) and ROSETTA-estimated parameters and uncertainty.

Scenario	Soil hydraulic parameters ^a				
	θ_r (cm ³ cm ⁻³)	θ_s (cm ³ cm ⁻³)	α (cm ⁻¹)	n	K_s (cm/s)
Texture only	$\mu = 0.05$ $\sigma = 0.04$ A = 0.00 B = 0.18	$\mu = 0.39$ $\sigma = 0.07$ A = 0.17 B = 0.61	$\gamma = -3.454$ $\zeta = 1.082$ A = 0.001 B = 0.896	$\gamma = 0.55$ $\zeta = 0.37$ A = 1.50 B = 5.42	$q = 0.572$ $r = 8.904$ A = 0.000 B = 0.037
%SSC ^b (84.5% sand, 13.4% silt, 2.1% clay)	$\mu = 0.04$ $\sigma = 0.01$ A = 0.02 B = 0.05	$\mu = 0.39$ $\sigma = 0.01$ A = 0.36 B = 0.41	$\gamma = -3.130$ $\zeta = 0.141$ A = 0.028 B = 0.068	$\gamma = 0.72$ $\zeta = 0.04$ A = 1.82 B = 2.30	$q = 3.412$ $r = 3.909$ A = 0.001 B = 0.004
%SSC + $\rho_b^c = 1500$ kg m ⁻³	$\mu = 0.04$ $\sigma = 0.01$ A = 0.02 B = 0.06	$\mu = 0.38$ $\sigma = 0.01$ A = 0.36 B = 0.40	$\gamma = -3.168$ $\zeta = 0.154$ A = 0.026 B = 0.068	$\gamma = 0.76$ $\zeta = 0.05$ A = 1.84 B = 2.50	$q = 3.382$ $r = 3.893$ A = 0.001 B = 0.005
%SSC + $\rho_b = 1500$ kg m ⁻³ + measured K_s	“	“	“	“	0.003
Baseline: measured soil hydraulic parameters	0.04	0.43	0.017	1.27	0.003
%SSC + $\rho_b = 1600$ kg m ⁻³	$\mu = 0.04$ $\sigma = 0.01$ A = 0.02 B = 0.06	$\mu = 0.35$ $\sigma = 0.01$ A = 0.33 B = 0.37	$\gamma = -3.145$ $\zeta = 0.157$ A = 0.027 B = 0.070	$\gamma = 0.76$ $\zeta = 0.05$ A = 1.86 B = 2.47	$q = 2.549$ $r = 4.546$ A = 0.001 B = 0.004
%SSC + $\rho_b = 1600$ kg m ⁻³ + measured K_s	“	“	“	“	0.001
Baseline: measured soil hydraulic parameters	0.04	0.40	0.026	1.23	0.001
%SSC + $\rho_b = 1700$ kg m ⁻³	$\mu = 0.03$ $\sigma = 0.01$ A = 0.02 B = 0.06	$\mu = 0.33$ $\sigma = 0.01$ A = 0.30 B = 0.35	$\gamma = -3.096$ $\zeta = 0.195$ A = 0.025 B = 0.083	$\gamma = 0.73$ $\zeta = 0.06$ A = 1.74 B = 2.47	$q = 3.036$ $r = 6.201$ A = 0.001 B = 0.003
%SSC + $\rho_b = 1700$ kg m ⁻³ + measured K_s	“	“	“	“	0.001
Baseline: measured soil hydraulic parameters	0.06	0.36	0.019	1.33	0.001

^a θ_r , θ_s = Residual and saturated water content; α , n = van Genuchten (1980) parameters; K_s = saturated hydraulic conductivity.

^b %SSC = Percent sand, silt, and clay.

^c ρ_b = Bulk density.

Based on Eq. (1), the deviation in predicted i_{max} is proportional to the deviation in predicted seepage force. Also, assuming $a = 1.0$ in Eq. (2), the deviation in predicted seepage erosion rate (i.e., E_{rs}/k_{se}) is proportional to the deviation in i_{max} . The baseline i_{max} for calculating deviations was simulated using the exact data for all soil hydraulic parameters measured by Chu-Agor et al. (2008b), as shown in Table 1. The deviation of the predicted i_{max} from the baseline i_{max} was calculated, and cumulative distribution functions (CDFs) of the deviations in i_{max} were derived for each scenario.

