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LETTER TO THE EDITOR

Electron Energy Dissipation

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Abstract

A new algorithm for the computation of the energy dissipated by normally incident, monoenergetic electron beams, provides good agreement with experimental data and with the computations of Spencer.

For the interpretation of many radiation effects, a simple computing algorithm which yields information about the dissipation of the energy of normally incident

electron beams is of great utility. Such an algorithm¹ has been profitably applied to the study of heavy ion interactions, through a model which attributes heavy ion

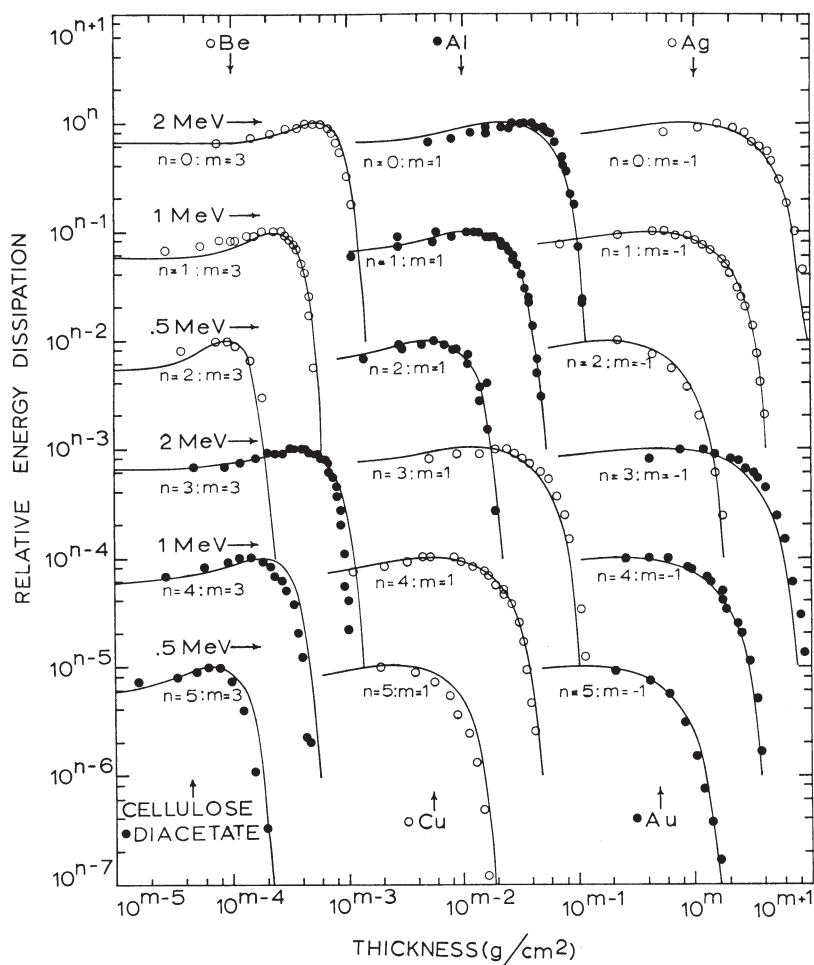


Figure 1. Relative electron energy dissipation data from Aiginger et al.⁵ for 0.5, 1.0, and 2 MeV electrons in Be, cellulose diacetate, Al, Cu, Ag, and Au, plotted over calculations from equation (4). Since these data are in relative units, with the maximum dissipation set to unity in each case, the calculations have been similarly normalized.

