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## THE COMA/A1367 SUPERCLUSTER AND ITS ENVIRONS

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### ABSTRACT

The three-dimensional galaxy distribution in the region of space surrounding the two rich clusters Coma and A1367 is analyzed by using a nearly complete redshift sample of 238 galaxies with  $m_p < 15.0$  in a  $260^\circ$  region of the sky; 44 of these redshifts are reported here for the first time. We find that the two clusters are enveloped in a common supercluster which also contains four groups and a population of isolated galaxies. The least dense portions of the Coma/A1367 supercluster have a density which is approximately 6 times that of the Local Supercluster in the regions of our own Galaxy. In front of the Coma/A1367 supercluster we find eight distinct groups or clouds but no evidence for a significant number of isolated "field" galaxies. In addition, there are large regions of space with radii  $r > 20 h^{-1}$  Mpc where there appear to be no galaxies whatever. Since tidal disruption is probably responsible for the isolated component of supercluster galaxies, the observations suggest that all galaxies are (or once were) members of groups or clusters. A number of related topics with more general significance are also discussed. (1) The size-to-separation ratio for foreground groups indicates that the redshift of group formation is  $z \lesssim 9$ . (2) There is a general correlation between the volume mass density of a galaxy system and the morphologies of the component galaxies. (3) Finally, we speculate that all clusters of richness class  $\geq 2$  are located in superclusters.

*Subject headings:* galaxies: clusters of — galaxies: redshifts

### 1. INTRODUCTION

Galaxies appear to be organized on the largest scale in extensive, second-order clusters called *superclusters*. The early controversy over this matter (see Abell 1975) has been settled by Peebles and his collaborators (see Peebles 1974), who have studied the projected distribution of galaxies on the sky. More detailed information on superclustering is available if a third spatial dimension can be added directly. For example, Rood (1976) studied the three-dimensional distribution of nearby clusters by assuming that the average redshift of the observed members of a cluster is an accurate indicator of the cluster's distance, and his findings are consistent with earlier results. Our purpose in this paper is to use a redshift-based technique for studying the three-dimensional distribution of a large number of galaxies in the region of the sky defined by  $11^h 5 \leq \alpha \leq 13^h 3$ ,  $19^\circ \leq \delta \leq 32^\circ$ . Within this surveyed region lie the two rich clusters Coma and A1367, and the results presented below will show that they are embedded in a common, very large supercluster.

The existence of the Coma/A1367 supercluster per se was not suggested until recently (Tift and Gregory 1976; Chincarini and Rood 1976). We note that Abell

(1961) thought that there might be a supercluster containing six clusters centered at  $11^h 45^m$ ,  $+29^\circ 5'$  (1950) which had a diameter of  $45 h^{-1}$  Mpc and would therefore include Coma and A1367. However, this suggestion was made before redshifts were available for any of the clusters except Coma. Two of the members, A1185 and A1213, are now known to have significantly higher redshifts than Coma and A1367 (Noonan 1973). The present study is the first that can actually demonstrate that Coma and A1367 form a unified system. The reason that the Supercluster<sup>1</sup> was not recognized long ago is that the two major cluster centers are widely separated. Hauser and Peebles (1973) found that rich cluster pairs are correlated if their separation is less than  $\sim 20 h^{-1}$  Mpc, where  $h \equiv H_0/100 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . For the case of Coma and A1367 the separation is  $21 h^{-1}$  Mpc. This wide physical separation coupled with the Supercluster's proximity to our own Galaxy (the distance to the Supercluster is  $\sim 70 h^{-1}$  Mpc) make the angular

<sup>1</sup> Hereafter we will use the proper noun "Supercluster" when referring to the Coma/A1367 supercluster if no confusion results. Following current usage, the general term "supercluster" will be used when referring to groups of galaxy clusters. At times in the past (cf. Shane 1975), these groups of clusters have been called "clouds," a term which is now reserved for loose aggregates of galaxies such as the Coma I cloud.

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separation  $\sim 20^\circ$ , which is too large to be visually impressive at, say, the scale of the Sky Survey.

The very large sizes of superclusters offer compelling reason for studying them in detail. Internal mixing cannot be well advanced, so the present distributions of galaxy luminosity and morphology must reflect to some extent the properties of the primordial supercluster material. We will show in the following analysis that there are three observationally distinct populations of galaxies within the Supercluster. These are (1) galaxies located in the two rich cluster cores, (2) galaxies located in intermediate- or low-mass clusters, and (3) a nearly homogeneously distributed population of isolated galaxies.

An important additional benefit of our magnitude-limited survey is that it samples foreground galaxies in addition to those in the more distant Supercluster. This adds a fourth distinct population to the three found in the Supercluster. The foreground galaxies are found in low-mass clusters; they are not distributed in a homogeneous "field." The addition of these foreground systems to our sample of clusters enables us to examine intrinsic properties of clusters over a range of  $\sim 10^2$  in mass.

## II. THE REDSHIFT SURVEY

The purpose of our new redshift program is to provide a sample of galaxies complete to a limiting magnitude of  $m_p < 15.0$  in the area of the sky encompassing the two rich clusters Coma (A1656) and A1367. Previous redshift observations are summarized by Tift and Gregory (1976) for galaxies with  $m_p < 15.0$  and  $r < 6^\circ$  from the Coma cluster center, by Chincarini and Rood (1976) for galaxies with  $m_p \leq 15.0$  in a region directly west of Coma, and by both Tift and Tarenghi (1975) and Dickens and Moss (1976) for galaxies near the center of A1367.

Although the above mentioned surveys cover a substantial region of the sky, they left a large gap along a line connecting Coma and A1367 in which very few galaxies have been studied. For our new observations we tried to observe each apparently isolated galaxy in this gap for which no previous redshift determination existed. However, because of observing time limitations and two aborted attempts on very low-surface-brightness objects, five of the galaxies lying within  $r \lesssim 3^\circ$  of the line joining the two clusters still do not have measured redshifts. In addition to the apparently isolated galaxies, there were five obvious groups for which no distance information existed. We tried to be as complete as possible in obtaining redshifts in the two groups nearest to A1367 so that their relationship to the rich cluster might be clarified. For the remaining groups we assumed that the redshifts of the one or two brightest galaxies were representative of the whole.

We obtained the new spectra during the nights 1976 April 27–28 to April 30–May 1 with the Kitt Peak 2.1 m telescope equipped with the white CIT spectrograph and a HeNeAr comparison source. The 300 line  $\text{mm}^{-1}$  grating gave a dispersion of  $240 \text{ \AA mm}^{-1}$  in the blue, and the spectra were recorded on baked

IIIa-J spectroscopic plates. The spectrograms were measured with either a Mann comparator or a Grant measuring engine with scanning display. No significant difference was found between the results obtained for selected spectrograms measured on both instruments. The [O I]  $\lambda = 5577.35$  night-sky line was measured and used to correct for systematic spectrograph or measuring errors; the average correction was  $+6 \pm 28 \text{ km s}^{-1}$ . We used the effective wavelengths given by Sandage (1975), and we corrected for  $300 \text{ km s}^{-1}$  galactic rotation.

In Table 1 we list the new redshifts along with other pertinent data. Column (1) contains the identification number from Zwicky and Herzog (1963, hereafter CGCG). The first three digits give the CGCG field number, and the last three digits give the sequential galaxy number. Columns (2), (3), (4), and (5) give the NGC or IC numbers, the 1950 epoch right ascension and declination, and the photographic magnitude  $m_p$ . In column (6) we list the new redshift determinations. Typical uncertainties for redshifts of galaxies with  $13 \leq m_p \leq 15$  at this dispersion are  $\pm 100 \text{ km s}^{-1}$ ; parentheses in column (6) denote one particularly uncertain redshift and one which was estimated. Column (7) lists those spectral lines which were measured with nonzero weight. The lines  $\lambda = 3727$  and  $\lambda = 5007$  were, of course, always in emission. Hydrogen Balmer lines were found in absorption unless denoted by (em). Because of possible blending with He, the Ca I H-line was not used if any Balmer lines of shorter wavelength than H $\beta$  were visible.

When the 44 new redshifts are combined with those in the literature, we have a total sample of 238 galaxies with  $m_p < 15.0$  in the surveyed area.

## III. RESULTS

### a) Overview of the Supercluster Area

Although we are most interested in studying the galaxies located between and in the immediate vicinity of the Coma and A1367 clusters, it is of importance to investigate the total possible extent of the Supercluster. Consequently, we show in Figure 1 an isophotal diagram for the region of the sky which contains the Supercluster; the surface area of this diagram is  $\sim 10$  times that of our redshift survey. The contours represent the luminosity distribution of galaxies at surface-brightness intervals of 0.5 mag. The diagram was constructed by averaging at  $1^\circ$  centers the total luminosity of those galaxies which fall within a radial distance of  $1^\circ$  from each averaging center. All galaxy magnitudes and positions were taken from a magnetic tape version of CGCG, and the averaging process was carried out by computer at the Kitt Peak National Observatory. Because the surface-brightness contours are by definition luminosity-weighted, background contamination is insignificant. Foreground contamination can be substantial, and two techniques were used to reduce this problem. First, no galaxy was included in the luminosity average if it had an apparent magnitude brighter than the first brightest galaxy in either A1367 or Coma (NGC 4889 has  $m_p = 13.0$ ). Second,