3. Results and discussion

Using the laboratory measured soil properties at the three different ρ_b as baseline conditions allowed an evaluation of the deviations for six different soil conditions. Soil hydraulic parameters derived using ROSETTA and uncertainty estimates for the sand and loamy sand soils are shown in Table 4. Considerable reduction

occurred in the variability of ROSETTA-derived soil hydraulic parameters when including %SSC as opposed to only texture. Specification of the ρ_b tended to keep the uncertainty in ROSETTA-derived parameters the same or slightly increased the uncertainty compared to only using %SSC. These findings were most likely due to the availability of data points within the neural network training set for these soils at this selected ρ_b . Unlike ROSETTA, some PTFs which account for ρ_b include both texture and organic matter content (Kaur et al., 2002; Nemes et al., 2005), and future research that tests these other pedotransfer functions would be valuable. Similar to the laboratory measured parameters (Table 1), θ_s and K_s decreased with increased ρ_b , but the change in α was inconsistent with increased ρ_b . Also, n values were consistently larger than those reported by Chu-Agor et al. (2008b). Parameters of the statistical distributions are given in Tables 5 and 6 for the sand and loamy sand soils, respectively.

The conversion between Q' , v_{max} , and i_{max} is shown in Fig. 2 for scenario 2 in Table 2 (i.e., sand soil with ROSETTA-derived soil