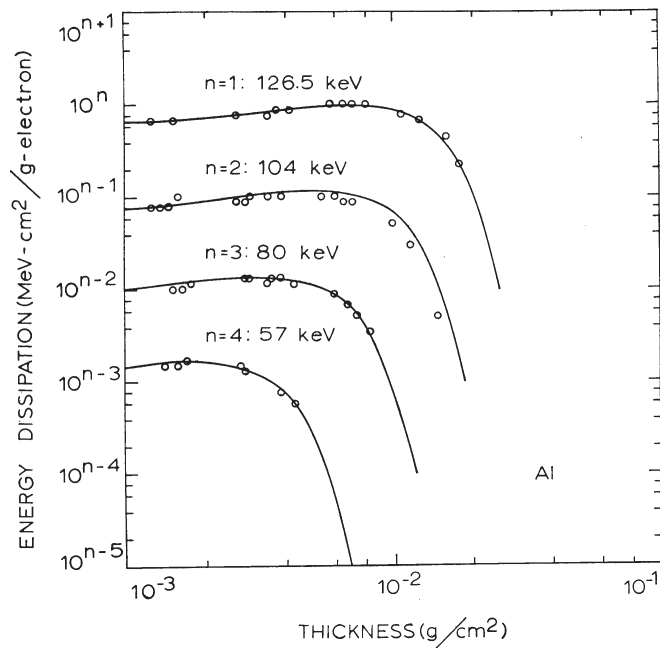


Figure 2. Electron dissipation data from Huffman et al.⁶ for 57, 80, 104, and 126.5 keV electrons in Al, plotted over calculations from equation (4).

effects to the dose of ionization energy deposited by δ -rays. The present paper describes an improved form of the earlier algorithm, developed for the same purpose.

The characteristic thickness:

The work of Depouy et al.² has shown that the definition of the practical (extrapolated) range of electrons in many materials is somewhat ambiguous, and that a more suitable description of the interaction of electron beams with foils is obtained through use of the characteristic thickness r_η , at which the probability for electron transmission is η . These authors have given expressions for the transmission probability (for an energy interval 50-1,200 keV) and its associated characteristic thickness (for an energy interval 20 keV to 20 MeV) as a function of the atomic number and atomic mass of the absorber.