TABLE 1  
NEW REDSHIFTS

Zwicky No.	Name	$\alpha$ (1950)	$\delta$ (1950)	$m_p$	$V_0$	Spectral Lines Used	Notes
097030	N 3768	11 <sup>h</sup> 34 <sup>m</sup> 6	+18° 07'	13.7	3288	K, H, 5175	
097051	N 3801	11 37.7	+18 00	13.3	3356	K, 4384, 5269	
097161	N 3919	11 48.0	+20 17	14.5	6052	H, G, 4384, 5175	
127022	N 3798	11 37.6	+24 59	13.9	3459	K, H $\delta$	
127027	N 3812	11 38.5	+25 07	13.9	3529	K, H	
127050		11 43.4	+21 19	14.8	(6736)	H	1
127063	N 3910	11 47.4	+21 38	14.4	7768	K, G, 5175	
127064	N 3920	11 47.5	+25 13	14.1	3547	3727, K, H $\delta$ , H $\gamma$ , 5007	
127076N		11 48.9	+22 19	--	8514	H, G	2
127076S	N 3926	11 48.9	+22 19	14.1	7464	K, H	2
127080	N 3929	11 49.1	+21 17	14.5	7041	K, H, G	
127086		11 50.0	+23 53	14.8	6793	K, H, G	
127088	N 3937	11 50.1	+20 55	14.0	6554	K, G, 5175	
127089	N 3940	11 50.1	+21 17	14.3	6341	K, G, 4384	
127090	N 3943	11 50.3	+20 46	14.7	6559	H, G	
127098	N 3954	11 51.1	+21 10	14.4	6800	K, H, G	
127099	N 3951	11 51.1	+23 40	14.5	6430	K, H	
127100		11 51.4	+20 52	14.9	6840	K, H, G	
127110	N 3987	11 54.7	+25 29	14.4	4508	K, H	
127115	N 4003	11 55.4	+23 24	14.8	6438	K, H	
127120	N 4005	11 55.6	+25 24	14.1	4333	K, H, H $\delta$ , 4226, G, 5175	
128003		12 00.9	+22 30	14.6	6476	3727, K, H, 4384, H $\beta$ (em)	
128005	N 4061	12 01.5	+20 30	14.4	7072	K, H, 5175	
128007	N 4065	12 01.6	+20 30	14.0	6216	K, H, 5269	
128008	N 4066	12 01.6	+20 38	14.4	7294	H, G	
128009	N 4070	12 01.6	+20 42	14.3	7143	K, H, 5175	
128017	N 4084	12 02.7	+21 30	14.9	6621	K, H, G, 5269	
128020	N 4089	12 03.0	+20 50	14.9	6905	K, H, G	
128023	N 4092	12 03.3	+20 46	14.4	6737	K, H	
128025	N 4095	12 03.4	+20 51	14.6	7057	K, H, 4226, G, 5269	
128026	N 4098	12 <sup>h</sup> 03 <sup>m</sup> 5	+20° 53'	14.5	7280	K, H $\delta$ , H $\beta$	
128027	N 4101	12 03.6	+25 50	14.7	6089	K, H, G	
128034		12 05.5	+25 31	14.4	(6700)		3
128054		12 10.8	+21 55	14.6	7220	K, H, 5175	
128060	N 4204	12 12.7	+20 56	14.3	690	3727	4
128065	N 4213	12 13.1	+24 15	14.3	6986	K, H	
128077	I 780	12 17.4	+26 03	14.5	6779	K, H	
128078	I 3171	12 17.9	+25 51	14.8	6935	K, H	
128089	I 791	12 24.5	+22 55	14.2	6735	K, H	
129002	N 4455	12 26.2	+23 06	13.0	588	3727	4
129012	I 3581	12 34.1	+24 42	14.9	6972	K, H	
129020	I 3692	12 40.4	+21 16	14.8	6412	K, H, G	
161042		13 21.4	+31 50	13.9	4723	K, H, G	
161056	N 5157	13 25.0	+32 17	14.4	7230	K, H, 5175	

- NOTES: 1. Redshift is more uncertain than usual, since only one line had non-zero weight in the determination.  
 2. Northern component is fainter; both appear imbedded in the same halo.  
 3. One side of the comparison spectrum was ruined;  $V_0$  is an estimate.  
 4. Poor quality spectrum; however,  $\lambda$ 3727 was easily measured. Accuracy of  $V_0$  is not as poor as if only one absorption line had been measured.

two separate contour diagrams were produced, the first for  $m_p \geq 13.0$  and the other for  $m_p < 13.0$ . The second version shows mainly local galaxies, so it was possible to identify on the first version those regions that are strongly contaminated by faint galaxies in nearby groups and clusters. Figure 1 shows only the first version (i.e.,  $m_p \geq 13.0$ ), but those features in Figure 1 that have corresponding contours in the second version are shown in dashed lines. For instance, the faint galaxies in the extensive Virgo cluster complex dominate the region centered at 12<sup>h</sup>30<sup>m</sup>, +13°, but since the contours are shown as dashed lines they are easy to ignore.

Some interesting features are obvious. First, the Coma cluster has an elliptical shape with ellipticity approximately equal to 0.5; estimates of the ellipticity have been published elsewhere (Rood *et al.* 1972; Thompson and Gregory 1978; Schipper and King 1978). There also seems to be a difference between the regions just exterior to the two rich clusters. A1367 is surrounded by a tenuous group of galaxy clouds, whereas the region around Coma is nearly devoid of structure. Only one concentration is seen near Coma. This is the NGC 5056 group, which may not be part of the Supercluster. The contour diagram is somewhat deceptive because the faintest illustrated isophote is

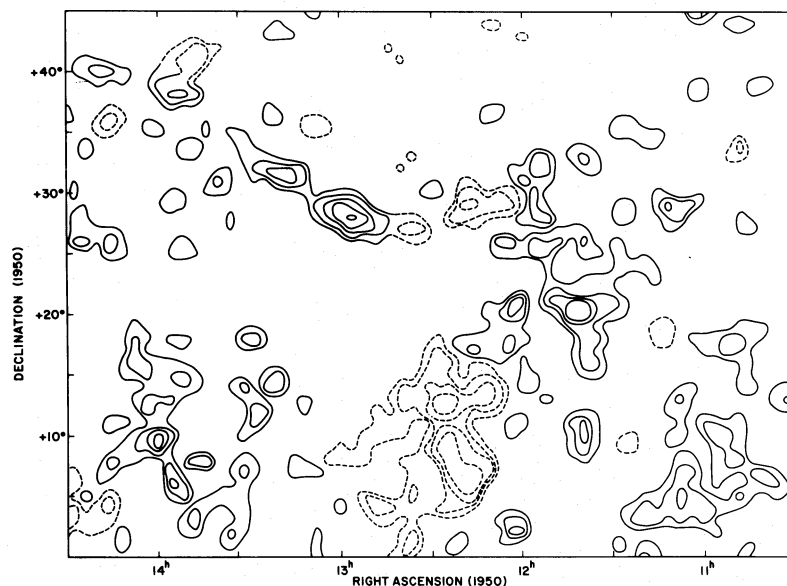


FIG. 1.—Luminosity contour diagram of the Coma/A1367 Supercluster and its surroundings for galaxies in the Zwicky catalog with  $m_p \geq 13.0$ . The contours are spaced at 0.5 mag intervals. The brightest contour level is  $29.5 \text{ mag arcsec}^{-2}$ , and the faintest is  $31.5 \text{ mag arcsec}^{-2}$ . Dashed lines, regions that are probably in the foreground. The NGC 5416 cluster ( $\alpha \approx 14^h$ ,  $\delta \approx 10^\circ$ ) has a luminosity similar to that of the Coma ( $\alpha \approx 13^h$ ,  $\delta \approx 28^\circ$ ) and A1367 ( $\alpha \approx 11^h40^m$ ,  $\delta \approx 20^\circ$ ) clusters.

not at the limiting luminosity of CGCG but at the level beyond which the background becomes quite noisy. We will show in the following section, using the complete redshift sample to eliminate foreground and background confusion, that the region around the Coma cluster is not entirely empty but contains a widely dispersed but significant population of Supercluster galaxies.

An additional feature of Figure 1 which has potential importance is the concentration of galaxies at  $\alpha = 14^h$ ,  $\delta = +10^\circ$ . Although this concentration is nearly as prominent as A1367, it has escaped notice (for example, it has no Abell number). We will refer to this system as the NGC 5416 cluster. No redshifts are available for any of the member galaxies, but a comparison of apparent luminosity functions shows that the NGC 5416 cluster may well lie at the same distance as Coma and A1367 and may therefore indicate that the Supercluster is larger than the boundaries of our redshift survey. The NGC 5416 cluster is surrounded by an extensive system of galaxy clouds and hence is very similar to A1367.

#### b) Coma/A1367 Supercluster: The Interconnection

There is no widely accepted definition of the term "supercluster." At present, observational studies of superclusters use largely subjective criteria which are based on the distance and angular proximity of cluster centers. In the case of two clusters which are as widely separated as Coma and A1367, we believe that, in order to show that they are members of the same supercluster, it is both necessary and sufficient to demonstrate the presence of a population of galaxies

linking the two clusters which is itself a region of significantly enhanced density. For ease of discussion, the area between Coma and A1367 will be called the intercluster region (ICR), and the galaxies in this region will be referred to as ICR galaxies. We present a list of these galaxies in § IIIe; here we will show only that the density of the ICR is indeed significantly large.

The intercluster region is easily recognized in Figure 2a. The diagram shows the projected three-dimensional distribution of our sample galaxies. Since Coma and A1367 are separated primarily in the east-west direction, we have plotted the positions in the coordinate system right ascension versus redshift. By making the width of the R.A. axis a linear function of redshift, we have removed the major distance-dependent distortion. If the R.A. axis were of uniform width over the entire redshift range, a hypothetically spherical nearby group would appear to be unrealistically elongated in right ascension. According to the Hubble relation, redshift is proportional to distance for galaxies at rest with respect to their local comoving coordinates. However, in the relaxed cores of massive clusters galaxies have large kinetic energies, and the extreme redshifts are not indicative of distance effects. These clusters appear as very elongated structures which point toward the origin of the wedge diagram.

