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# Search for a Fourth Generation $t$ Quark in $p\bar{p}$ Collisions at $\sqrt{s}= 1.96$ TeV

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We present a search for pair production of a fourth generation  $t'$  quark and its antiparticle, followed by their decays to a  $W$  boson and a jet, based on an integrated luminosity of  $5.3 \text{ fb}^{-1}$  of proton-antiproton collisions at  $\sqrt{s} = 1.96 \text{ TeV}$  collected by the D0 Collaboration at the Fermilab Tevatron Collider. We set upper limits on the  $t'\bar{t}'$  production cross section that exclude at the 95% C.L. a  $t'$  quark that decays exclusively to  $W + \text{jet}$  with a mass below 285 GeV. We observe a small excess in the  $\mu + \text{jets}$  channel which reduces the mass range excluded compared to the expected limit of 320 GeV in the absence of a signal.

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Measurements of the partial width of the  $Z$  boson to invisible final states at LEP exclude the existence of a fourth neutrino flavor with a mass less than half the  $Z$  boson mass [1]. However, this does not exclude the existence of a fourth generation of fermions as long as its neutrino is more massive. Precision electroweak data favor a small mass splitting between the up-type quark of this fourth generation,  $t'$ , and its down-type partner,  $b'$ , so that  $m(t') - m(b') < m(W)$  [2]. Provided there is moderate mixing between the new fourth generation and the first three generations, the  $t'$  quark will predominantly decay to  $Wq$ , where  $q$  includes all standard model down-type quarks.

We report on a search for a fourth generation  $t'$  quark that is produced in proton-antiproton collisions together with its antiparticle. We assume that the  $t'$  quark is a narrow state that always decays to  $Wq$ . This search is

also sensitive to other new particles that are pair produced and decay to a  $W$  boson plus a jet. We select lepton + jets final states with one isolated electron or muon with high transverse momentum ( $p_T$ ), a large imbalance in transverse momentum ( $\cancel{p}_T$ ), and at least four jets corresponding to events in which one of the  $W$  bosons decays to leptons and the other  $W$  boson decays to quarks. A similar search has been carried out by the CDF Collaboration in  $0.76 \text{ fb}^{-1}$  of integrated luminosity and excluded  $t'$  quarks of mass below 256 GeV [3].

The D0 detector consists of central tracking, calorimeter, and muon systems [4,5]. The central tracking system is located inside a 2 T superconducting solenoidal magnet. Central and forward preshower detectors are located just outside of the coil and in front of the calorimeters. The liquid-argon-uranium calorimeter is divided into a central section covering pseudorapidity  $|\eta| < 1.1$  and two end

calorimeters extending  $\eta$  coverage to 4.2. The calorimeter is segmented longitudinally into electromagnetic, fine hadronic, and coarse hadronic sections with increasingly coarser sampling. The muon system, located outside the calorimeter, consists of one layer of tracking detectors and scintillation trigger counters inside 1.8 T toroidal magnets and two similar layers outside the toroids. A three-level trigger system selects events that are recorded for off-line analysis.

This analysis is based on data corresponding to an integrated luminosity of  $5.3 \text{ fb}^{-1}$ , collected by the D0 Collaboration at the Fermilab Tevatron proton-antiproton collider at a center of mass energy of  $\sqrt{s} = 1.96 \text{ TeV}$ . Events must satisfy one of several trigger conditions, all requiring an electron or muon with high transverse momentum, in some cases in conjunction with one or more jets. For all events, the  $p\bar{p}$  collision point must be reconstructed with at least three tracks and located within 60 cm of the center of the detector along the beam direction. Jets are reconstructed using a midpoint cone algorithm [6] with cone size  $\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = 0.5$ , where  $\phi$  is the azimuth, and must have at least two reconstructed tracks within the jet cone. The jet energy is corrected on average to the total energy of all particles emitted inside the jet cone. Jets in simulated events are adjusted to reproduce the reconstruction efficiency and energy resolution and response observed in data. All events must have at least four jets with  $|\eta| < 2.5$ ,  $p_T > 40 \text{ GeV}$  for the leading jet, and  $p_T > 20 \text{ GeV}$  for all other jets. The momentum carried away by neutrinos is inferred from the  $\cancel{p}_T$ , computed from the energies in the cells of the electromagnetic and fine hadronic calorimeters and adjusted for the energy corrections applied to the reconstructed jets and electrons and for the momentum of any reconstructed muons, taking into account their energy loss in the calorimeter.