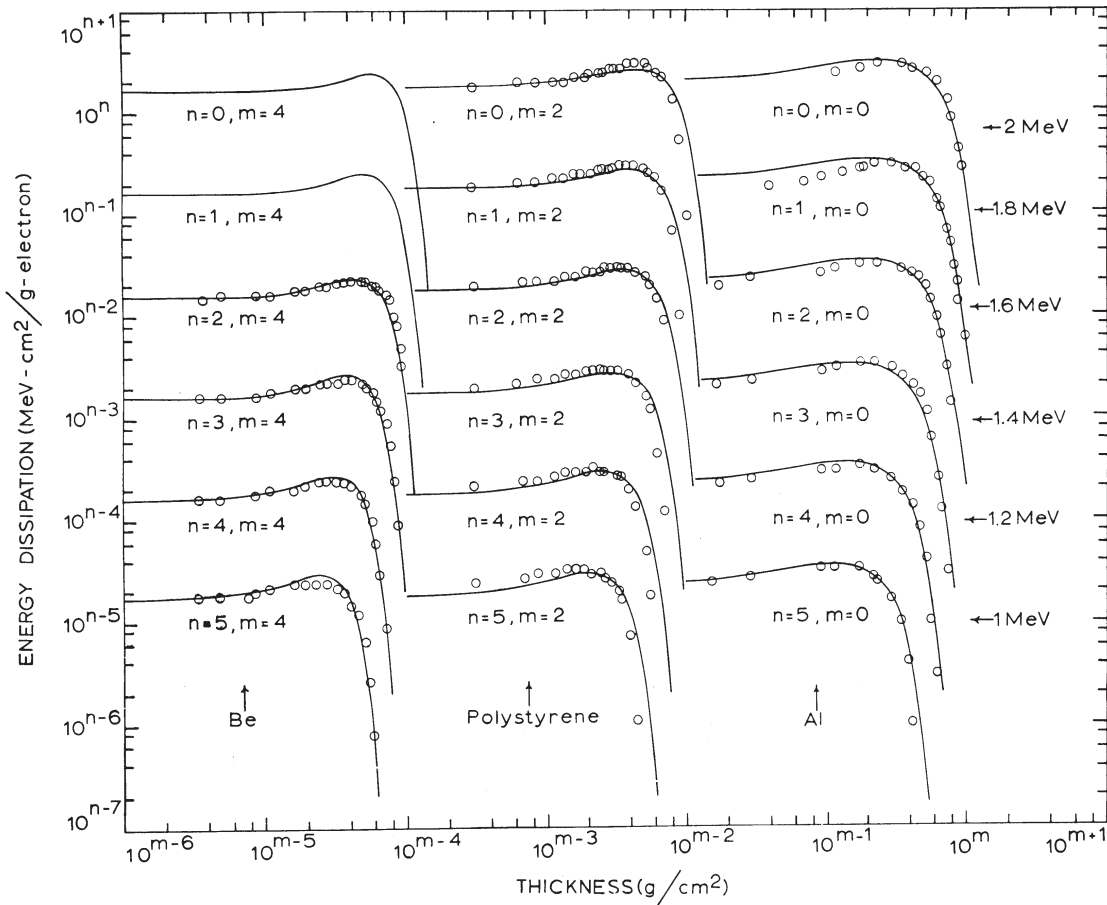


Figure 3. Electron energy dissipation data from Nakai et al.⁷ for 1.0, 1.2, 1.4, 1.6, 1.8, and 2.0 MeV electrons in Be, polystyrene, and Al, plotted over calculations from equation (4).

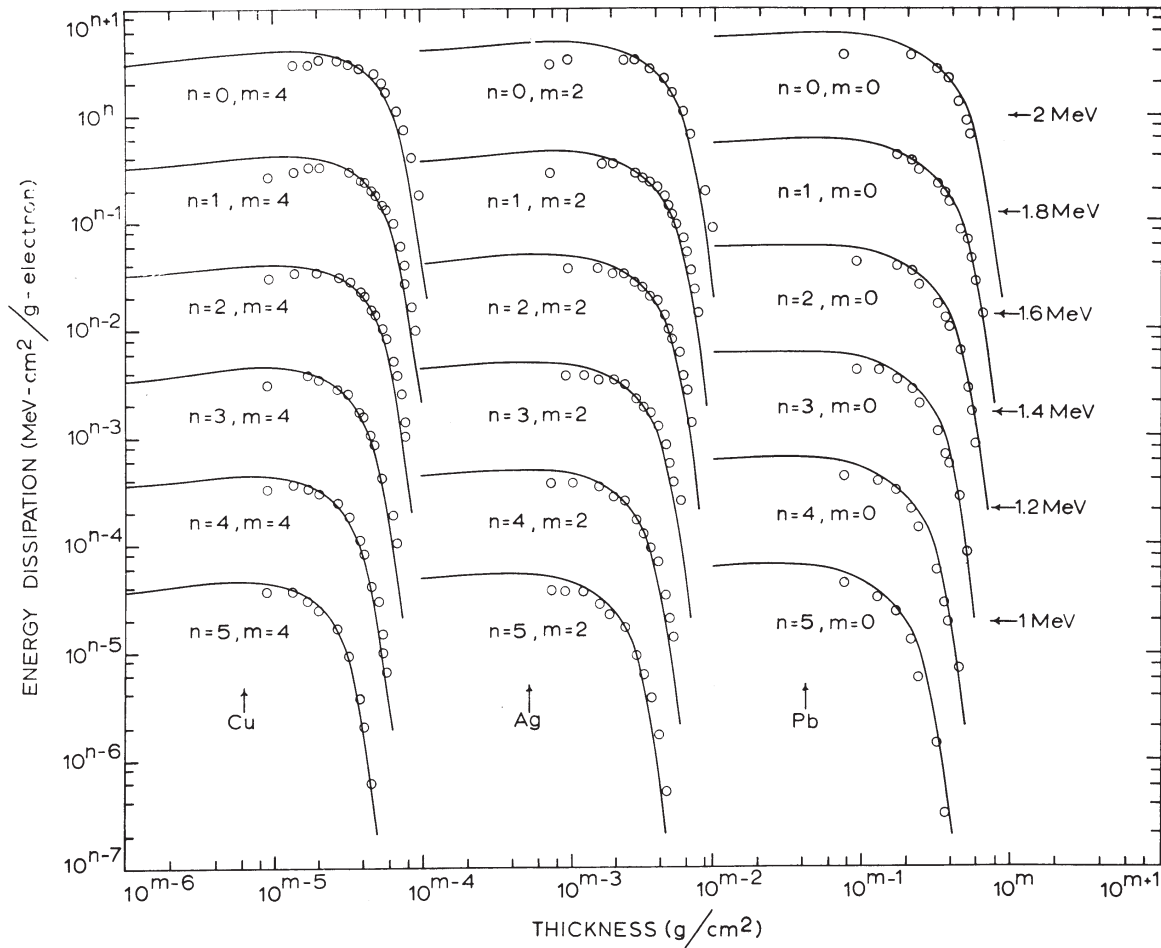


Figure 4. Electron energy dissipation data from Nakai⁷ for 1.0, 1.2, 1.4, 1.6, 1.8, and 2.0 MeV electrons in Cu, Ag, and Pb, plotted over calculations from equation (4).