Two features of Figure 2a are significant. First, the clumpiness of the foreground distribution is clear. There are several groups of galaxies, and it is important to note there are large regions which are devoid of galaxies. (In fact, we note that no galaxies with  $m_p < 15.0$  are found within 20 Mpc of the near side of the intercluster region.) The second point is that

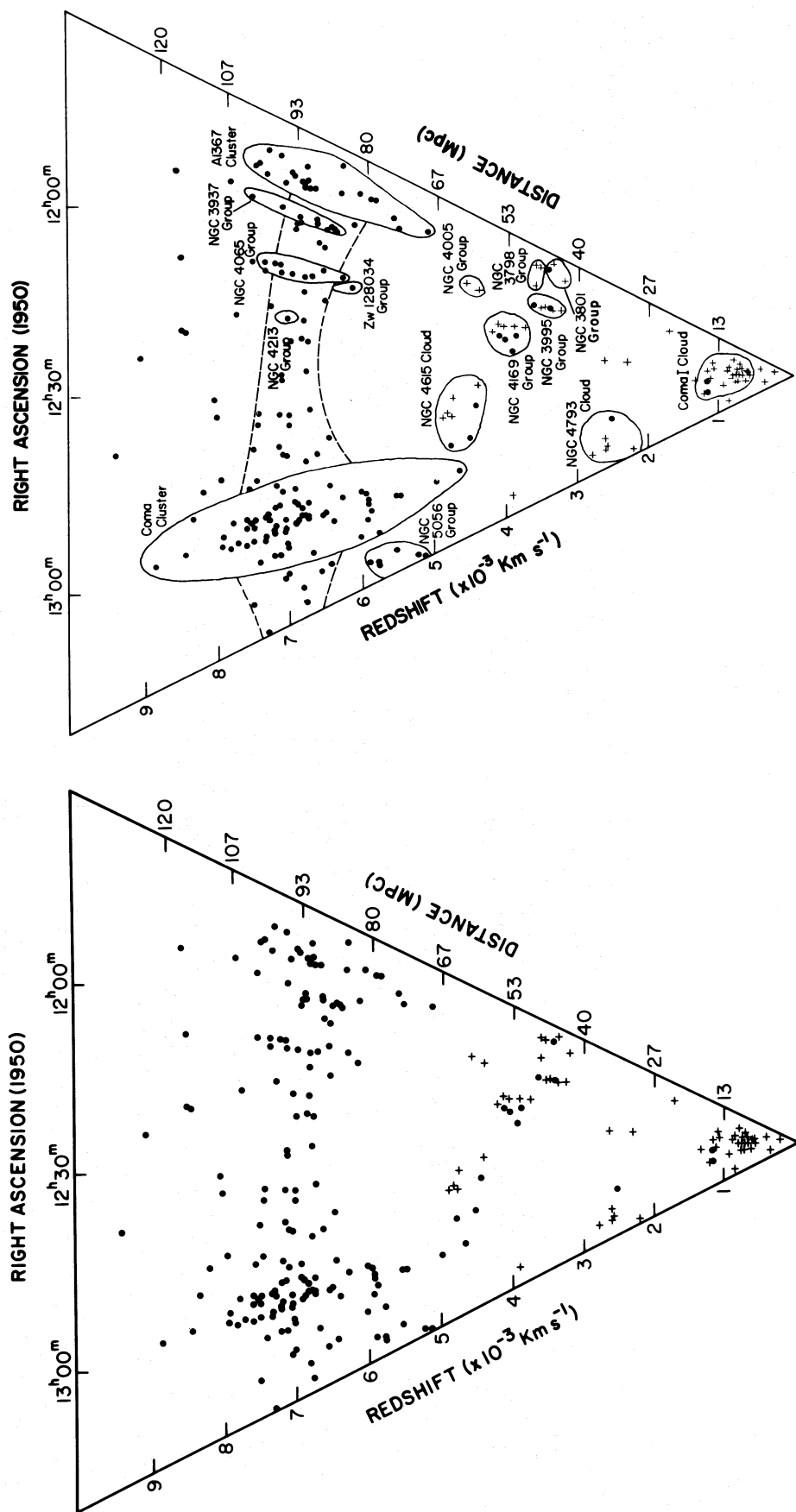


FIG. 2.—(a) (left panel) Wedge diagram for all galaxies in our sample. The Supercluster is clearly seen at an average redshift of approximately  $7000 \text{ km s}^{-1}$ . The distribution of foreground galaxies is very clumpy. Those galaxies with  $V_0 < 5000 \text{ km s}^{-1}$  that are represented by crosses are too faint to be surveyed if they were at the distance of the Supercluster. The distance scale assumes  $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , and the angular size of the survey has been magnified by approximately 2 times. (b) (right panel) An interpretive form of the wedge diagram.

Figure 2a gives a misleading visual impression of the density of the foreground. Since our survey is limited by a fixed apparent magnitude, nearby groups are studied to intrinsically fainter limits than the Supercluster. We correct for this effect by using two symbols for those galaxies with  $V_0 < 5000 \text{ km s}^{-1}$ . Galaxies represented by large filled circles have absolute magnitudes  $M_p$  which satisfy the condition  $M_p \leq M_l$ , where  $M_l$  is the limiting absolute magnitude of galaxies studied in the Supercluster. With  $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (assumed throughout unless explicitly stated otherwise) and a limiting apparent magnitude of  $m_p = 14.9$ , we find  $M_l = -19.9$ . Those foreground galaxies that are represented by crosses have  $M_p > M_l$  and would be too faint to be included in our survey if they were members of the Supercluster. Figure 2b is an interpretive form of Figure 2a. Borders for all the galaxy systems have been added, and they will be discussed below.

We will now use two comparisons to show that the ICR has a significantly enhanced density. First, we calculate the density contrast  $\rho_{\text{ICR}}/\rho_f$  between the intercluster region and the foreground ( $f$ ) because  $\rho_f$  is characteristic of the mean density of the universe outside of rich clusters. We take the ICR to be  $6.4 h^{-1} \text{ Mpc}$  thick (see § IIIe). The 69 ICR galaxies are distributed over  $167 \text{ degrees}^2$  of the sky, so they occupy a volume of  $1.6 \times 10^3 h^{-3} \text{ Mpc}^3$ , giving a number density  $n_{\text{ICR}} = 4.4 \times 10^{-2} h^3 \text{ Mpc}^{-3}$ . In the foreground there are 13 galaxies with  $M_p \leq M_l$ , and they occupy the volume of space out to a redshift of  $\sim 5000 \text{ km s}^{-1}$ , corresponding to  $3.3 \times 10^3 h^{-3} \text{ Mpc}^3$ . The number density of foreground galaxies is then  $n_f = 3.9 \times 10^{-3} h^3 \text{ Mpc}^{-3}$ . By assuming that the  $M/L$  ratios and luminosity functions of the two populations are identical, we find  $\rho_{\text{ICR}}/\rho_f = 11$ .

For the second test we will compare the density of the ICR to that of the Local Supercluster (LSC) in our own vicinity. We are located at a distance from the center of the Local Supercluster that corresponds to the midpoint between the two rich clusters in the Coma/A1367 Supercluster. Jones (1976) finds that the local density of galaxies with  $M_B < -18$  is  $n_0 \approx 9 \times 10^{-3} \text{ Mpc}^{-3}$ . We convert this density to the limiting magnitude of our survey by using the luminosity function given by Abell (1975); this gives  $n_{\text{LSC}} \approx 3 \times 10^{-3} \text{ Mpc}^{-3}$ . Once again we assume constant  $M/L$  ratios and find  $\rho_{\text{ICR}}/\rho_{\text{LSC}} = 15 h^3$ . In his calculations, Jones used a value of  $h = 1$ , appropriate to the local vicinity of space (see van den Bergh 1970). For comparison with  $\rho_{\text{ICR}}$  we use both  $h = 1$  and  $h = 0.75$  and find a density contrast  $6 \leq \rho_{\text{ICR}}/\rho_{\text{LSC}} \leq 15$ .

Now that we have calculated the density of the ICR, we ask if such a large density could result from random fluctuations of a homogeneous "field." The method used to test this hypothesis is given by Chincarini and Rood (1976); we compare the observed redshift distribution of galaxies to that expected from a smooth field. A  $\chi^2$  test of the observed redshift distribution of foreground galaxies plus those in the ICR when compared to the theoretical distribution of field

objects (scaled to our larger data sample) shows that there is less than a  $10^{-7}$  probability that the observed distribution arises by chance fluctuations. Although the quoted probability refers to the entire redshift distribution from the foreground out to the Supercluster, it is clear that the ICR dominates the redshift distribution and could not be a chance fluctuation.

### c) Properties of the Foreground Galaxies

For the purposes of our analysis we will assume that the foreground consists of those galaxies with  $V_0 < 5000 \text{ km s}^{-1}$ . An exception is made for galaxies near the Coma and A1367 centers; for those galaxies with  $r < 1^\circ$ , a foreground galaxy must have  $V_0 < 4500 \text{ km s}^{-1}$ . This variation in the redshift criterion is necessitated by large kinetic energies of the galaxies projected near the centers of massive, relaxed clusters.

Given these criteria, we find eight distinguishable groups in the foreground, and only four out of 90 galaxies do not lie in these eight groups. For seven of these groups, detailed maps and lists of member galaxies are given in the Appendix. In addition to previously published data and new redshifts from Table 1, the lists in the Appendix give new estimates of the morphological types of the component galaxies. These new morphologies were determined by examination of the Kitt Peak National Observatory glass copies of the Sky Survey. In the present section we summarize the general properties of the foreground systems.

In order to compare the intrinsic characteristics of one cluster with those of another, we have extrapolated the mass and luminosity estimates to a fixed absolute limit. We choose  $M_p = -15.0$  as the limit because this is just fainter than the faintest galaxy luminosity in the closest group in our survey. Our extrapolation uses the luminosity function introduced by Abell (1975). Ideally, the luminosity function should be derived for each group independently. However, the small number of objects in the individual groups precludes such analysis. Fortunately, the shape of the luminosity function for galaxies in nearby groups seems to be similar to that in rich clusters (see Shapiro 1971).

We define  $n(M_{\text{lim}})/n(-15)$  to be the fractional number of cluster members that are bright enough to be included in our survey;  $M_{\text{lim}}$  is the limiting absolute luminosity corresponding to the  $m_p = 14.9$  at the distance of each cluster. The total estimated population of the cluster,  $N_{\text{calc}}$ , is then obtained from the relation

$$N_{\text{calc}} = N_{\text{obs}}[n(M_{\text{lim}})/n(-15)]^{-1},$$

where  $N_{\text{obs}}$  is the number of cluster members with  $m_p < 15.0$ .