Electrons are identified as clusters of energy depositions in the calorimeter that are isolated from other energy deposits. The electromagnetic section of the calorimeter must contain 90% of their energy, and the energy deposition pattern must be consistent with that of an electromagnetic shower. Every electron must be matched to a reconstructed track with  $p_T > 5 \text{ GeV}$ . For the  $e + \text{jets}$  channel, we require exactly one electron with  $p_T > 20 \text{ GeV}$  and  $|\eta| < 1.1$  that originates from the  $p\bar{p}$  collision point. We also require  $\cancel{p}_T > 20 \text{ GeV}$  and  $|\Delta\phi(e, \cancel{p}_T)| > 2.2 - 0.045 \times \cancel{p}_T/\text{GeV}$ , where  $\Delta\phi(e, \cancel{p}_T)$  is the azimuthal angle between electron and  $\cancel{p}_T$ , to reject events with jets that are misidentified as electrons.

Muons are defined as tracks reconstructed in the muon system matched to tracks in the central tracker. Muons must be separated from jets and isolated in the calorimeter and in the tracker. For the  $\mu + \text{jets}$  channel, we require exactly one muon with  $p_T > 20 \text{ GeV}$  and  $|\eta| < 2$  that originates from the  $p\bar{p}$  collision point. The invariant mass of the selected muon and any other muon must be

less than 70 GeV or more than 110 GeV to reject  $Z(\rightarrow \mu\mu) + \text{jets}$  events. We require  $\cancel{p}_T > 25 \text{ GeV}$  and  $|\Delta\phi(\mu, \cancel{p}_T)| > 2.1 - 0.035 \times \cancel{p}_T/\text{GeV}$  to reject events with mismeasured muons. More details about the lepton + jets event selection can be found in Ref. [7].

The two main standard model processes that produce events with an isolated lepton,  $\cancel{p}_T$ , and at least four jets are  $t\bar{t}$  and  $W + \text{jets}$  production. The third most important source of events arises from mismeasured multijet events in which a jet is misidentified as an electron or a muon from heavy flavor decay appears isolated. Single top quark,  $Z + \text{jets}$ , and diboson production can also give rise to such final states but have much smaller cross sections and/or acceptances.

We use ALPGEN [8] to simulate  $t\bar{t}$  production with the top quark mass set to 172.5 GeV and generate additional jets from parton showers with PYTHIA [9]. We normalize the  $t\bar{t}$  sample to the theoretical  $t\bar{t}$  production cross section of  $7.48_{-0.72}^{+0.56} \text{ pb}$  [10]. Samples of  $W + \text{jets}$  events are generated using ALPGEN and PYTHIA with a jet-matching algorithm [11]. Three subsamples are generated:  $Wb\bar{b}$ ,  $Wc\bar{c}$ , and  $W + \text{light partons}$ . The  $Wc$  subprocesses are included in the  $W + \text{light parton}$  sample with massless charm quarks. We fix the relative normalization of  $Wb\bar{b}$ ,  $Wc\bar{c}$ , and  $W + \text{light parton}$  events to match next-to-leading order (NLO) cross sections [12]. The  $Z(\rightarrow ee, \mu\mu, \tau\tau) + \text{jets}$  samples are generated with ALPGEN and PYTHIA and broken up into  $Zb\bar{b}$ ,  $Zc\bar{c}$ , and  $Z + \text{light parton}$  samples in the same way as the  $W + \text{jets}$  samples. We fix their relative normalization to NLO predictions and normalize the total  $Z$  boson sample to the NNLO cross section [13]. We simulate single top quark production using the COMPHEP-SINGLETOP [14] Monte Carlo event generator with the top quark mass set to 172.5 GeV and normalize to the NNLO cross section with NNNLO threshold corrections in the  $s$  and  $t$  channels of 3.3 pb [15]. Diboson samples are generated with PYTHIA. Their NLO cross sections are 12.3 pb for  $WW$ , 3.7 pb for  $WZ$ , and 1.4 pb for  $ZZ$  production [12]. The CTEQ6L1 parton distribution functions [16] are used for all Monte Carlo samples. We simulate detector effects using the GEANT [17] program. Events from random collisions are added to all simulated events to account for detector noise and additional  $p\bar{p}$  interactions. The events are reconstructed with the same program as the data.