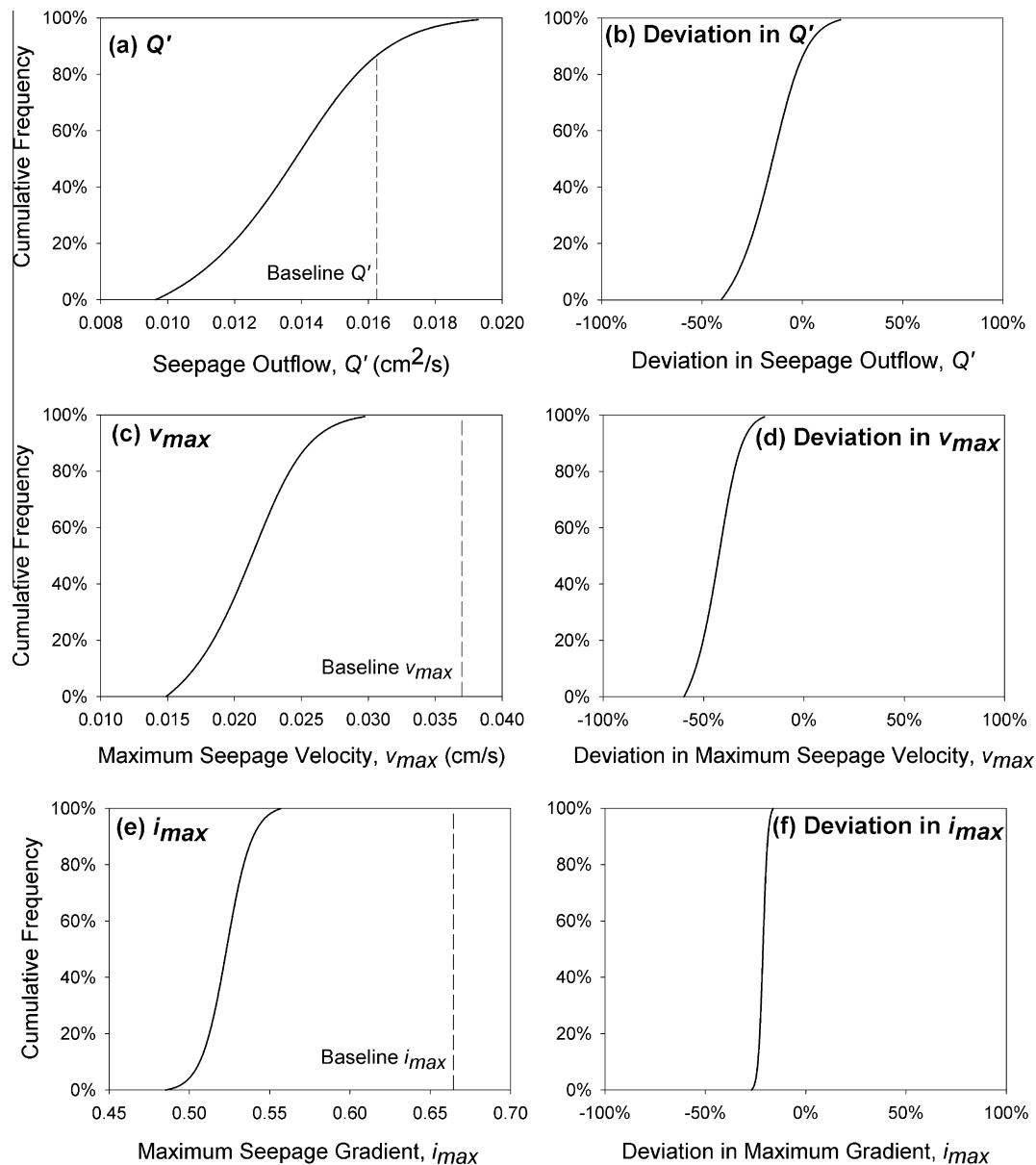


Fig. 2. Cumulative distribution curves for: (a) seepage outflow (Q'), (b) deviation in Q' from baseline, (c) maximum seepage velocity (v_{max}), (d) deviation in v_{max} from baseline, (e) maximum seepage gradient (i_{max}), and (f) deviation in i_{max} from baseline for the sand soil at bulk density of 1300 kg m^{-3} with ROSETTA-derived input parameters based on input percent sand, silt, and clay (%SSC).

hydraulic parameters based on %SSC at $\rho_b = 1300 \text{ kg m}^{-3}$). The baseline Q fell in the upper range of the statistical distribution because K_s was larger for the baseline than the %SSC- K_s distribution (Fig. 2a and b). Also, differences between the baseline and average %SSC ROSETTA-derived soil hydraulic parameters (most notably in the n value) also resulted in a smaller perched water table depth at the outflow boundary for the baseline condition (Fig. 3). Therefore, the smaller perched water table depth at the outflow face resulted in a larger baseline v_{max} as compared to the average of the %SSC distribution, resulting in the %SSC v_{max} distribution falling below the baseline v_{max} (Fig. 2c and d). As expected, the position of the baseline i_{max} relative to the %SSC i_{max} distribution was similar (Fig. 2e and f). Deviation curves for i_{max} were much more confined than Q and v_{max} due to the conversion based on Eq. (9) using the most variable soil hydraulic parameter, K_s . An advantage of the dependence of the erosion rate on the ground water flow gradient was the variability due to K_s being removed from the analysis as compared to Q or v_{max} .

Knowledge of texture alone resulted in large deviations in predicted i_{max} across all simulated soil textures (Figs. 4 and 5). The 95% CI tended to shift towards more positive deviations (i.e., overestimation) as ρ_b increased. For example, for the sand, the 95% CI were -46% to -7% , -40% to 3% , and -30% to 18% for $\rho_b = 1300, 1450,$ and 1600 kg m^{-3} , respectively (Fig. 4). As expected, using measured %SSC as input into ROSETTA reduced the deviation from the texture alone scenario for all six soil conditions, as shown in