A similar method is used to estimate each cluster's total luminous mass. We define  $l_i(M_{\text{lim}})/l(-15)$  to be the fractional luminosity of galaxies with  $M_p < M_{\text{lim}}$ . The mass estimate is obtained from

$$\mathfrak{M}_{\text{calc}} = \sum_{i=\text{E}, \text{S}, \text{O}, \text{S}} N_i(M/L)_i [l_i(M_{\text{lim}})/l(-15)]^{-1},$$

TABLE 2  
FOREGROUND SYSTEMS

Name	Type	$N_{\text{obs}}^{(1)}$	$N_{\text{calc}}^{(2)}$	$\bar{V}_0$	$\sigma_v$	Morphology (% Spiral)	$\log L_{\text{obs}}^{(3,4)}$	$\log N_{\text{calc}}^{(5,6)}$ (4)	Virial M/L	$R_h$ (degrees)	$\log \rho_{(M_\odot \text{ Mpc}^{-3})}^{(7,8,9)}$	
Coma I	cloud	22	46	933	224	59	11.15	13.25	12.32	(10 <sup>3</sup> )	2.72	11.63
NGC 4793	cloud	8	35	2513	186	100	10.73	12.77	11.62	1253*	2.74	10.95
NGC 3801	group	14	90	3262	-	65	10.91	13.10	12.12	-	0.58	12.96
NGC 3798	group	3	22	3512	-	(50)	10.42	12.64	11.69	-	0.79	12.00
NGC 3995	group	6	41	3390	131	67	10.85	13.05	12.10	185	0.65	12.71
NGC 4169	group	10	81	3955	140	61	11.10	13.33	12.38	31	0.64	12.81
NGC 4005	group	10	95	4420	-	55	10.95	13.11	12.02	-	0.32	13.35
NGC 4615	cloud	8	73	4623	193	88	11.02	13.17	12.18	247	2.52	10.66

NOTES: (1)  $m_p < 15.0$   
 (2) calculated for  $M_p \leq -15.0$   
 (3) solar units  
 (4)  $M/L = 200$  for E and S0 galaxies;  $M/L = 100$  for spirals  
 (5)  $M/L = 50$  for E galaxies, 30 for S0s, and 7 for spirals  
 (6) assuming  $H = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$

\*This value is probably high because of the inclusion of nonmembers; see discussion in text.

where the summation is taken over morphological types grouped into E, S0, and S classes,  $N_i$  is the observed number of member galaxies in each class, and  $(M/L)$  is an assumed mass-to-luminosity ratio for each morphological type. For each foreground system  $N_{\text{calc}}$  and  $\mathcal{M}_{\text{calc}}$  are given in Table 2, and a discussion of the results will be given in § IV. Further discussion of how these results relate to the spectrum of galaxy clustering will be given in a subsequent paper (Gregory and Thompson 1978).

Much of the discussion in § IV will refer to the volume mass densities of the observed clusters. The volume occupied by each cluster is taken to be  $V = 4/3\pi R_h^3$ , where  $R_h$  is the projected mean harmonic radius of the cluster and is found from

$$1/R_h = 1/n_{\text{pairs}} \sum_{\text{pairs}} 1/r$$

( $r$  is the separation between the members of a galaxy pair; for those pairs with  $r < 0.1$ ,  $1/r$  is not included in the average because large values of  $1/r$  force  $R_h$  toward unrealistically small values).

For four foreground groups enough data exist to warrant calculation of the virial  $M/L$  ratio required to bind the system. For the virial calculation, we use the method described by Materne (1974), except that we assume there is a  $100 \text{ km s}^{-1}$  uncertainty for the redshift of each galaxy and that redshift differences among group members represent only line-of-sight motion.

In Table 2 we present the observed and calculated data for the foreground systems. The adopted system name and type (group or cloud) are found in columns (1) and (2), respectively. In columns (3) and (4) we list  $N_{\text{obs}}$  and  $N_{\text{calc}}$ , while columns (5) and (6) give the mean redshift and dispersion. Column (7) presents the relative number of galaxies with morphological type later than S0 (i.e., %S).<sup>2</sup> The total observed luminosity

<sup>2</sup> Hereafter, %S indicates percent of spirals.

is given in column (8). Columns (9) and (10) contain the mass estimates for two cases.  $M/L$  ratios of 200, 200, and 100 were used for E, S0, and S galaxies, respectively, to obtain the values in column (9);  $M/L$  ratios of 50, 30, and 7 were used for column (10). Virial  $M/L$  ratios are presented in column (11) for the four systems with sufficient data.  $R_h$  and the logarithm of the volume mass density ( $M_\odot \text{ Mpc}^{-3}$ ) are listed in columns (12) and (13).

Galaxies were assigned membership in groups and clouds on the basis of their projected spatial proximity and their redshift similarities. If clusters merged slowly into a smooth field of galaxies, our subjective method would be unreliable. However, the absence of an observed field makes cluster definition simple and natural when enough redshifts are available. We find that the scale length contrast—i.e., the ratio of the average nearest-neighbor separation of groups and clouds,  $l_{\text{cl}}$ , to the average mean harmonic radius—is  $l_{\text{cl}}/R_h = 7$ .

In general, the calculated virial  $M/L$  ratios are typical for galaxy systems, ranging between  $31 \leq M/L \leq 247$ . An exception, however, is the value of  $M/L = 1253$  for the NGC 4793 cloud. Such a large value suggests that we may have included nonmembers. However, even after excluding the three most likely nonmembers (NGC 4275, NGC 5089, and IC 777), we find that the ratio is still large,  $M/L = 381$ . Since the only galaxies in the foreground that might be considered isolated are in the vicinity of this cloud, and since it requires an unusually high mass-to-light ratio to be bound, it seems likely that the NGC 4793 cloud is dispersing.

Considering the general properties given in Table 2 and the details and maps given in the Appendix, we can summarize the foreground region as follows: No evidence is found for a significant population of isolated galaxies. Nearly all galaxies lie in low-mass clusters of the types called "groups" or "clouds"



(distinguished by their densities). These groups and clouds have radii which are small compared with their separations. They have low masses,  $M_{\text{calc}} < 2 \times 10^{13} M_{\odot}$ , and are sparsely populated,  $N_{\text{calc}} < 100$ . These systems have small velocity dispersions of  $\sigma < 200 \text{ km s}^{-1}$ . Of all their component galaxies, 79% are of late morphological type. Finally, these groups have little tendency toward central concentration.

#### d) Background Galaxies

Because our redshift survey is limited by a fixed apparent magnitude which corresponds to a rather bright intrinsic luminosity ( $M_p = -19.9$ ) at the distance of the Supercluster, the sample of galaxies lying behind the Supercluster is quite small. Consequently, we can draw only limited conclusions about their distribution. The only background galaxies that were recognized in earlier surveys are too faint to be included in our sample. These galaxies were discussed by Tift and Gregory (1976), who suggest that they are probably members of groups similar to those in the foreground.

We find evidence for an additional population of background galaxies with  $m_p < 15.0$  which lie within 20 Mpc of the Supercluster, having  $7900 < V_0 < 9500 \text{ km s}^{-1}$ . These galaxies are easily identified in Figure 3, which is a redshift histogram of those ICR galaxies that do not lie in groups. There are 50 galaxies plotted in the figure with  $6000 < V_0 < 9500 \text{ km s}^{-1}$ . An obvious peak is found at the redshift of the Supercluster ( $6900 \text{ km s}^{-1}$ ), and a sharp cutoff is found for  $V_0 < 6400 \text{ km s}^{-1}$ . We include the NGC 4615 group in Figure 3 to illustrate the large gap of  $\sim 25 \text{ Mpc}$  between the ICR and the highest-redshift group lying in front of the ICR. The redshift distribution of the ICR galaxies is skewed toward higher redshifts. The moment of skewness for all galaxies with  $V_0 > 6000 \text{ km s}^{-1}$  is  $\gamma = 1.33$  [ $\gamma = m_3/(m_2)^{3/2}$ , where  $m_2$  and  $m_3$  are the second and third moments about the mean, respectively]. Since no significant skewness is seen in the Coma cluster itself (Gregory and Tift 1976b), we suggest that the high-redshift tail is caused by the

TABLE 3  
BACKGROUND GALAXIES

Zwicky No.	Name	Type	$m_p$	$V_0$	Source†
127076S*	N 3926	E	14.7	7464	GT
127076NW	N 3926	E	14.7	8514	GT
158024	N 4104	SO	13.7	8473	CR
158072	N 4272	SO	14.2	8460	CR
158076	IC 3165	Sc	14.9	8428	CR
158100	N 4375	Sab	13.9	9034	CR
159011	N 4514	Sb	14.2	8011	CR
159022W	N 4556	E	14.4	7980	CR
159052		Sc	14.9	9377E	TG
159082		Sb	14.8	8174E	TG

\*included because of association with 127076NW

†CR = Chincarini and Rood (1976 + references therein)

GT = present study

TG = Tift and Gregory (1976 and references therein)

inclusion of  $\sim 10$  background galaxies. However, we cannot rule out the possibility that the ICR has an asymmetric distribution. The curve superposed on the histogram in Figure 3 is a normal distribution fitted to the remaining 40 ICR galaxies.

Before listing the possible background galaxies, we note two instances of CGCG apparent doubles which have one member with  $V_0 < 7900 \text{ km s}^{-1}$  (the apparent division between the Supercluster and the background) and one with  $V_0 > 7900 \text{ km s}^{-1}$ . Zw 159022w has  $V_0 = 7980 \text{ km s}^{-1}$ , and Zw 159022e has  $V_0 = 7395 \text{ km s}^{-1}$ . Since these two galaxies show no evidence of physical interaction, we consider them to be a chance optical pair. Zw 127076s has  $V_0 = 7464 \text{ km s}^{-1}$  and Zw 127076n has  $V_0 = 8514 \text{ km s}^{-1}$ . These two galaxies do seem to share a common envelope, and we place them both in the suggested background, since their mean is  $\bar{V}_0 = 7989 \text{ km s}^{-1}$ . In Table 3 we list the 10 galaxies that we consider to be located behind the Supercluster. In columns (1) and (2) the CGCG and NGC/IC identification numbers are given. In column (3) we give the new morphological classifications. Columns (4), (5), and (6) present  $m_p$ , the redshift, and the redshift source, respectively.