To define the background model, we proceed as follows. First we estimate the number of multijet events that enter the final data sample. We use a data driven method [18] based on a superset of the final data sample obtained by removing the lepton isolation and  $\cancel{p}_T$  requirements from the selection. At low  $\cancel{p}_T$  this sample is dominated by multijet events and we can determine the ratio of the number of multijet background events with lepton candidates before and after applying the lepton isolation criteria. We determine the same ratio for leptons from simulated  $t\bar{t}$  events. Using these two ratios and the ratio of events

TABLE I. Composition of the final data sample with systematic uncertainties. The number of  $W$  + jets events is chosen to equalize the total number of events observed and expected.

Source	$e$ + jets	$\mu$ + jets
$t\bar{t}$ production	$678 \pm 76$	$508 \pm 55$
Single $t$ production	$12 \pm 4$	$8 \pm 3$
$W$ + jets	$503 \pm 87$	$648 \pm 59$
$Z$ + jets	$41 \pm 7$	$40 \pm 7$
$WW, WZ, ZZ$ + jets	$25 \pm 5$	$21 \pm 5$
Multijets	$173 \pm 42$	$43 \pm 18$
Data	1431	1268

observed with the full selection before and after applying the lepton isolation criteria, we estimate the number of multijet events in the final data sample. We compute the number of multijet events in the  $e$  + jets and  $\mu$  + jets samples separately. We then subtract the number of multijet events and the expected number of events from all other backgrounds, except from  $W$  + jets production, from the number of data events and normalize the  $W$  + jets contribution to the remaining number of events. This corresponds to scaling the total number of  $W$  + jets events expected by a factor 1.3, which is consistent with NLO expectations. Table I summarizes the resulting composition of the data sample. To test for the presence of a  $t'$  quark signal, we fix the relative normalizations of the  $W$  + jets,  $Z$  + jets, single top quark, and diboson backgrounds, as given in Table I, but float their overall normalization.

To simulate the signal, we use  $t'\bar{t}'$  production in PYTHIA and force the decay  $t' \rightarrow Wb$ . However, since we do not identify  $b$  jets in this analysis, our results are also applicable to  $t'$  quarks decaying to a  $W$  boson and a light down-type quark. We generate events at 13  $t'$ -mass values between 200 and 500 GeV. We set the total width of the  $t'$  quark to 10 GeV. This is smaller than the resolution for reconstructing the  $t'$  mass, which ranges between 50 GeV at  $m_{t'} = 200$  GeV and 100 GeV at  $m_{t'} = 500$  GeV. Therefore, the exact value of the width does not affect the analysis.

We define  $H_T$  as the scalar sum of  $\not{p}_T$  and of the transverse momenta of all jets and the charged lepton. A kinematic fit to the  $t'\bar{t}' \rightarrow \ell\nu b q \bar{q}' \bar{b}$  hypothesis reconstructs the mass  $m_{\text{fit}}$  of the  $t'$  quark. We use the two-dimensional histograms of  $H_T$  versus  $m_{\text{fit}}$  to test for the presence of signal in the data and to compute 95% C.L. upper limits on the  $t'\bar{t}'$  production cross section as a function of  $t'$  mass. Figure 1 shows the scatter plots observed in data and expected from  $t'\bar{t}'$  production,  $t\bar{t}$  production, and from all other background sources. For each hypothesized value of the  $t'$  mass, we fit the data to background-only and to signal + background hypotheses. We then use the likelihood ratio  $L = -2 \log(P_{S+B}/P_B)$  as the test statistic, where  $P_{S+B}$  is the Poisson likelihood to observe the data under the signal + background hypothesis and  $P_B$  is the

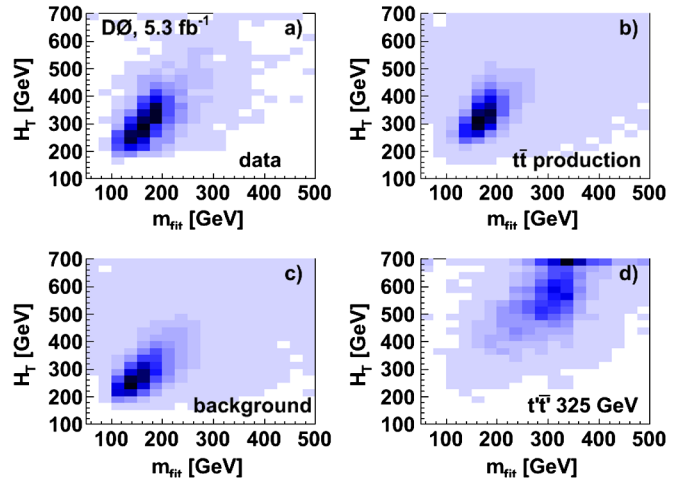


FIG. 1 (color online).  $H_T$  versus  $m_{\text{fit}}$  for (a) data, (b)  $t\bar{t}$  production, (c) other background, and (d)  $t'\bar{t}'$  signal with  $m(t') = 325$  GeV. The bins at the upper and right edges of the plots also contain overflows.