Since the form of the expression given by Depouy et al. for the characteristic thickness does not lend itself either to application to gases, or to extrapolation to lower energies, constants have been calculated for a formula of Weber,³ giving the 5% characteristic thickness, $r_{0.05}$, for electrons of incident energy w , for use as a starting place in the development of an energy dissipation algorithm.

The expression

$$r_{0.05} = Aw[1 - B/(1 + Cw)], \quad (1)$$

where

$$A = (1.06 Z^{-0.38} + 0.18) \times 10^{-3} \text{ g/cm}^2 \cdot \text{keV},$$

$$B = 0.22 Z^{-0.055} + 0.79,$$

$$C = (1.3 Z^{0.3} + 0.21) \times 10^{-3} / \text{keV},$$

yields results in 5% agreement with those of Depouy et al., for the materials investigated by these authors.

Our earlier algorithm for the computation of electron energy dissipation made use of a practical range-energy

relation for aluminum, based on the formula of Weber,³ in combination with an expression for the probability for the transmission of electrons through any material, due to Rao.⁴

The present work utilizes the expressions of Depouy et al. for the transmission probability η and the characteristic thickness r as its starting place, recasting the latter expression in the form of equation (1). Constants and exponents in these expressions have been altered through a parameter-seeking computer program, set to minimize the difference between computations from the algorithm and experimental energy dissipation data. The procedure used allows Z-dependence in both r and η .

Energy dissipation algorithm:

The structure of the energy dissipation algorithm is motivated by the argument that electrons of initial energy w and characteristic thickness r which penetrate a foil of