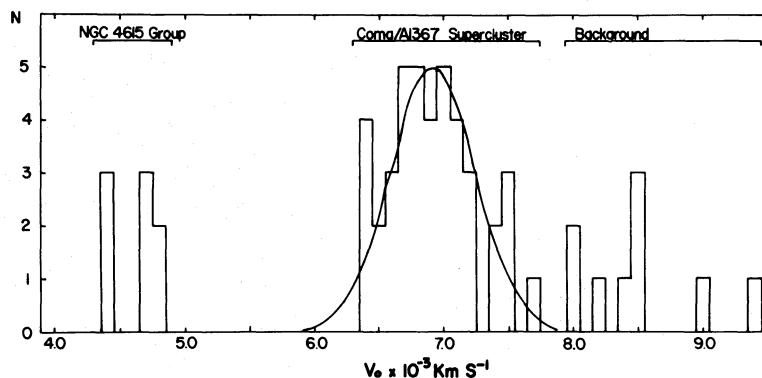


FIG. 3.—The redshift distribution of the isolated ICR galaxies plus the NGC 4615 group and the probable background. There is a very large gap in redshift between the ICR and the highest-redshift galaxies located directly in front of the ICR. The curve is a normal distribution which was fitted to the redshift distribution of the isolated ICR galaxies.

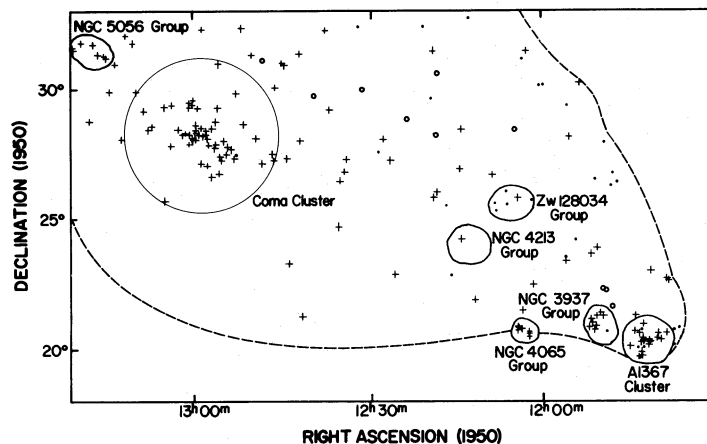


FIG. 4.—A map of the Supercluster. Dashed curve, approximate borders of our redshift survey. Solid curves, groups and rich clusters. Crosses, Supercluster galaxies. Open circles, the location of the probable background objects; small, filled circles, remaining galaxies with  $m_p < 15.0$  which do not have known redshifts.

#### e) Properties of the ICR Galaxies and the Structure of the Supercluster

In the preceding sections we listed both the foreground and background galaxies that are seen in our sample. The remaining galaxies are part of the Supercluster, and we devote the present section to an examination of their properties and spatial distribution. We identify two previously unrecognized populations of galaxies in the Supercluster that differ from each other and from the rich cluster population in distribution, dynamics, and component morphological types. These two newly recognized populations are (1) galaxies found in intermediate- or low-mass clusters and (2) a dispersed population of isolated galaxies.

In Figure 4 we show the area of the sky that contains the Supercluster. The two rich clusters and the Supercluster groups are outlined by solid curves. The dashed line shows the approximate borders of our survey area. Within the borders there are 31 galaxies with  $m_p < 15.0$  that do not have measured redshifts (this number does not include eight unobserved objects which are almost certainly members of the NGC 4005 group). Those galaxies known to be in the foreground have been omitted from Figure 4, so the map contains only the Supercluster galaxies (crosses), the 10 probable background galaxies (open circles), and the remaining unobserved galaxies (small filled circles). We estimate that  $\sim 20$  of the unobserved galaxies may be members of the Supercluster. Hence our redshift survey is approximately 89% complete in the indicated region of the sky.

The Supercluster groups have average projected densities which are quite high, approximately 9 times that of the isolated ICR galaxies. We also note that the Supercluster groups generally have higher central concentrations than those in the foreground, and there are no systems in the Supercluster comparable to the foreground clouds. Table 4 lists the properties of the individual galaxies in the four supercluster groups; we also include the NGC 5056 group, whose membership

in the Supercluster is doubtful. Although redshifts are not available for a total of eight listed galaxies, they are included with the groups because of their projected proximity to the known group members. In Table 5 we list the properties of the 40 isolated ICR galaxies. (The formats of Tables 4 and 5 are the same as that of Table 3.) The isolated galaxies are not strictly homogeneously distributed throughout the surveyed region. They show a general curving extension from Coma toward A1367 and an avoidance of the region south of the Coma cluster. This indicates that we have encountered the southern boundary to the Supercluster. The sharp boundary on the near side of the ICR is the only other well-determined border.

The isolated ICR galaxies may also have a tendency to congregate near the two rich clusters. To test this suggestion, we grouped these 40 galaxies into the portions of eight concentric annuli that intersect our surveyed region. The annuli were centered on the Coma core and contain five galaxies each. Over the distance range  $3^\circ < r < 12.5^\circ$  we find that the apparent two-dimensional number density,  $S$ , has a shallow falloff away from Coma;  $S \propto r^{-0.9 \pm 0.4}$ . This result agrees well with that found by Chincarini and Rood (1976),  $S \propto r^{-1.2 \pm 0.2}$ . A similar calculation based on annuli centered on A1367 yields  $S \propto r^{-0.5 \pm 0.1}$  over the distance range  $1^\circ < r < 11.5^\circ$ . We emphasize that these surface density falloffs do not characterize cluster profiles but refer only to the density of galaxies in the ICR (see further discussion in Thompson and Gregory 1978).

We can use these same isolated galaxies to determine whether there is any significant systematic variation of redshift across the Supercluster. Although A1367 has a significantly lower redshift than Coma, the isolated galaxies show only a very marginal trend in the same direction. A linear regression solution of redshift on projected distance along the line of separation of Coma and A1367 gives a result of  $10.2 \pm 9.7 \text{ km s}^{-1} \text{ degree}^{-1}$  variation from the mean of  $\bar{v}_0 = 6902 \text{ km s}^{-1}$ .

TABLE 4  
GALAXIES IN SUPERCLUSTER GROUPS

Zwicky No.	Name	Type	$m_p$	$V_0$	Source <sup>†</sup>	Zwicky No.	Name	Type	$m_p$	$V_0$	Source <sup>†</sup>
(a) <u>NGC 3937 Group</u>						(c) <u>Zw 128034 Group</u>					
127063	N 3910	S0	14.4	7768	GT	128004		Sm	14.9	-	
127080	N 3929	E/S0	14.5	7041	GT	128027	N 4101	S0	14.7	6089	GT
127082		Sd	14.7	6555E	DM	128034		S0	14.4	(6700)*	GT
127088	N 3937	S0 <sup>-</sup>	14.0	6554	GT	128037	I 762	S0 <sub>p</sub>	14.8	-	
127089	N 3940	S0 <sup>-</sup>	14.3	6341	GT	128045		S	14.6	-	
127090	N 3943	SBO	14.7	6559	GT	128047		S0	14.5	-	
127095	N 3947	Sc	14.2	6288E	DM	*bad comparison spectrum					
127098	N 3954	E	14.4	6800	GT	(d) <u>NGC 4213 Group</u>					
127100		S	14.9	6840	GT	128065	N 4213	E <sup>+</sup>	14.3	6986	GT
127072		Sbc	14.6	-		(e) <u>NGC 5056 Group</u>					
097161*	N 3919	E/S0	14.5	6052	GT	160173	N 5056	Sb	13.6	5481	TG
*membership uncertain						160176	N 5057	S0	14.6	5856	TG
(b) <u>NGC 4065 Group</u>						160181	N 5065	Sbc	14.3	5732	TG
128005	N 4061	E	14.4	7072	GT	160183	N 5074	Pec	14.7	5720	TG
128007	N 4065	S0 <sup>-</sup>	14.0	6216	GT	160202		-	14.9	5183	TG
128008	N 4066	S0	14.4	7294	GT	161030		S0	14.8	5088	TG
128009	N 4070	S0 <sup>-</sup>	14.3	7143	GT						
128012	N 4076	S0/a	14.3	-							
128020	N 4089	E:	14.9	6905	GT						
128023	N 4092	Sbc	14.4	6737	GT						
128025	N 4095	S0	14.6	7057	GT						
128026	N 4098	E <sub>p</sub>	14.5	7280	GT						
098032	N 4053	S0 <sup>+</sup>	14.6	-							
098034		Pec	14.8	-							

<sup>†</sup>DM = Dickens and Moss (1976)

GT = present study

TG = Tifft and Gregory (1976 and references therein)

To find the line-of-sight depth of the Supercluster, we will assume that the redshift dispersion is caused by differential Hubble expansion. This estimated thickness will be only an upper limit because we can *a priori* predict that there will be two other components contributing to the dispersion. One component,  $\sigma_{vir}$ , would be large if these galaxies were ever in virially relaxed groups. Another component,  $\sigma_p$ , represents the primordial random kinetic energy of the galaxies themselves. We assume  $\sigma_{vir} \ll \sigma_d$  and  $\sigma_p \ll \sigma_d$ , where  $\sigma_d$  is the dispersion caused by differential Hubble flow. For an operational definition of the characteristic depth, we use the difference in distances determined by a  $2\sigma$  spread from the mean. The observed  $\sigma = 318 \text{ km s}^{-1}$  then yields a thickness of  $6.4 h^{-1} \text{ Mpc}$ . Since this is only 30% of the apparent separation between Coma and A1367, the Supercluster is seen to be highly asymmetric. However, if the 10 background galaxies indicate an extension on the far side of the Supercluster, then its depth would be  $\sim 13 h^{-1} \text{ Mpc}$ .