Poisson likelihood to observe the data under the background-only hypothesis. For the background-only hypothesis, we fit three components to the data:  $t\bar{t}$  production constrained to its theoretical cross section, the multijets background constrained to the number of events given in Table I, and  $W$  + jets and all other backgrounds in the proportions given in Table I. We add the  $t'\bar{t}'$  cross section as a parameter to the signal + background fit. The fit can discriminate between background and signal contributions because their distributions in the  $H_T$  and  $m_{\text{fit}}$  variables are different. For each hypothesis we also vary the systematic uncertainties given in Table II subject to a Gaussian constraint to their prior values to maximize the likelihood ratio [19].

We use the  $CL_s$  method [20] to determine the cross section limits. Using pseudoexperiments, we determine the probability to measure values of  $L$  that are larger

TABLE II. Summary of systematic uncertainties above 1%. Some values vary with channel and with the time at which the data were taken. The numbers give the range for the size of the uncertainties.

Source	$t'\bar{t}'$	$t\bar{t}$	Multijets
$t\bar{t}$ cross section	...	9%	...
Multijets normalization	...	...	(25–50)%
Integrated luminosity	6.1%	6.1%	...
Monte Carlo model	...	4.3%	...
Trigger efficiency	$\leq 5\%$	$\leq 5\%$	...
$p\bar{p}$ collision point reconstruction	1.6%	1.6%	...
Lepton identification	(3–4)%	(3–4)%	...
Jet energy calibration	(1–2)%	(2–5)%	...
Jet energy resolution	(1–2)%	(2–3)%	...
Jet identification	1%	(1–3)%	...

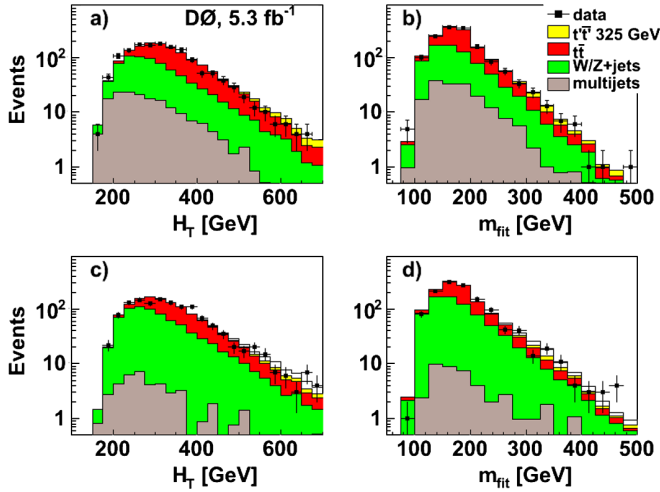


FIG. 2 (color online). Distributions of (a)  $H_T$  and (b)  $m_{\text{fit}}$  for  $e + \text{jets}$  data and (c)  $H_T$  and (d)  $m_{\text{fit}}$  for  $\mu + \text{jets}$  data compared with expectations. The  $W/Z + \text{jets}$  category also includes single top quark and diboson production. The  $t'\bar{t}'$  signal is normalized to the expected yield. The unfilled histograms in (c) and (d) show the distributions with the best fit  $t'\bar{t}'$ -production cross section.

than the value observed in the data sample for a  $t'$  signal,  $CL_{s+b}$ , and for no  $t'$  signal,  $CL_b$ . The value of the  $t'$  pair production cross section for which  $1 - CL_{s+b}/CL_b = 0.95$  is the 95% C.L. upper limit. We repeat this procedure for each  $t'$  mass point.

Table II summarizes the sources of systematic uncertainties included in the limit calculation. The first four uncertainties affect the normalization of the components of our signal and background models. All other uncertainties affect the selection efficiency. When estimating the effect of uncertainties in the jet energy scale, the jet identification efficiency, and the jet energy resolution, we also vary the shapes of the  $H_T$  and  $m_{\text{fit}}$  distributions. No uncertainties are given for the  $W + \text{jets}$  background because its normalization is a free parameter of the fit.