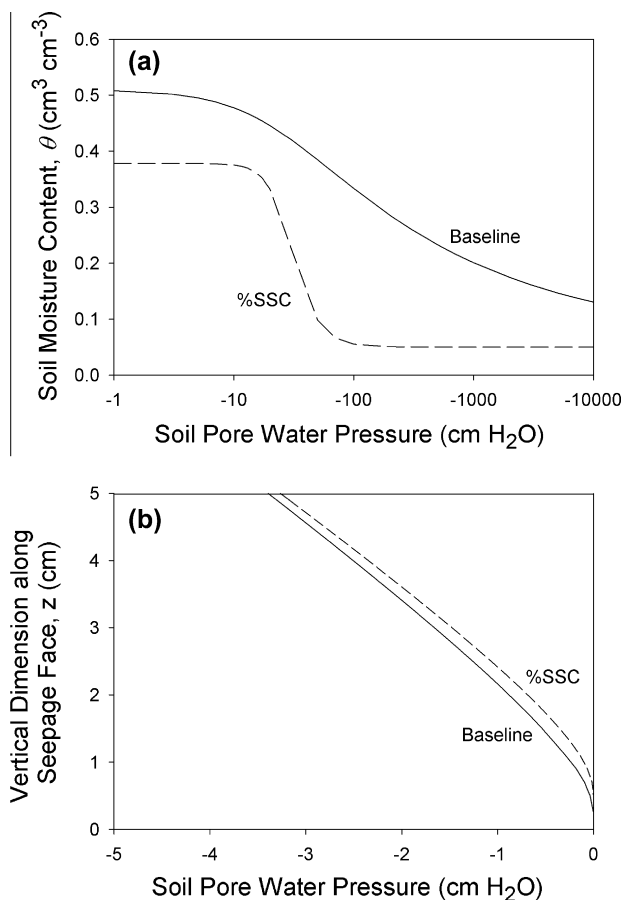


Fig. 3. (a) Water retention curves for the sand soil at bulk density of 1300 kg m^{-3} for the baseline condition based on laboratory measured soil hydraulic properties ($\theta_r = 0.06$, $\theta_s = 0.51$, and $\alpha = 0.048 \text{ cm}^{-1}$, and $n = 1.3$) and the ROSETTA-estimated soil hydraulic parameters based on input percent sand, silt, and clay, %SSC ($\theta_r = 0.05$, $\theta_s = 0.38$, and $\alpha = 0.035 \text{ cm}^{-1}$, and $n = 4.3$). (b) Water pressure head versus elevation along the seepage face of the modeling boundary for the two different scenarios: baseline ($K_s = 0.0284 \text{ cm/s}$) and ROSETTA with %SSC ($K_s = 0.0204 \text{ cm/s}$).

Figs. 4 and 5. The 95% CI were more confined due to the decrease in variability in ROSETTA-derived soil hydraulic parameters. The 95% CI for the sand at $\rho_b = 1300, 1450,$ and 1600 kg m^{-3} were -24% to -18% , -16% to -9% , and -4% to 5% , respectively. The 95% CI for loamy sand at $\rho_b = 1500, 1600,$ and 1700 kg m^{-3} were -6% to 2% , -5% to 3% , and -9% to 2% , respectively. The 95% CI suggest that for ρ_b at the center of sand or loamy sand soils' expected ρ_b range, the use of %SSC alone was a reasonable procedure for deriving soil hydraulic parameters with deviations from the baseline in i_{max} on the order of 20% or less. Therefore, knowing %SSC reduced the deviation across both soil types. This finding suggests that at a minimum, soil samples should be taken for particle size analysis. The deviation incurred by not measuring the %SSC directly is dependent upon the soil texture and ρ_b .

For ρ_b in the range of $1450\text{--}1500 \text{ kg m}^{-3}$, deviations in predicted i_{max} when using only %SSC were approximately equivalent to deviations in i_{max} for scenarios using ρ_b and/or K_s (Figs. 4b and 5a). When the ρ_b for the soil was less than the $1450\text{--}1500 \text{ kg m}^{-3}$ range, inputting ρ_b and/or K_s typically reduced the magnitude of deviations in i_{max} (Fig. 4a). For ρ_b greater than $1450\text{--}1500 \text{ kg m}^{-3}$, inputting ρ_b and/or K_s resulted in larger magnitude deviations in i_{max} (Figs. 4c, 5b and c), with the magnitude of the deviations increasing as ρ_b increased.

Note that considerable deviations in i_{max} were calculated even with measurements of ρ_b and K_s due to significant deviations in ROSETTA-derived versus laboratory-measured values of other soil hydraulic parameters (compare Table 1 to Tables 5 and 6). More specifically, the n parameter of the van Genuchten (1980) curve possessed the greatest discrepancy between ROSETTA ($n = 3.2\text{--}4.5$ for sand, Table 5, and $n = 1.7\text{--}2.1$ for loamy sand, Table 6) and the laboratory measurements ($n = 1.2\text{--}1.3$ for both sand and loamy sand, Tables 5 and 6). These results emphasized properly quantifying all the soil hydraulic parameters for modeling seepage through high ρ_b soils, even if only considering steady-state seepage. Without these discrepancies in the soil hydraulic parameters other than hydraulic conductivity, deviations in seepage gradients were less than 5%.

4. Summary and conclusions

Recent research has focused on seepage gradient forces and particle mobilization and undercutting as important bank instability mechanisms. This research investigated uncertainty in soil hydraulic parameters relative to modeling seepage gradients, a necessary variable for predicting seepage gradient forces and erosion rates. This research was applicable to seepage from homogeneous, isotropic layers of sand and loamy sand that mimicked in situ observations of streambanks. Therefore, conclusions were specific to seeps that did not involve preferential flow through biological or structural channels. Future research should consider the impact of heterogeneity and anisotropy on seepage gradient predictions, a wider range of soil types and seepage layer dimensions, and the role of preferential flow.