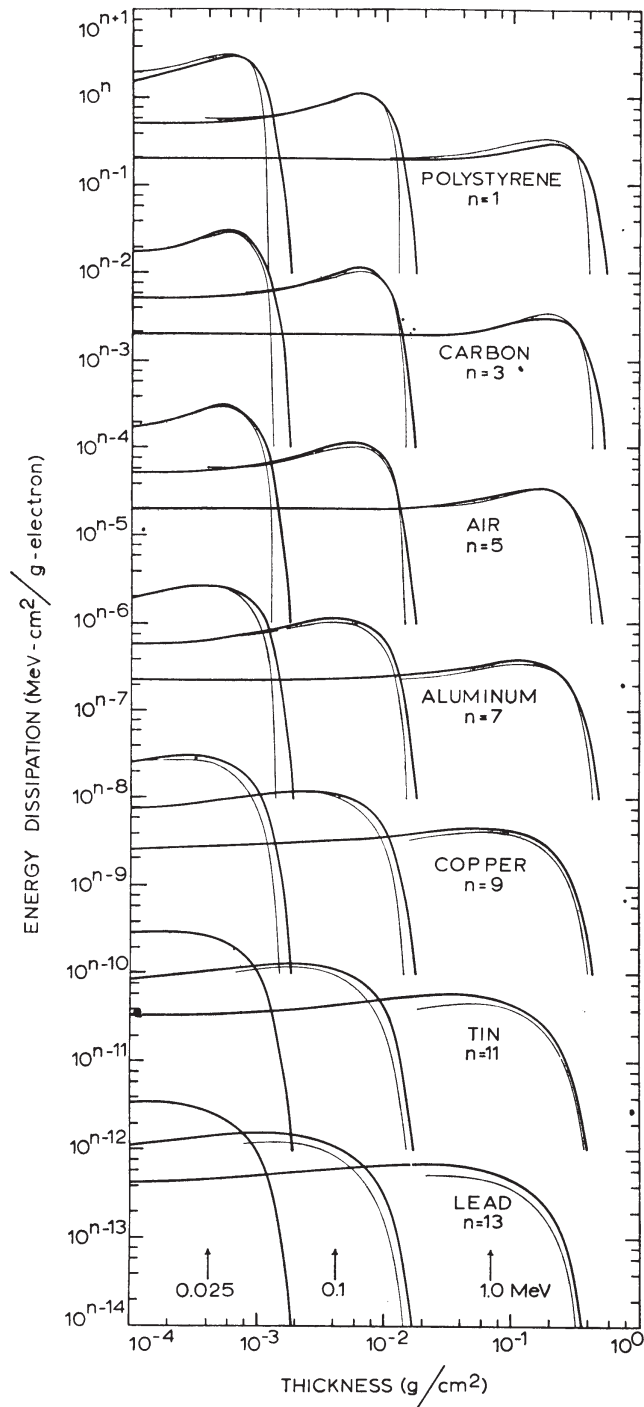


Figure 5. Electron energy dissipation for 0.025, 0.1, and 1 MeV electrons in polystyrene, C, air, Al, Cu, Sn, and Pb. Light lines are from Spencer,⁸ while dark lines are from equation (4).

thickness t have residual energy W , which can be found from the characteristic thickness-energy relationship as the energy to go to the residual distance $r - t$. The residual energy may be written in functional form as

$$W(r, t) = w(r - t). \quad (2)$$

The energy transmitted through a foil by a single incident electron is then approximated by the product of η , the probability of transmission, and W , the residual energy. The energy E , dissipated at depth t by a beam containing one electron/cm² may be represented as

$$E = d(\eta W) dt. \quad (3)$$

The use of a characteristic thickness-energy relationship in such a structure suffers from several difficulties. First, it appears to neglect back-scattering, though it may be argued that the energy lost from a layer dt by backscattering is compensated by energy back-scattered from later layers. Second, all electrons are represented by an underscattered class, namely those which penetrate to the characteristic distance. Third, the energy deposited by the least scattered electrons, which penetrate to a thickness $t > r$, is neglected. It must therefore be expected that improved agreement with experiment will arise from limiting the applicability of equation (3) to some thickness less than $r_{0.05}$, and by utilizing a second expression expressly created to accommodate straggling beyond that thickness. This has been done, with the following results.

The energy density $E(t)$, dissipated in a material of atomic number Z , in a layer of thickness dt at depth t by a normally incident beam containing 1 electron/cm², of initial energy w , whose characteristic thickness is r , is given by the expressions:

for $t/r \leq 0.9$:

$$\begin{aligned} E(t) &= d(\eta W) / dt, \\ \eta &= \exp \{-(qt/r)^p\}, \\ W(r, t) &= w(r - t), \\ r &= Aw[1 - B/(1 + Cw)], \\ q &= 0.0059 Z^{0.98} + 1.1, \\ p &= 1.8 (\log_{10} Z)^{-1} + 0.31, \\ A &= (1.06 Z^{-0.38} + 0.18) \times 10^{-3} \text{ g/cm}^2 \cdot \text{keV}, \\ B &= 0.21 Z^{-0.055} + 0.78, \\ C &= (1.1 Z^{0.29} + 0.21) \times 10^{-3} / \text{keV}; \end{aligned} \quad (4)$$

for $t/r > 0.9$:

$$E(t) = E(0.9r) \times \{\eta/\eta(0.9r)\}^{4/p}.$$

For mixed materials and compounds, Z is replaced by its average value, weighted over the mass fractions.

Comparison with experimental data:

The precise expressions for the constants q , p , A , B , and C , in equation (4) depends on the data which is represented by these expressions, for there is some disagreement among investigators. The values reported were obtained by a criterion of best agreement with the combined data of Aiginger et al.,⁵ Huffman et al.,⁶ and Na-

kai et al.⁷ Calculations from equation (4) are compared with their experimental results in Figures 1–4. For completeness we also show the comparison of calculations from equation (4) with the theory of Spencer⁸ in Figure 5. The results of the present computing algorithm represent a significant improvement over our earlier effort. Over a wide range of materials and energies, equation (4) represents experimental data to an average deviation of about 10%, which approximates the uncertainty of the data itself.

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