We first analyze the  $e + \text{jets}$  and  $\mu + \text{jets}$  data separately. Figure 2 shows the distributions of  $H_T$  and  $m_{\text{fit}}$  from the standard model backgrounds and a 325 GeV  $t'$  quark

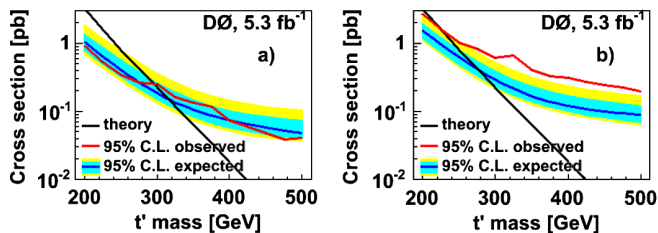


FIG. 3 (color online). Observed and expected upper limits and predicted values for the  $t'\bar{t}'$  production cross section as a function of the mass of the  $t'$  quark for (a)  $e + \text{jets}$ , (b)  $\mu + \text{jets}$ . The shaded regions around the expected limit represent the  $\pm 1$  and  $\pm 2$  standard deviation bands.

signal compared to data. There is no excess in the  $e + \text{jets}$  data. In the  $\mu + \text{jets}$  data we observe a small excess of events over standard model expectations. We can fit the data best with a  $t'\bar{t}'$  production cross section of  $3.2 \pm 1.1$  times the theoretical cross section for a  $t'$  quark mass of 325 GeV. The value of  $1 - CL_b$  for the data gives the probability of getting a local deviation of at least this size from the standard model expectation in the absence of physics beyond the standard model. We find a  $p$  value of 0.007, corresponding to 2.5 Gaussian-equivalent standard deviations.

Figure 3 shows the resulting cross section limits compared to the limits expected in the absence of  $t'\bar{t}'$  production and to the predicted NLO  $t'$  pair production cross section [21] as a function of the  $t'$  mass. We expect to be able to exclude  $t'\bar{t}'$  production for  $t'$  quark masses below 315 GeV in the  $e + \text{jets}$  channel and below 280 GeV in the  $\mu + \text{jets}$  channel. The observed cross section limit allows us to exclude  $t'\bar{t}'$  production for  $t'$  quark masses at the 95% C.L. below 295 GeV in the  $e + \text{jets}$  channel and below 225 GeV in the  $\mu + \text{jets}$  channel. Combining  $e + \text{jets}$  and  $\mu + \text{jets}$  data as shown in Fig. 4, we expect to exclude  $t'\bar{t}'$  production for  $t'$  quark mass values below 320 GeV. Based on the observed limits we can exclude at the 95% C.L.  $t'\bar{t}'$  production for  $t'$  quark masses below 285 GeV. We achieve the best fit to the data with a  $t'\bar{t}'$  production cross section of  $1.1 \pm 0.5$  times the theoretical cross section for a  $t'$  quark mass of 325 GeV which gives a  $p$  value of 0.015, corresponding to 2.2 standard deviations from zero.

In conclusion, we searched for pair production of a  $t'$  quark and its antiparticle followed by their decays into a  $W$  boson and a jet. We do not see a signal consistent with  $t'\bar{t}'$  production, although we observe a small excess of events in the  $\mu + \text{jets}$  channel. Combining the  $e + \text{jets}$  and  $\mu + \text{jets}$  channels and under the assumption that the branching fraction  $B(t' \rightarrow Wq) = 100\%$ , we exclude at 95% C.L.  $t'\bar{t}'$  production for  $t'$  quark mass values below 285 GeV.

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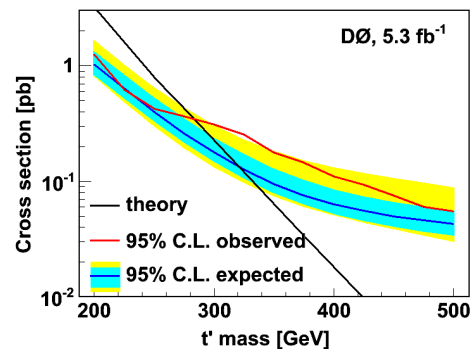


FIG. 4 (color online). Same as Fig. 3 but for both channels combined.



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