Table 6 summarizes the general properties of the Supercluster systems; the format is the same as that of Table 2. Four of the eight systems (Coma, two groups, and the isolated ICR galaxies) have mean redshifts in the narrow range  $6900 < \bar{V}_0 < 7000 \text{ km s}^{-1}$ . A1367 and the Zw 128034 group have considerably lower values of  $\bar{V}_0 = 6450$  and  $6395 \text{ km s}^{-1}$ , respectively, and the NGC 3937 group has redshifts intermediate between the two extremes. The NGC 5056 group has  $\bar{V}_0 = 5510 \text{ km s}^{-1}$ , which is  $\sim 900 \text{ km s}^{-1}$  lower than

any system which is definitely part of the Supercluster. The line-of-sight velocity dispersions vary from  $\sigma \approx 300$  to  $\sigma \approx 1,000 \text{ km s}^{-1}$ .

The morphological data show significant differences among the populations. Of the foreground galaxies with  $M_p \leq M_i$ , 69% are spiral or related late types, while only 39% of all the Supercluster galaxies are spiral. Yet, within the Supercluster, we find that 59% of the isolated ICR galaxies are spiral, while spirals account for only 33% and 36% of the galaxies in rich clusters and groups, respectively. Since we are comparing morphologies for galaxies having a wide range in distances and hence diameters, we have compared morphologies judged from the Sky Survey (the source of most of our data) with independent morphologies determined from excellent 4 m prime focus plates of Coma and A1367. We find that the rough statistic of spiral percentage is relatively independent of the plate material and hence also of distance.

For those Supercluster groups where enough data exist, we have calculated the virial  $M/L$  ratios; they are found to range  $200 < M/L < 400$ .  $N_{calc}$  and  $m_{calc}$  were obtained as in § IIIc and show that the Coma cluster, having an estimated 1269 galaxies with  $M_p < -15.0$ , contributes 43% of the total number of Supercluster galaxies and 37% of the total luminosity. We estimate the total mass of the Supercluster to be  $8.4 \times 10^{14} M_\odot$  (assuming  $M/L$  ratios of 200, 200, and 100 for E, S0, and S galaxies); fully 50% of this mass is located in the Coma cluster itself.

TABLE 5  
ISOLATED SUPERCLUSTER GALAXIES

Zwicky No.	Name	Type	$m_p$	$V_0$	Source*
127025	N 3808	Sd	14.1	7050	DM
127025B	N 3808	S/SO	--	7230	DM
127038		Sc	14.0	6906	DM
127050		Sa	14.8	6736	GT
127086		E	14.8	6793	GT
127099	N 3951	S	14.5	6430	GT
127115	N 4003	S/SO	14.8	6438	GT
128003		Sd <sub>p</sub>	14.6	6476	GT
128017	N 4084	E	14.9	6621	GT
128054		SO <sup>-</sup>	14.6	7220	GT
128077	IC 780	E/SO	14.5	6779	GT
128078	IC 3171	E	14.8	6935	GT
128089	IC 791	Sab	14.2	6735	GT
129011	IC 3582	?	14.3	7113	CR
129012	IC 3581	Scd	14.9	6972	GT
129020	IC 3692	Sc	14.8	6412	GT
129022	IC 813	S <sub>p</sub>	14.4	7049E	TG
157054	N 3971	E <sup>+</sup>	13.9	6862	CR
157061	N 3988	E	14.7	6535	CR
158009		S	14.0	7462	CR
158033		E	14.4	6753	CR
158036	N 4146	Sbc	13.8	6461	CR
158053	N 4211	SO <sub>p</sub>	14.4	6752	CR
158054		S <sub>p</sub>	14.6	7689	CR
158081		Pec	14.5	6697	CR
158112	IC 3376	Sd	14.4	7078	CR
159005	IC 3407	Sc	14.7	7062	CR
159021	N 4555	E <sup>+</sup>	13.5	6685	CR
159022E	N 4556	E <sup>+</sup>	14.4	7395	CR
159037	N 4585	S <sub>p</sub>	14.6	7411E	TG
159038		SO <sub>p</sub>	14.6	6972	CR
159059		S <sub>p</sub>	14.5	7456E	TG
159061		Scd	14.8	7113E	TG
159070	N 4673	E	13.7	6990	BGC
159072N	N 4676	S <sub>p</sub>	14.1	6585	TG, BGC
159072S	N 4676	S <sub>p</sub>	--	6598	TG, BGC
159076	IC 821	Scd	14.5	6726	TG, K
159095	IC 826	Sbc	14.9	7153	TG
159103		SO	14.8	6894E	TG
160080		Sb	14.7	6844E	TG

\*BGC = de Vaucouleurs and de Vaucouleurs (1964)  
 CR = Chincarini and Rood (1976 + references therein)  
 DM = Dickens and Moss (1976)  
 GT = present study  
 K = Kintner (1971)  
 TG = Tift and Gregory (1976 + references therein)

#### IV. DISCUSSION

In the preceding portions of this paper, we have presented observations dealing with four distinct populations of galaxies that differ from one another in distribution, dynamics, and component morphological types. In the following discussion we will examine the implications which these observations have on the evolution of galaxy systems in general and on the Coma/A1367 Supercluster in particular.

Two of the four galaxy populations have been studied previously.

1. The properties of galaxies in the two rich clusters are known in detail. In addition to the references given in § II, analyses of the properties of these galaxies can be found in Rood *et al.* (1972), Gregory (1975), and Gregory and Tift (1976a, b). Here our major objective is to examine the environment in which these clusters are located. We note that the present-day separation between Coma and A1367 is  $24 h^{-1}$  Mpc. Hence

their relative separation (i.e., Hubble flow) velocity is  $2400 \text{ km s}^{-1}$  (joint gravitational attraction causes negligible deceleration). The dominant component of this velocity must be in the plane of the sky, since the line-of-sight velocity difference is only  $500 \text{ km s}^{-1}$ . This indicates that the separation vector between Coma and A1367 lies at an angle of  $\sim 12^\circ$  from the plane of the sky. We find no reason at present to speculate on possible orbital motion of the two clusters about a mutual center of mass.

2. Galaxies in sparse groups, such as those found in the foreground of the Supercluster, have also been studied before, but our findings show some new and unexpected results. Groups are found to have separations much larger than their radii, and the intergroup space is nearly devoid of galaxies. (Chincarini and Martins 1975 have suggested that the redshift distribution in the direction of the Hercules supercluster is also clumpy.) There are large regions of space with radii  $> 20 h^{-1}$  Mpc which contain no detectable galaxies, groups, or clusters, giving an upper limit to the detected mass density in these regions of  $\rho < 4 \times 10^{-34} \text{ g cm}^{-3}$ . A redshift survey now being done by Gregory, Thompson, and Tift (1978) which examines the supercluster surrounding A426 (Perseus), A347, and A262 shows that there exist even larger voids than any found in the present study.

It is an important challenge for any cosmological model to explain the origin of these vast, apparently empty regions of space. There are two possibilities: (1) the regions are truly empty, or (2) the mass in these regions is in some form other than bright galaxies. In the first case, severe constraints will be placed on theories of galaxy formation because it requires a careful (and perhaps impossible) choice of both  $\Omega$  (present mass density/closure density) and the spectrum of initial irregularities in order to grow such large density irregularities. If the second case is correct, then matter might be present in the form of faint galaxies, and an explanation would have to be sought for the peculiar nature of the luminosity function. Alternatively, the material might still be in its primordial gaseous form (either hot or cold neutral hydrogen), and the physical state of this matter may be similar to that discussed in a number of speculative papers (see Rees and Ostriker 1977). A search for radio radiation should be made in the direction of the voids.

##### a) The Supercluster Groups

Our census of groups within the ICR is probably complete for (1) groups with at least one galaxy having  $m_p < 15.0$ , and (2) groups with easily recognizable central concentrations. As an example, because the charts in CGCG extend 0.8 mag fainter than our survey, we were able to discern the presence of the NGC 4213 group even though NGC 4213 itself is the only bright galaxy. It will be important to eventually push the redshift survey in the Supercluster to  $m_p = 15.7$ , the limit of the Zwicky catalog. Undetected groups that do not meet the criteria given above may exist within the Supercluster.

TABLE 6  
SUPERCLUSTER SYSTEMS

Name	Type	$N_{\text{obs}}^{(1)}$	$N_{\text{calc}}^{(2)}$	$\bar{V}_0$	$\sigma_v$	Morphology (% Spiral)	$\log L_{\text{obs}}^{(1,2,3)}$	$\log M_{\text{calc}}^{(2,3,4,5)}$ (4)	(5)	Virial M/L	$R_h$ (degrees)	$\log \rho^{(2,3,4,5)}$ ( $M_\odot \text{ Mpc}^{-3}$ )
Coma*	rich cluster	66	1269	6947	~1000	27	12.17	14.63	13.87	2x10 <sup>3</sup>	0.96	12.85
Coma†	cluster core	33	635	6870	944	15	11.89	14.39	13.68		0.43	13.67
A1367†	rich cluster	24	400	6373	715	46	11.73	13.93	13.11	2x10 <sup>3</sup>	0.45	13.25
NGC 3937	group	9	196	6680	306	44	11.35	13.80	12.97	293	0.44	13.08
NGC 4065	group	11	212	6963	354	15	11.39	13.87	13.08	205	0.35	13.40
Zw 128034	group	6	100	6395	-	33	10.99	13.41	12.55	-	0.62	12.30
NGC 4213	group	1	22	6986	-	0	10.41	12.99	12.39	-	-	-
NGC 5056	group	6	71	5510	316	67	10.94	13.14	12.09	384	0.43	12.70
Isolated ICR	-	40	785	6902	318	59	11.97	14.12	13.29	-	-	-

NOTES: (1)  $m_p < 15.0$   
 (2) calculated for  $M_p \leq -15.0$   
 (3) solar units  
 (4)  $M/L = 200$  for E and S0 galaxies;  $M/L = 100$  for spirals  
 (5)  $M/L = 50$  for E galaxies, 30 for S0s, and 7 for spirals  
 (6) assuming  $H = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$

\*out to radius =  $3^\circ$

†out to radius =  $1^\circ$

Our estimates of the masses and richnesses of clusters are limited by the accuracy of the assumed luminosity function. For faint galaxies in groups there is some evidence that the slope of the integrated luminosity function might be flatter than the Abell luminosity function used in § IIIc (Gregory and Thompson 1977; Felten 1977). Therefore we might have systematically overestimated  $N_{\text{calc}}$  and  $\mathcal{M}_{\text{calc}}$  for Supercluster groups as compared with the foreground groups, since corrections to observed quantities are larger for the more distant systems.