The advantage of the dependence of the seepage gradient force and the erosion rate on the ground water flow gradient is that some variability with respect to hydraulic conductivity is removed from the analysis as compared to seepage outflow or maximum seepage velocity, both of which depend explicitly on saturated hydraulic conductivity. Monte Carlo analyses with the various input scenarios demonstrated that knowledge of soil texture alone to derive soil hydraulic parameters for seepage gradient prediction was insufficient. Inputting percent sand, silt, and clay consistently reduced variability in soil hydraulic parameters and corresponding deviations in predicted seepage gradients from the baseline conditions. While knowledge of bulk density did not consistently reduce

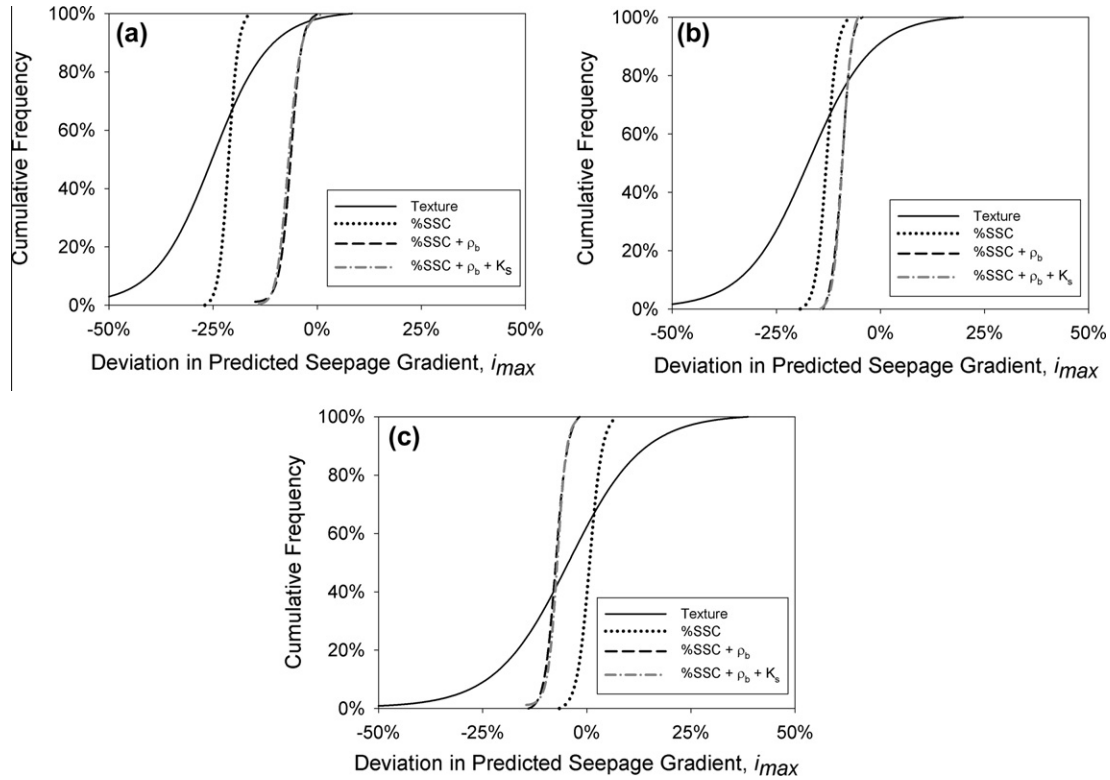


Fig. 4. Cumulative distribution curves of deviations in predicted seepage gradient (i_{max}) derived from Monte Carlo analysis for the sand soil at three different bulk densities (ρ_b): (a) 1300 kg/m³, (b) 1450 kg/m³, and (c) 1600 kg/m³. Various levels of information have been used to derive soil hydraulic properties for each curve: texture only; percent sand, silt and clay (%SSC); %SSC and ρ_b ; and %SSC, ρ_b , and saturated hydraulic conductivity (K_s).