Two independent lines of argument confirm that, even if we have overestimated  $N_{\text{calc}}$  and  $\mathcal{M}_{\text{calc}}$  for the Supercluster systems, the Supercluster groups would still be found more massive than the foreground groups. One argument is that the NGC 4065 and NGC 3937 groups each contains at least eight galaxies with  $M_p \leq -19.9$ , while no foreground system has more than four galaxies that satisfy the same inequality (see Fig. 2). Any reasonable luminosity function would indicate that groups containing many bright galaxies are richer and more massive than systems with few bright galaxies. The second argument is that the line-of-sight velocity dispersions of the NGC 4065 and NGC 3937 groups are higher than any found in the foreground systems. If all of these groups are gravitationally bound, the higher dispersions of the Supercluster groups imply higher masses.

One of the other two Supercluster groups, Zw 128034, also has a mass larger than any of the foreground systems. Unfortunately, five of the brighter galaxies ( $m_p < 15.0$ ) in this system have not had their redshifts determined. It would be useful to see whether its velocity dispersion is also larger than those of the foreground groups. The fourth system, the NGC 4213 group, clearly has a very low mass, but  $N_{\text{calc}}$  and  $\mathcal{M}_{\text{calc}}$  are uncertain because only one galaxy is bright enough to be in our survey.

### b) The Isolated ICR Galaxies

The only galaxies in our sample that are not located in distinct groups, clouds, or clusters are those we find dispersed within the Supercluster. It is of some importance to determine whether these isolated ICR galaxies are truly primordial "field" galaxies or, alternatively, if they are the remnants of tidally disrupted groups or clouds. If it can be shown that the isolated galaxies are remnants of disrupted groups, then it follows that all galaxies were located within discrete clusters (or groups or clouds) at an early stage of their development. This idea is an alternative to the view that groups, clouds, and clusters grow from small irregularities in the initially smooth galaxy distribution (cf. Press and Schechter 1974; Peebles 1974).

If we hypothesize that the primordial galaxy systems within the ICR were similar to those systems now seen in the foreground sample, the following observations support the idea that dynamic interactions could produce the present-day ICR configuration:

i) The two least-dense foreground systems, the NGC 4615 and NGC 4793 clouds, would be disrupted by tidal interactions if they were located within  $10 h^{-1} \text{ Mpc}$  of the Coma cluster or  $2.5 h^{-1} \text{ Mpc}$  of A1367.

ii) Spirals dominate the least-dense foreground clouds, and we find that the isolated ICR galaxies have the highest spiral incidence among the Supercluster systems.

iii) The isolated galaxies have a weak tendency to congregate near the two rich clusters (see § IIIe). This effect could have two origins. One is that the developing clouds nearest to Coma and A1367 would be the most effectively disrupted. The other is that the two rich clusters attract more than half the galaxies dispersing from a cloud even if the velocity vectors of the galaxies were initially isotropic. (A galaxy located

10 Mpc from the Coma cluster could be completely decelerated from an initial  $100 \text{ km s}^{-1}$  separation velocity in  $\sim 5 \times 10^9 \text{ yr.}$ ) This process is reminiscent of the cosmological infall discussed by Gunn and Gott (1972), except the infalling material comes not from a homogeneously distributed "field" but from the highly asymmetric distribution of Supercluster clouds and groups. It is likely that intergalactic gas, if present, would possess a distribution similar to that of the visible galaxies and would therefore also be infalling asymmetrically.

iv) The existing ICR groups are found to lie closer to A1367 than to Coma; this is expected because the more massive cluster should be more effective at disrupting small systems.

Although the present data are not conclusive, it seems likely that the evolution of the structure of the ICR was dominated by tidal interactions with Coma and A1367. We look forward to dynamical simulations of this picture.

#### c) Epoch of Cluster Formation

If we adopt the conventional viewpoint that groups and clusters were formed by dissipationless collapse, we can use the observations in the present survey to calculate the epoch of cluster formation. Observationally the problem is simple. We determine  $V_f$ , the fraction of the total volume which clusters or groups occupy at the present epoch, and then use the relation  $(Z_f + 1) = V_f^{-1/3}$  to find the redshift of formation  $Z_f$  which is identified with the epoch when the borders of all groups and clusters were in direct contact with one another. Since our total survey volume was selected to include two rich clusters, we will consider only the foreground sample of groups and clouds out to the redshift limit of  $5500 \text{ km s}^{-1}$ . The small portion of this volume occupied by the groups themselves is

$$V_g = \frac{4}{3}\pi \sum (2R_h)^3 \quad (1)$$

where the sum is taken over all groups,  $R_h$  is the harmonic mean radius of each group ( $\pi/2$  times the projected harmonic mean radius listed in Table 2), and the factor of 2 in parentheses corrects for the reduction in radius which occurs when a group becomes virialized. If we define  $V_f = V_g/V_t$ , then

$$V_t = \frac{4}{3}\pi \left( \frac{55}{h} \text{ Mpc} \right)^3 \times \frac{260}{41,253}$$

where  $260 \text{ degree}^2$  is the area in the sky over which the survey was made. Using the cluster radii from Table 2 in equation (1), we find

$$V_f = \frac{V_g}{V_t} = \frac{1}{549}.$$

This implies that  $1 + Z_f \approx 10$ . If the cluster-formation process included dissipation, then a tightly bound cluster which appears to have formed at high redshift could have formed more recently. We conclude that the redshift of formation for the foreground groups is  $Z_f \lesssim 9$ .

#### d) The Morphologies of Galaxies

The various galaxy systems that are found in our sample show a wide range in the simple morphology index, %S, the fractional number of component galaxies that are spiral or related late type. Figure 5 shows a plot of this morphological index versus mass density of the system (using  $M/L = 200, 200, 100$ ). Two of the galaxy systems that we have identified are not represented in Figure 5 because of the small number of observed galaxies in each. These are the NGC 3798 group and the NGC 4213 group. The isolated ICR galaxies are also not shown in Figure 5 because of difficulty in defining a meaningful mass density. The remaining systems given in Tables 2 and 6 are represented in the following manner: open circles indicate clouds; filled circles indicate foreground

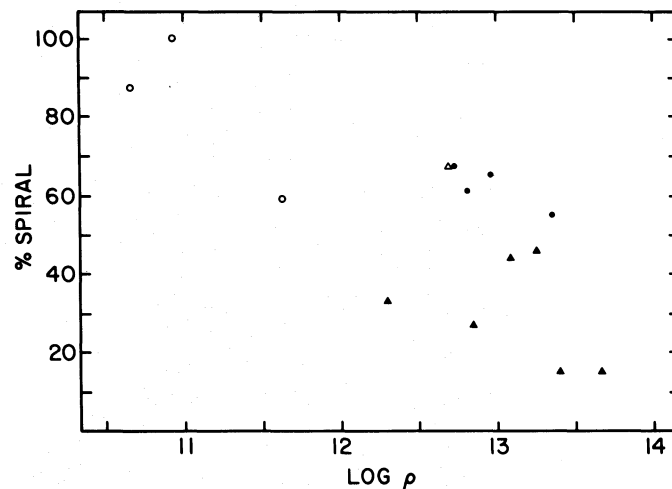


FIG. 5.—A plot of the morphology index versus the logarithm of the volume mass density (in units of  $M_\odot \text{ Mpc}^{-3}$ ). The Supercluster systems are represented by solid triangles and are found to have the highest densities and lowest spiral incidence. The foreground clouds (open circles) have the lowest densities and highest incidence of spirals. The foreground groups (small, filled circles) and the NGC 5056 group (open triangle) lie between the extremes of  $\rho$  and %S.

groups; filled triangles represent Supercluster systems; the NGC 5056 group is shown as an open triangle.

The data plotted in Figure 5 show a moderate correlation ( $r = -0.74$ ), but the statistical significance of the distribution comes from points with extreme values of  $\rho$  and  $\%S$ . Those systems with intermediate values of  $\rho$  show a wide range in  $\%S$ . It is also significant that the points are segregated according to population. The systems which are called clouds because of their low densities have the highest incidence of spirals. The Supercluster systems have the lowest spiral incidence. It is also interesting that the NGC 5056 group, which lies near the Supercluster but has differing dynamical properties, lies near the foreground groups in this diagram.

#### e) General Speculations

Our purpose has been to study one supercluster in detail. However, when the Coma/1367 Supercluster is considered along with the other nearby superclusters, at least two features are of note.

Coma and A1367 have a very wide separation, forming a supercluster which is morphologically different from the others. Since important physical processes may manifest themselves by morphological properties, it will eventually be necessary to have a classification scheme for superclusters. A formal scheme should await detailed studies of more exam-

ples, but we can suggest the following three classes on the basis of the nearby examples:

I. *Single core/halo superclusters*.—The prototype is the Local Supercluster, which is centered on Virgo and contains many outlying groups.

II. *Binary superclusters*.—The prototypes are Coma/A1367 (widely separated) and A2197/2199 (nearly in contact).

III. *Extended linear superclusters*.—The prototype for this class is the extensive chain of clusters extending from A426 (Perseus) through A347, A262, and onto NGC 507 and NGC 383 groups.

The final speculation is based on the fact that Coma and A1367 complete an important set of clusters. In Abell's (1958) catalog there are only five clusters with distance class  $d \leq 2$  and richness class  $\geq 2$ . Superclusters containing Hercules, Perseus, and A2199 were previously recognized (e.g., Rood 1976). Coma and A1367 now complete the set. *Every nearby very rich cluster is located in a supercluster*. We suggest that all  $\geq 2$  clusters will eventually be found to lie in superclusters. Perhaps such very massive objects can form only in close association with other clusters.

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## APPENDIX

### DEFINITION OF GROUP MEMBERSHIP

The lowest-redshift group is the Coma I cloud. Since Gregory and Thompson (1977) gave a map and a list of member galaxies, we list only its general properties in Table 2. The remaining seven foreground systems are mapped in Figure 6, and we list their member galaxies in Tables 7a–7g; the columns of these tables give the same information as those of Table 3.

The next lowest redshift system after the Coma I cloud has redshifts in the range  $2190 < V_0 < 2860 \text{ km s}^{-1}$ . We refer to this system as the NGC 4793 cloud, and it was also recognized by Tift and Gregory (1976). In Figure 6, the NGC 4793 cloud lies near the eastern boundary of the survey, and Tift and Gregory list two probable

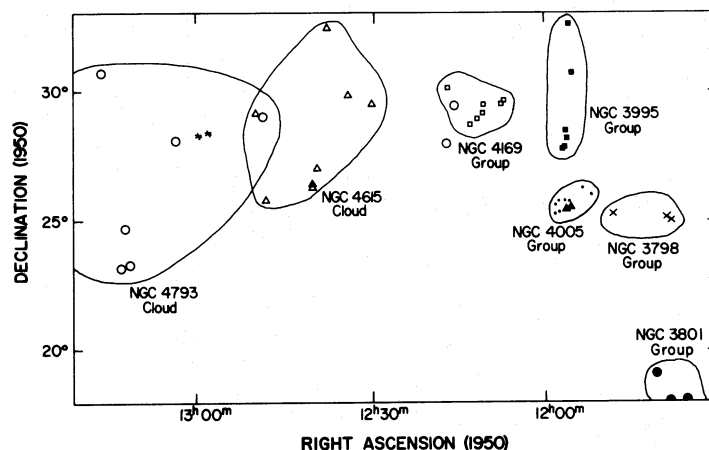


FIG. 6.—A map of seven of the eight foreground systems. (A map of the Coma I cloud is given in Gregory and Thompson 1977.) Two galaxies with redshifts similar to those in the NGC 4793 cloud are seen as open circles projected against the NGC 4169 group. Two other galaxies, lying at the center of the Coma cluster, are shown by star-shaped symbols. These have redshifts similar to those in the NGC 4615 cloud. Small, filled circles within the borders of the NGC 4005 group represent probable members with unknown redshifts.

TABLE 7  
GALAXIES IN FOREGROUND GROUPS

Zwicky No.	Name	Type	$m_p$	$V_0$	Source*	Zwicky No.	Name	Type	$m_p$	$V_0$	Source*
(a) NGC 4793 Group						(e) NGC 4169 Group					
130016	N 5012	Sb	13.6	2566	TG	158029	N 4131	S/SO	14.1	3697	CR
130019	N 5016	Sa	14.3	2769	TG	158030	N 4132	S/SO	14.6	4056	CR
130020		Im	14.8	2592	TG	158031	N 4134	Sbc	13.8	3845	CR
158064	I 777	S	14.5	2607	CR	158041	N 4169	SO	12.9	3829	CR
158073	N 4275	?	13.4	2292	CR	158042		?	14.8	4034	CR
159116	N 4793	Sb	12.3	2504	BGC	158044	N 4174	S/SO	14.3	4150	CR
160134	N 4961	Sb <sub>p</sub>	13.5	2582	TG, BGC	158045	N 4175	S	14.2	4050	CR
160194	N 5089	S <sub>p</sub>	14.4	2190	TG	158047	N 4185	Sb	13.5	4058	CR
						158050	N 4196	E/SO <sub>p</sub>	13.7	3966	CR
						158061	N 4253	Sd	13.7	3869	CR
(b) NGC 3801 Association						(f) NGC 4005 Group					
097025	N 3764	Pec	14.9			127101		SO <sup>-</sup>	14.9		
097030	N 3768	S/SO	13.7	3288	GT	127106	I 746	S	14.5		
097031	N 3767	SBO	14.5			127110	N 3987	Sbc	14.4	4508	GT
097032		Sd	14.8			127112	N 3993	SO/a	14.8		
097040		S	14.8			127114	N 3997	Sd	14.3		
097043	N 3790	S/SO	14.5			127120	N 4005	Sa	14.1	4333	GT
097045		S:	14.6			127122	N 4015	SO	14.2		
097048		S <sub>p</sub>	14.3			127123	N 4018	S	14.7		
097050		SBO	14.6			127125	N 4022	SBO	14.4		
097051	N 3801	SO <sub>p</sub>	13.3	3356	GT	127127	N 4023	E/SO	14.6		
097052	N 3802	S	14.7								
097054	N 3806	Sc	14.6								
097067		Sm	14.3								
097070	N 3827	Sc	13.6	3143	DM						
(c) NGC 3798 Group						(g) NGC 4615 Group					
127022	N 3798	S	13.9	3459	GT	129015	N 4614	Sd	14.2	4848	TG, CR
127027	N 3812	SO	13.9	3529	GT	129018	N 4615	Sd	13.8	4736	TG, CR
127064	N 3920	?	14.1	3547	GT	129025	N 4712	Sc	13.5	4456	CR
(d) NGC 3995 Group						159009	N 4495	S	14.1	4361	CR
157060		SO	14.5	3194	CR	159019		Scd	14.9	4702	CR
157065	N 4004	Sc <sub>p</sub>	14.0	3420	CR	159039		Sc <sub>p</sub>	14.0	4375	CR
157066	N 4008	SO <sup>-</sup>	13.1	3578	CR	159050	I 3651	E	14.4	4777	TG
157068		Sm	14.6	3466	CR	159092	N 4738	Sbc	14.9	4726	TG, K
157069	N 4016	Sd	13.5	3323	CR						
186075	N 3995	Sm	12.9	3356	BGC						

\*BGC = de Vaucouleurs and de Vaucouleurs (1964)  
 CR = Chincarini and Rood (1976 and references therein)  
 DM = Dickens and Moss (1976)  
 GT = present study  
 K = Kintner (1971)  
 TG = Tifft and Gregory (1976 and references therein)

members beyond our borders. Two other galaxies, NGC 4275 and IC 777, are shown in the figure as open circles, the same symbol used for the galaxies whose membership in the cloud is certain. However, these two galaxies lie more than  $5^\circ$  from the rest of the cloud, near the NGC 4169 group. A discussion of the possibility that this system is dispersing can be found in the main body of the paper. Table 7a summarizes the data for the galaxies associated with this cloud.

Between  $3000$  and  $4000 \text{ km s}^{-1}$ , the galaxies have a complicated distribution. Chincarini and Rood (1976) grouped all of these galaxies together, but the present evidence shows several different mass concentrations. We first mention the three galaxies shown near the lower right portion of Figure 6. These appear to be part of a loose grouping which we name after NGC 3801. The three members with known redshift have  $3143 < V_0 < 3356$ . More members of this group may lie to the south of A1367 where no redshifts are available.

About  $6^\circ$  north of the NGC 3801 group are three galaxies with only slightly higher redshifts,  $3459 < V_0 < 3547 \text{ km s}^{-1}$ . These are part of a very sparse group that we name after NGC 3798. Five degrees farther north and east we find a line of galaxies extending northward. These six galaxies have redshifts in the range  $3194 < V_0 < 3578 \text{ km s}^{-1}$  and will be referred to as the NGC 3995 group, although we note that NGC 3995 is the northernmost member and its physical association with the other five galaxies is not certain.



These last three groups are scattered over  $14^\circ$  ( $\sim 10$  Mpc), but the total range of known redshifts is only  $435 \text{ km s}^{-1}$ , so they may form a tenuously related association of sparse clusters. The properties of their constituent galaxies are given in Tables 7b, 7c, and 7d.

At somewhat higher redshift we find a much more tightly concentrated cluster which will be referred to as the NGC 4169 group. The redshift range is  $3697 < V_0 < 4150 \text{ km s}^{-1}$  with a mean of  $\bar{V}_0 = 3955 \text{ km s}^{-1}$  and a dispersion of  $\sigma = 133 \text{ km s}^{-1}$ . This is the group that was named after NGC 4131 by Tift and Gregory (1976), and Chincarini and Rood (1976) referred to it as we do but included galaxies from the NGC 3995 group.

Five degrees southwest of the NGC 4169 group is a concentrated group with only two known redshifts. Since NGC 4005 is the brightest with  $m_p = 14.1$ , we name the cluster after it. Eight additional galaxies with unknown redshifts are probably associated with this group and are shown as small filled circles in Figure 6.

The highest redshift system that is clearly in the foreground is the NGC 4615 cloud. (The NGC 5056 group is probably not associated with the Supercluster, but we cannot be certain.) Redshifts in this group lie in the range  $4361 < V_0 < 4848 \text{ km s}^{-1}$ . Since the lowest redshifts in the center of the Coma cluster itself fall in the upper part of this range, there may be confusion about the membership of individual galaxies. However, the general distribution of low-redshift objects in Coma is very tightly concentrated near the center of the cluster (see Tift and Gregory 1976, where fainter galaxies show the effect clearly), and the distribution of objects in the NGC 4615 cloud is very loose. Therefore, in general, Coma cluster galaxies can easily be distinguished. Two low-redshift Coma galaxies are shown in Figure 6 with star-shaped symbols. Finally, we point out that the NGC 4615 cloud may be an important object for study, since it is the least-dense cluster, group, or cloud that we have found in this survey.

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*Note added in proof.*—The redshifts reported by Dickens and Moss (1976) are not referred to a galactocentric reference frame as are all other redshifts used in this paper. However, since the galactic rotation corrections are typically only about  $-60 \text{ km s}^{-1}$  for the DM galaxies, our general results are not significantly affected.

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