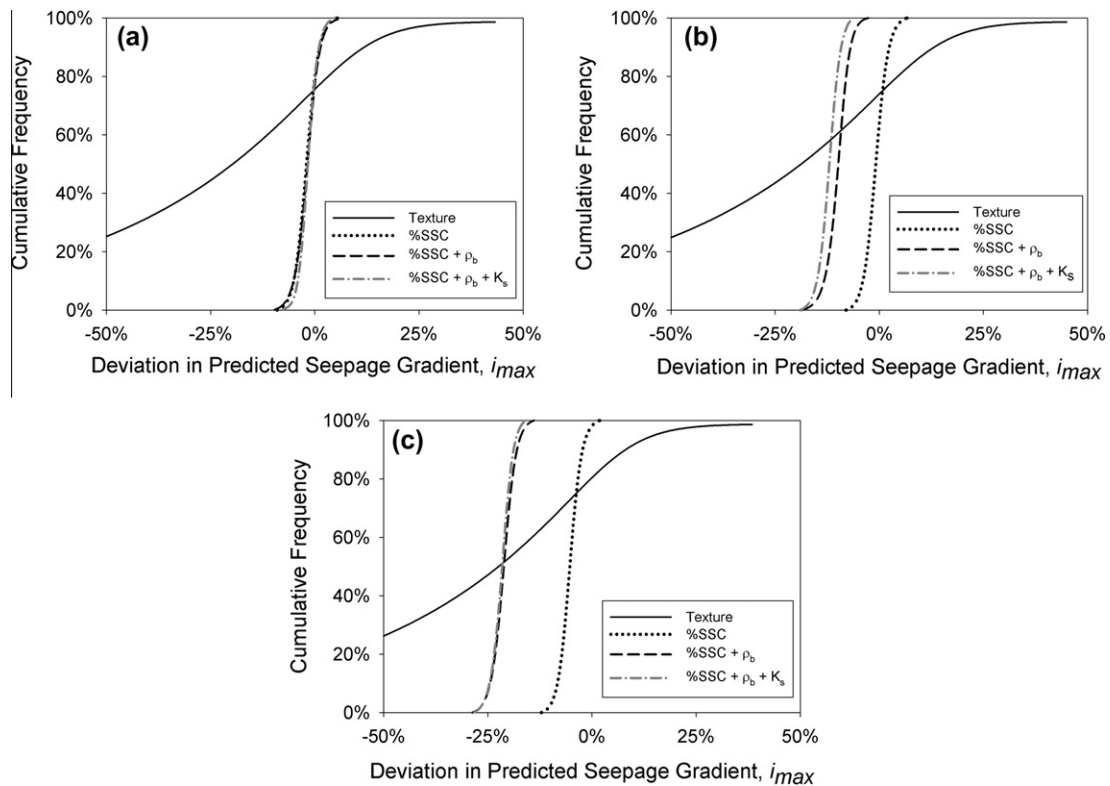


Fig. 5. Cumulative distribution curves of deviations in predicted seepage gradient (i_{max}) derived from Monte Carlo analysis for the loamy sand soil at three different bulk densities (ρ_b): (a) 1500 kg/m³, (b) 1600 kg/m³, and (c) 1700 kg/m³. Various levels of information have been used to derive soil hydraulic properties for each curve: textural class only; percent sand, silt and clay (%SSC); %SSC and ρ_b ; and %SSC, ρ_b , and saturated hydraulic conductivity (K_s).

deviation in all scenarios, this soil parameter played a vital role in the potential range in deviations in seepage gradient predictions. For bulk densities between 1450 and 1500 kg m⁻³, deviations in predicted seepage gradients when using only percent sand, silt, and clay were approximately equivalent to deviations with bulk density and/or saturated hydraulic conductivity being known. When the bulk density for the soil was less than 1450–1500 kg m⁻³, inputting bulk density and/or saturated hydraulic conductivity consistently decreased the magnitude of deviations in seepage gradients. However, when the bulk density for the soil was greater than 1450–1500 kg m⁻³, inputting bulk density and/or saturated hydraulic conductivity consistently increased the magnitude of deviations when discrepancies existed between the estimated and actual values of soil hydraulic parameters other than saturated hydraulic conductivity. More specifically, considerable deviations in seepage gradients (i.e., on the order of 20%) can exist even with measurements of bulk density and/or saturated hydraulic conductivity when significant discrepancies exist between ROSETTA-derived versus actual values of other soil hydraulic parameters. Without these discrepancies in soil hydraulic parameters other than hydraulic conductivity, deviations in seepage gradients were generally less than 5%. Therefore, for soil layers with bulk densities on the upper limits of the expected bulk density range, it is vital to have a complete quantification of the soil hydraulic parameters for accurately predicting seepage gradients.

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